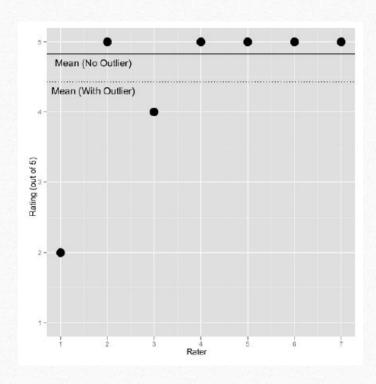
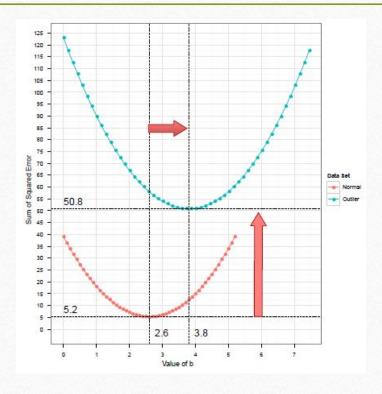


# Exploring Assumptions

Normality and Homogeneity of Variance

## **Outliers Impact**





## Assumptions

Parametric tests based on the normal distribution assume:

- Additivity and linearity
- Normality something or other
- Homogeneity of Variance
- Independence

## Additivity and Linearity

- The outcome variable is, in reality, linearly related to any predictors.
- If you have several predictors then their combined effect is best described by adding their effects together.
- If this assumption is not met then your model is invalid.

## Normality Something or Other

The normal distribution is relevant to:

- Parameters
- Confidence intervals around a parameter
- Null hypothesis significance testing

This assumption tends to get incorrectly translated as 'your data need to be normally distributed'.

# When does the Assumption of Normality Matter?

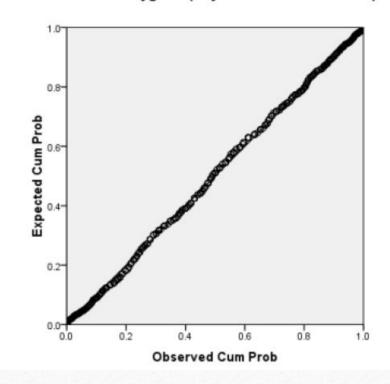
- In small samples The central limit theorem allows us to forget about this assumption in larger samples.
- In practical terms, as long as your sample is fairly large, outliers are a much more pressing concern than normality.

# Spotting Normality

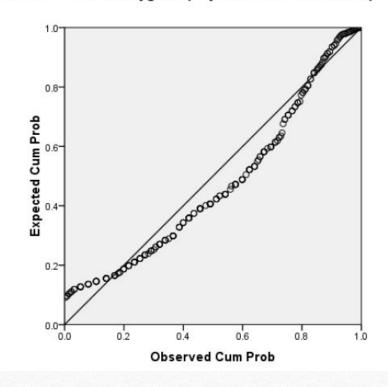
- We don't have access to the sampling distribution so we usually test the observed data
- Central Limit Theorem
  - If N > 30, the sampling distribution is normal anyway
- Graphical displays
  - P-P Plot (or Q-Q plot)
  - Histogram
- Values of Skew/Kurtosis
  - 0 in a normal distribution
  - Convert to z (by dividing value by SE)
- Kolmogorov-Smirnov Test
  - Tests if data differ from a normal distribution.
  - Significant = non-Normal data
  - Non-Significant = Normal data

### The P-P Plot

Normal P-P Plot of Hygiene (Day 1 of Download Festival)



#### Normal P-P Plot of Hygiene (Day 2 of Download Festival)



## Assessing Skew and Kurtosis

| LAHAHAA                | .401 | .020  | .004  |
|------------------------|------|-------|-------|
| Skewness               | 004  | 1.095 | 1.033 |
| Std. Error of Skewness | .086 | .150  | .218  |
| Kurtosis               | 410  | .822  | .732  |
| Std. Error of Kurtosis | .172 | .299  | .433  |
| Range                  | 2.67 | 3.44  | 3 30  |

#### **Tests of Normality**

|   | Kolmogorov-Smirnov <sup>a</sup> |     | Shapiro-Wilk |           |     |      |
|---|---------------------------------|-----|--------------|-----------|-----|------|
|   | Statistic                       | df  | Sig.         | Statistic | df  | Sig. |
| Hygiene (Day 1 of<br>Download Festival) | .083                            | 810 | .000         | .654      | 810 | .000 |

a. Lilliefors Significance Correction

 $H_0$ : Normality can be assumed.

 $H_1$ : Normality cannot be assumed.

K-S Test

D(810)=0.083, sig=0.000(<0.05)

This test is significant

Reject  $H_0$ 

Conclusion: It is not a normal distribution.

# Homoscedasticity/ Homogeneity of Variance

- When testing several groups of participants, samples should come from populations with the same variance.
- In correlational designs, the variance of the outcome variable should be stable at all levels of the predictor variable.
- Can affect the two main things that we might do when we fit models to data:
  - Parameters
  - Null Hypothesis significance testing

# Assessing Homoscedasticity/ Homogeneity of Variance

Graphs (see lectures on regression)

#### Levene's Tests

- Tests if variances in different groups are the same.
- Significant = Variances not equal
- Non-Significant = Variances are equal

#### Variance Ratio

- With 2 or more groups
- VR = Largest variance/Smallest variance
- If VR < 2, homogeneity can be assumed.

Test of Homogeneity of Variance

|                 |                                      | Levene Statistic | df1 | df2    | Sig. |
|-----------------|--------------------------------------|------------------|-----|--------|------|
| Age of surveyer | Based on Mean                        | .985             | 2   | 56     | .380 |
|                 | Based on Median                      | .499             | 2   | 56     | .610 |
|                 | Based on Median and with adjusted df | .499             | 2   | 36.562 | .611 |
|                 | Based on trimmed mean                | .872             | 2   | 56     | .424 |

 $H_0$ : Homogeneity of Variance can be assumed.

 $H_1$ : Homogeneity of Variance cannot be assumed.

#### Levene's Test

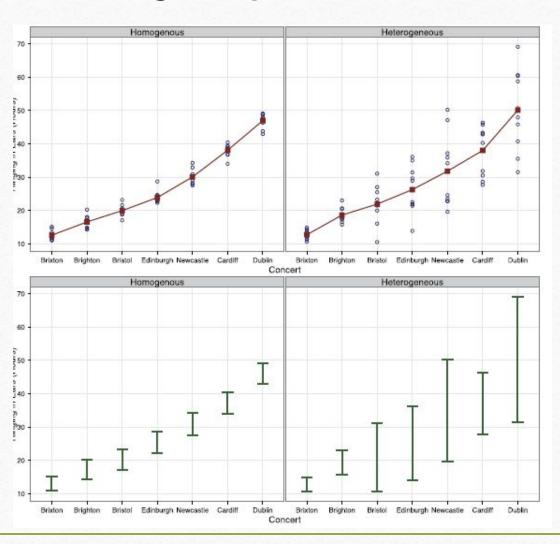
F(2.56)=0.985, sig =0.380 (>0.05)

This test is non-significant.

Accept  $H_0$ 

Conclusion : The variances are about the same in different groups

### **Homogeneity of Variance**



## Independence

- The errors in your model should not be related to each other.
- If this assumption is violated: Confidence intervals and significance tests will be invalid.

## Reducing Bias

- Trim the data: Delete a certain amount of scores from the extremes.
- Windsorizing: Substitute outliers with the highest value that isn't an outlier
- Analyze with Robust Methods: Bootstrapping
- Transform the data: By applying a mathematical function to scores

## Trimming the Data



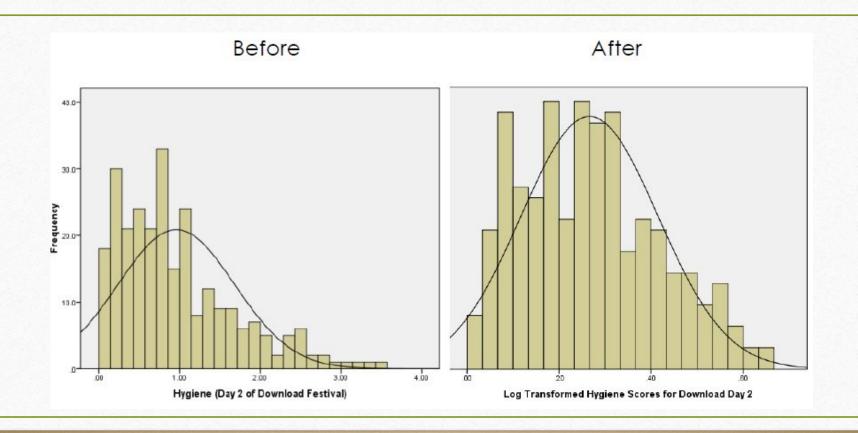
### Robust Methods

|                      | Comparing Treatments        | Relationships           |
|----------------------|-----------------------------|-------------------------|
| Principle            | Bootstrap                   | Bootstrap               |
|                      | Trimmed Means               | Least Trimmed Squares   |
|                      | M-estimators                | M-estimators            |
|                      | Median                      | Least Median of Squares |
|                      |                             |                         |
| Equivalen<br>t Tests | T-test                      | Correlation             |
|                      | ANOVA (Including factorial) | Regression              |
|                      | ANCOVA                      | ANCOVA                  |
|                      | MANOVA                      |                         |

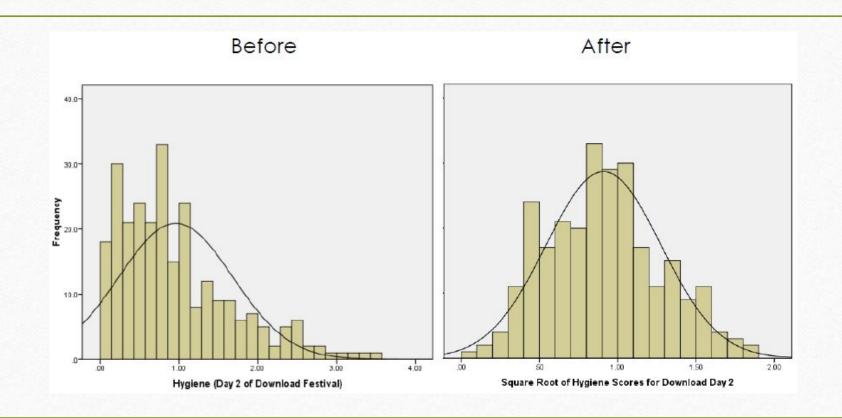
## Transforming Data

- Log Transformation ( $log(x_i)$ ): Reduce positive skew.
- Square Root Transformation  $(\sqrt{x_i})$ : Also reduces positive skew. Can also be useful for stabilizing variance.
- Reciprocal Transformation  $(1/x_i)$ : Dividing 1 by each score also reduces the impact of large scores. This transformation reverses the scores, you can avoid this by reversing the scores before the transformation,  $1/(x_{Highest}-x_i)$ .

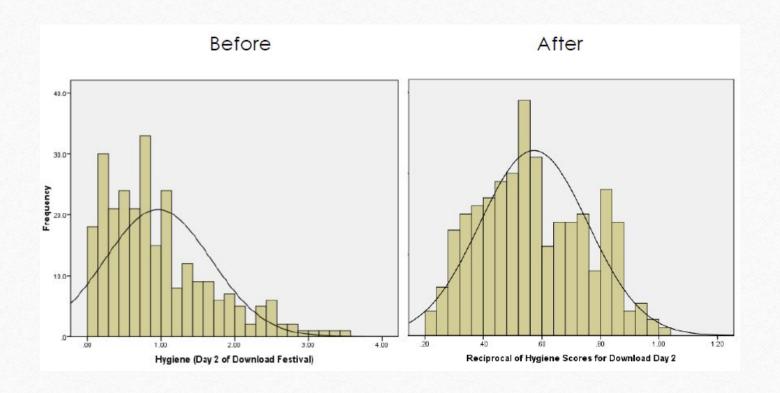
## Log Transformation



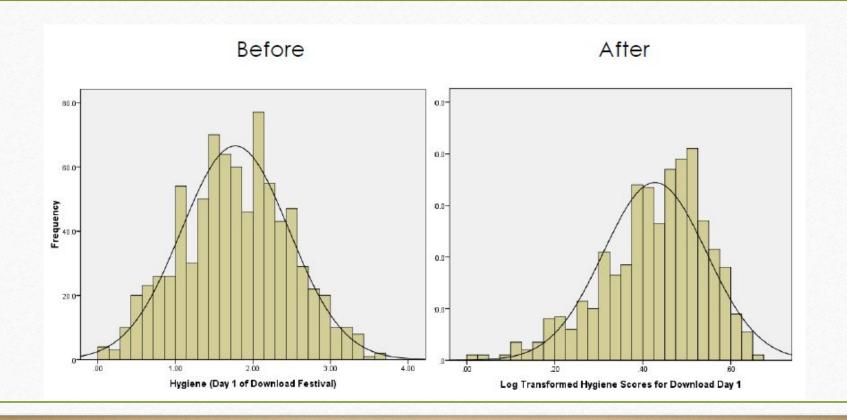
## Square Root Transformation



## Reciprocal Transformation



## But ...



### To Transform ... Or Not

Transforming the data helps as often as it hinders the accuracy of F (Games & Lucas, 1966).

#### Games (1984):

- The central limit theorem: sampling distribution will be normal in samples > 40 anyway.
- Transforming the data changes the hypothesis being tested
- E.g. when using a log transformation and comparing means you change from comparing arithmetic means to comparing geometric means
- In small samples it is tricky to determine normality one way or another.
- The consequences for the statistical model of applying the 'wrong' transformation could be worse than the consequences of analysing the untransformed scores.