



# Phase Formation Rules for High Entropy Alloys

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# Acknowledgements

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# Outlines

- I. Background & Motivations
- II. Results & Discussions
- III. Summaries



# I. Background & Motivations

# 1.1 Alloys Design Strategy

(1) Conventional alloys

Alloy=
$$A+\delta B+\delta C+$$
;  $A>50\%$ ; ...

Steel, A=Fe, B=Carbon, δB<2%;

Cast Iron, A=Fe, B=Carbon, δB<6.5%







## (2) High Entropy Alloys

HEAs=A+B+C+D+E;  $50\%<A\setminus B\setminus C\setminus D\setminus E>15\%$ 

#### **FCC type HEA Solid Solution**

CoCrCuFeNi=HEA,

Yeh, MMTA, 2004;

#### **BCC** type HEA Solid Solution

AlCoCrFeNi=HEA,

Zhou, APL, 2007

Al<sub>20</sub>[TiVMnHEA]<sub>80</sub>,

Zhou, MSEA, 2007





## 1.2 Thermodynamically

$$S = X_A S_A + X_B S_B + \Delta S_{mix}$$

For the regular solution:

$$\Delta S_{mix} = -R(X_A L n X_A + X_B L n X_B)$$



Solid solution has higher entropy than the mechanical mixture does.





 $G_{\scriptscriptstyle A}$ 

 $G_{\!\scriptscriptstyle B}$ 

Gibbs Free Energy

$$\Delta G_{mix} = G_{AB} - (X_A G_A + X_B G_B)$$

$$G_{AR}$$

$$\Delta G_{mix} = \Delta H_{mix} - T\Delta S_{mix}$$







## 1.3 Properties and Applications

## **Properties**

- 1. High Strength; Zhou, APL, 2007;
- 2. High wear resistance; Lin, Surface Coating technology, 2008.
- 3. High corrosion resistance; Lee, Thin Solid Films, 2008;
- 4. High thermo-stability; Tsai, APL, 2008.







## **Potential Applications**

1 Coatings, Barriers, etc.

Diffusion barriers for Cu interconnections; Tsai, APL, 2008

- 2 Structural Materials
- 3 Energy Storage Materials,

Raju, Journal of power Sources, 2008;

4 Molds





#### 1.4 Motivations

To understand what is the dominant factors for the phase formation of the HEAs

#### 1 Atomic radius, or atomic volume;

**Atomic Radius** 

The contents of Al, Ti, Cu, Co in the HEAs were changed

$$\delta = \sqrt{\sum_{i=1}^{N} c_i (1 - r_i / \bar{r})^2}$$

$$\bar{r} = \sum_{i=1}^{N} C_i r_i$$

## 2 Enthalpy of Mixing;

$$\Delta H_{mix} = \sum_{i=1, i \neq j}^{N} \Omega_{ij} c_i c_j$$

## 3 Entropy of Mixing

$$\Delta S_{mix} = -R \sum_{i=1}^{N} C_i LnC_i$$







## 4 Cooling Rate

Critical cooling rate? Like the BMG?

## 5 Tensile and compressive properties

Tensile elongation=0? Like BMG?







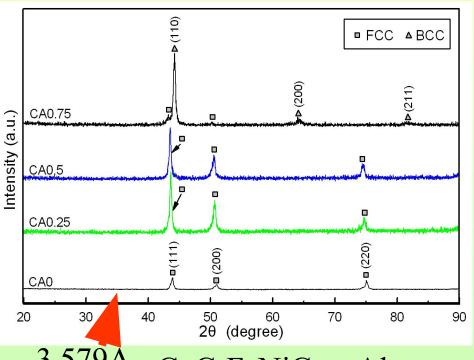
## II. Results & Discussions

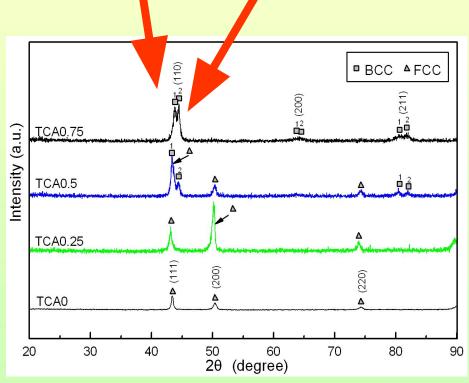
## 2.1. Alloying with different atomic size, Al, Cu, Co, Ti

Al=1.438A

(y=0, 0.25, 0.5, 0.75)

2.913A,2.872A





CoCrFeNiCu<sub>1-v</sub>Al<sub>v</sub>

Ti<sub>0.5</sub>CoCrFeNiCu<sub>1-v</sub>Al

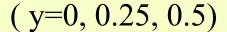


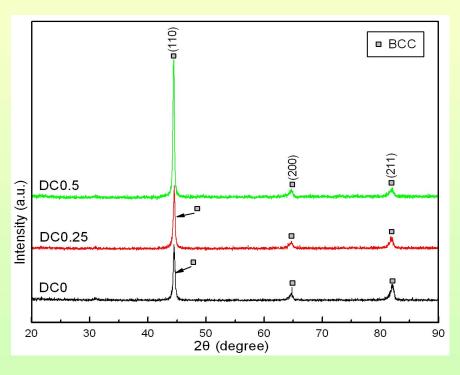
FCC BCC, High APE to Lower APE, with larger atoms Al

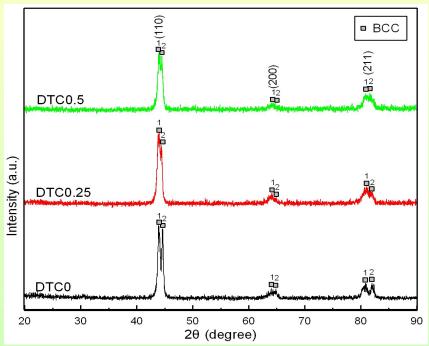




#### Cu = 1.278A







CoCrFeNiAlCu<sub>y</sub>

Ti<sub>0.5</sub>CoCrFeNiAlCu<sub>y</sub>

No PHASE TRANSITION





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 $C_0=1.251A$ 

Biger BCC1phase:2.913A;

Smaller BCC2phase:2.872A

The smaller BCC transit to FCC firstly after adding Co

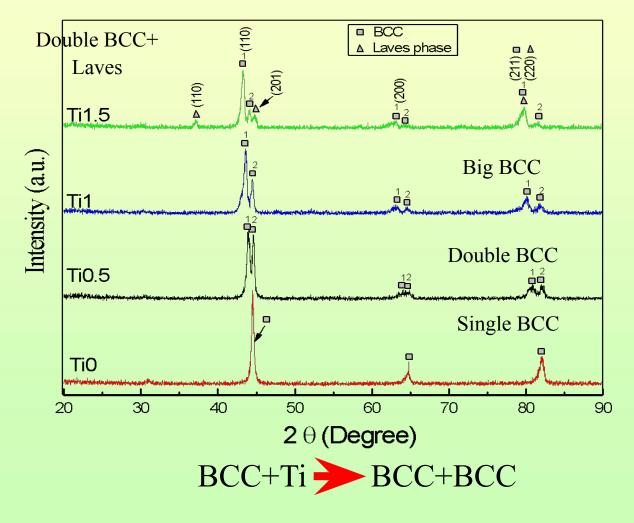






#### Ti=1.448A

## [Al<sub>1</sub>Co<sub>1</sub>Cr<sub>1</sub>Fe<sub>1</sub>Ni<sub>1</sub>]Ti<sub>x</sub> alloys









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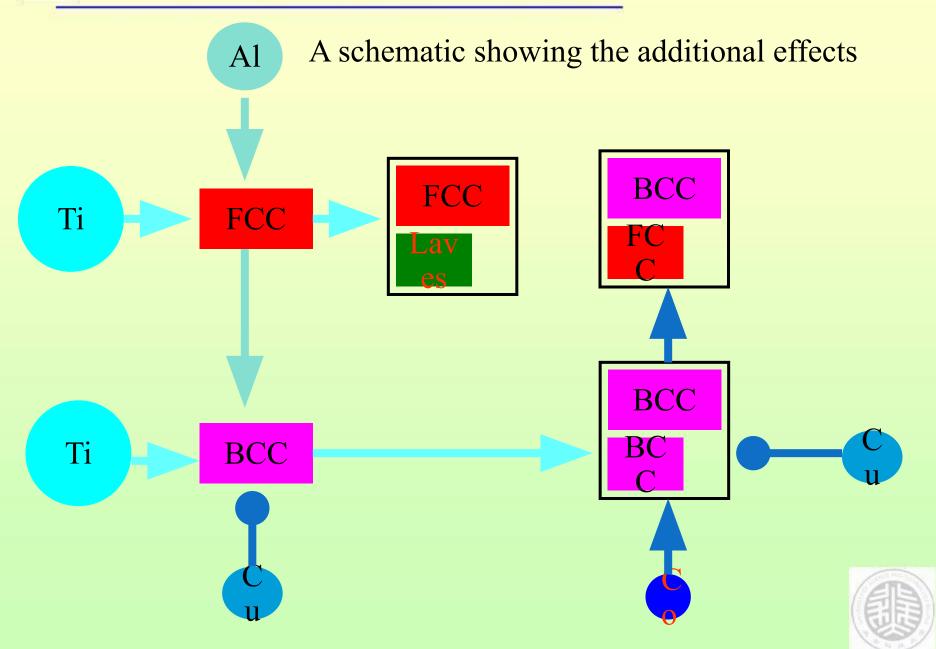
The transition is mainly lattice distortion induced and APE related





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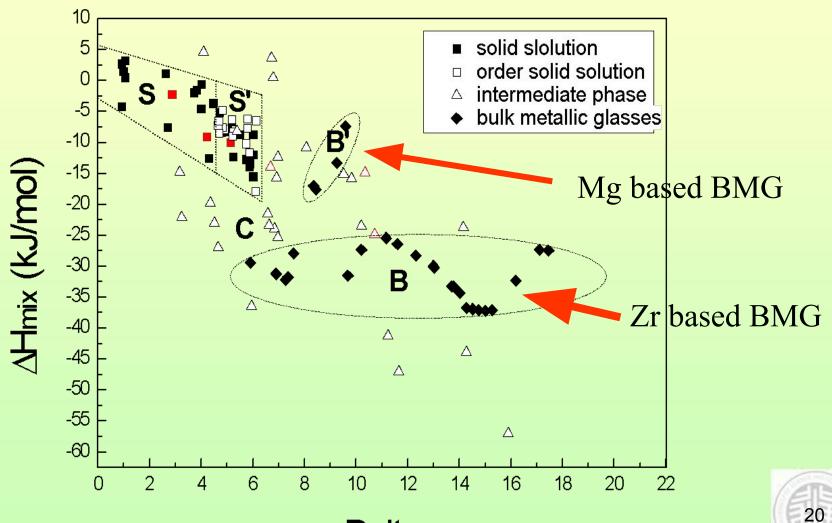
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# 2.2. Considering of the enthalpy of mixing $\Delta H_{mix}$



Zhang, AEM, 2008

Delta



## 2.3. Considering of the entropy of mixing $\Delta S_{mix}$

#### Adam - Gibbs 方程

$$\eta = \eta_0 \times \exp\left[\frac{C}{TS_c(T)}\right]$$

Here, C is a free enthalpy barrier to cooperative rearrangements. high entropy of mixing will lead to low viscosity, and a high mobility of the atoms in the liquid, thus a lower glass forming ability, this maybe the reason why the entropy of mixing for the bulk metallic glass forming alloys generally have a lower entropy of mixing , this maybe in some contradiction to the confusion principle.

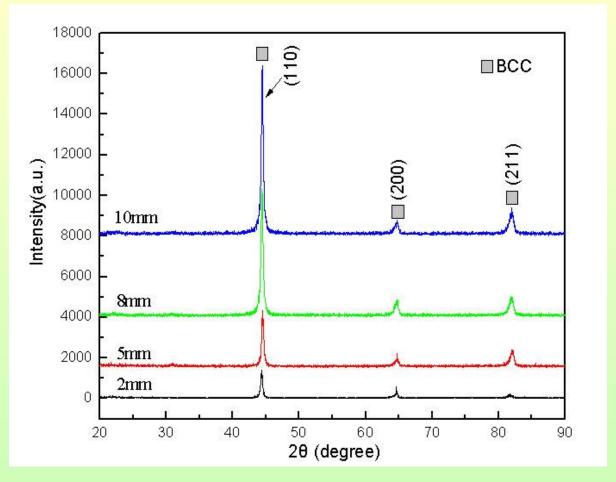
High Entropy is not good for the formation of BMG







## 2.4 Cooling Rate



AlCoCrFeNi



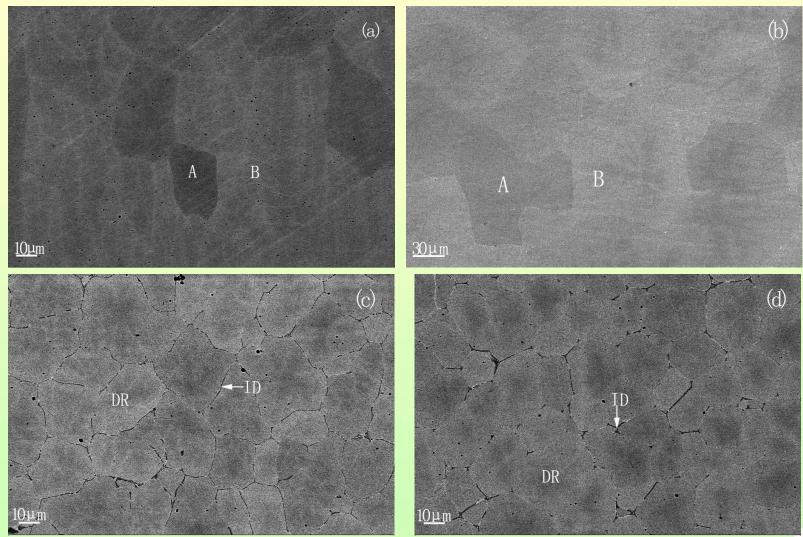




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2mm 5mm



8mm

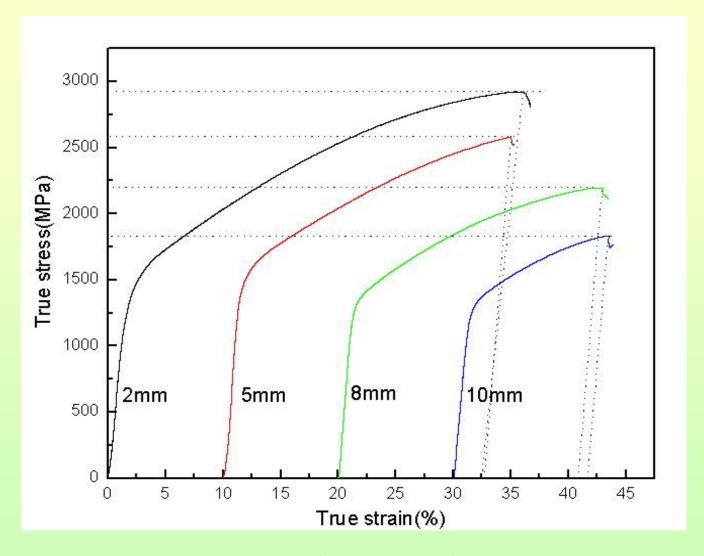
AlCoCrFeNi

10mm





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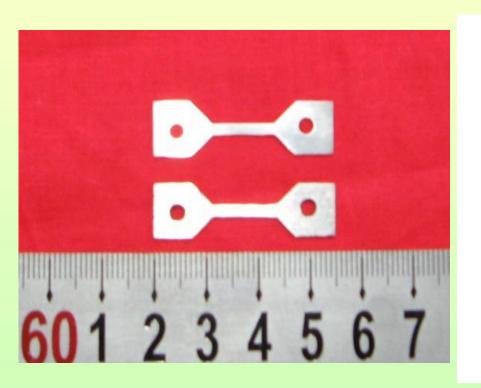
AlCoCrFeNi

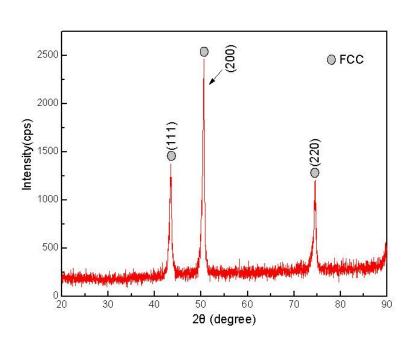






## 2.5 Tensile and Compressive properties





XRD pattern for the CoCrCuFeNiAl<sub>0.5</sub> alloy.



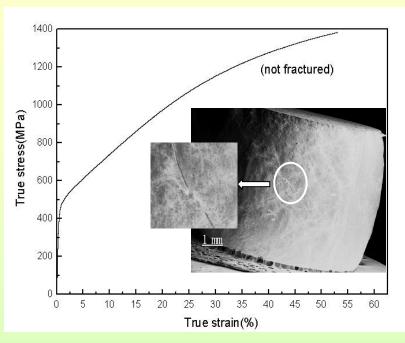




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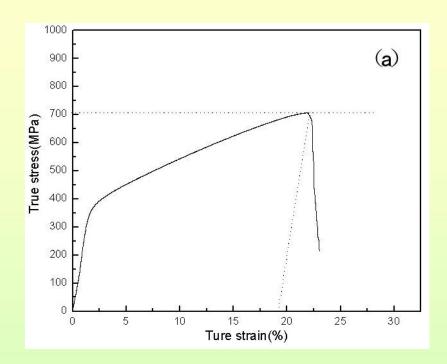


Table Room temperature mechanical test results for the CoCrCuFeNiAl0.5 alloy

This alloy	ε <sub>p</sub> (%)	ε <sub>0.2</sub> (MPa)	o (MPa)
Compres sive	>51.5	460	>1380
Tensile	19.1	360	707

 $\varepsilon_{\rm P}$ : plastic strain;  $\varepsilon_{0.2}$ : yield strength;  $\sigma_{\rm max}$ : compressive/tensile strength





## III. Summaries

- 1 Atomic size mismatch is the dominant factor for the phase formation of the high entropy alloys;
- 2 The formation of solid solution for the HEAs intends to have enthalpy of mixing close to zero;
- 3 High entropy of mixing facilitates the formation of the solid solution rather than the BMGs;
- 4 Cooling rate plays rather important role for the homogeneous microstructure than for the phase formation;
- 5 HEA can have tensile elongations as high as 19%.





# Thanks for your attention

