

# *Chapter 13*

# **Capital Budgeting Techniques**



# ***After studying Chapter 13, you should be able to:***

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- Understand the payback period (PBP) method of project evaluation and selection, including its: (a) calculation; (b) acceptance criterion; (c) advantages and disadvantages; and (d) focus on liquidity rather than profitability.
- Understand the three major discounted cash flow (DCF) methods of project evaluation and selection – internal rate of return (IRR), net present value (NPV), and profitability index (PI).
- Explain the calculation, acceptance criterion, and advantages (over the PBP method) for each of the three major DCF methods.
- Define, construct, and interpret a graph called an “NPV profile.”
- Understand why ranking project proposals on the basis of IRR, NPV, and PI methods “may” lead to conflicts in ranking.
- Describe the situations where ranking projects may be necessary and justify when to use either IRR, NPV, or PI rankings.
- Understand how “sensitivity analysis” allows us to challenge the single-point input estimates used in traditional capital budgeting analysis.
- Explain the role and process of project monitoring, including “progress reviews” and “post-completion audits.”



# ***Capital Budgeting Techniques***

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- **Project Evaluation and Selection**
- **Potential Difficulties**
- **Capital Rationing**
- **Project Monitoring**
- **Post-Completion Audit**



# ***Project Evaluation: Alternative Methods***

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- **Payback Period (PBP)**
- **Internal Rate of Return (IRR)**
- **Net Present Value (NPV)**
- **Profitability Index (PI)**



## ***Proposed Project Data***

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**Julie Miller is evaluating a new project for her firm, (*BMW*). She has determined that the after-tax cash flows for the project will be **\$10,000**; **\$12,000**; **\$15,000**; **\$10,000**; and **\$7,000**, respectively, for each of the **Years 1 through 5**. The initial cash outlay will be **\$40,000**.**



# ***Independent Project***

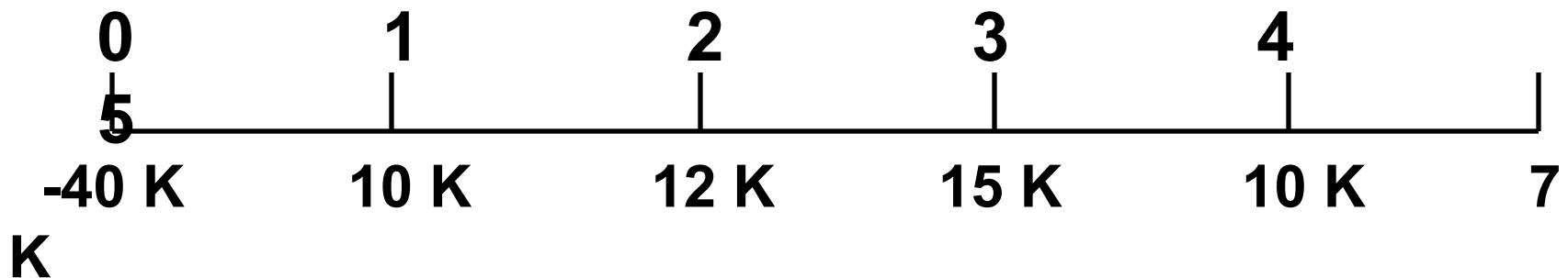
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- For this project, assume that it is **independent** of any other potential projects that *Basket Wonders* may undertake.
- **Independent** -- A project whose acceptance (or rejection) does not prevent the acceptance of other projects under consideration.



# *Payback Period (PBP)*

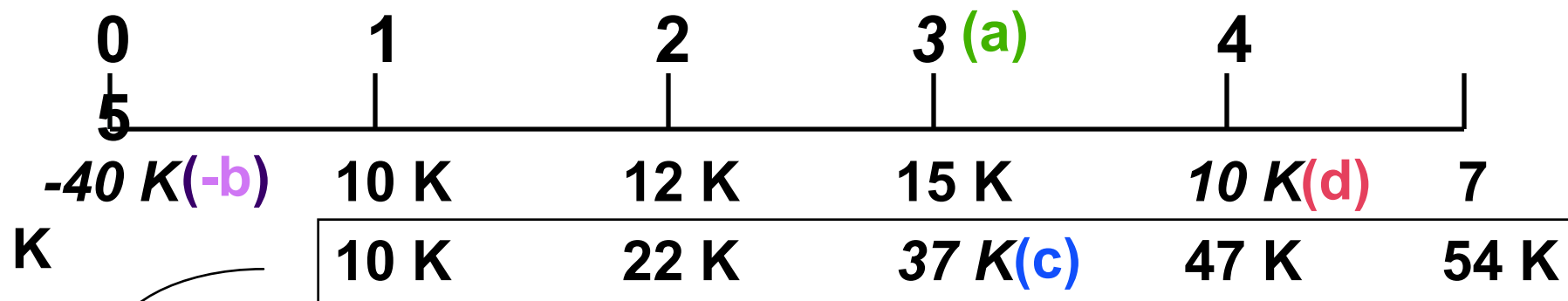
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**PBP** is the period of time required for the cumulative expected cash flows from an investment project to equal the initial cash outflow.



# Payback Solution (#1)



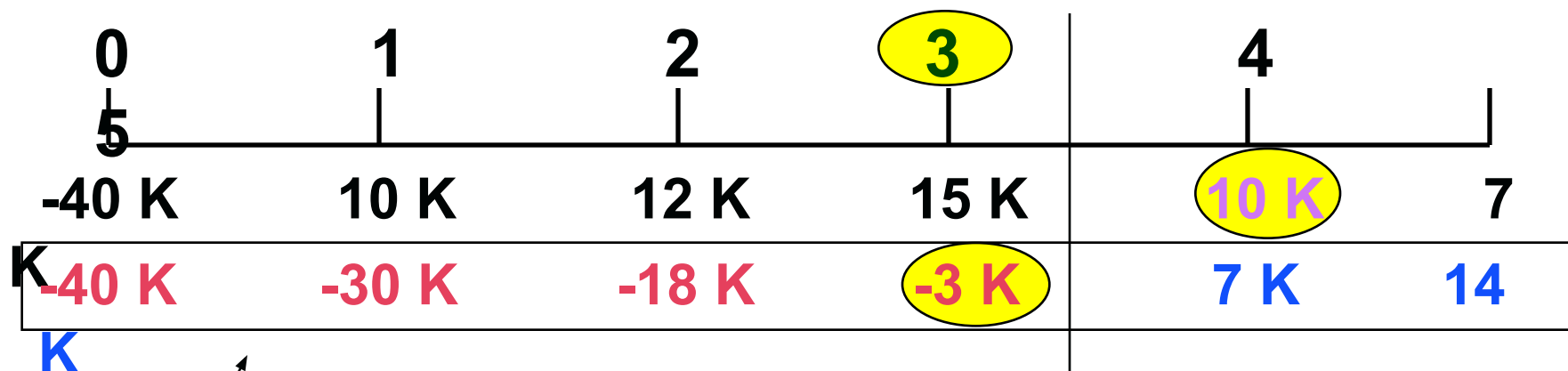
Cumulative  
Inflows

$$\begin{aligned}
 \text{PBP} &= a + (b - c) / d = \\
 &3 + (40 - 37) / 10 = 3 + \\
 &(3) / 10 = 3.3 \text{ Years}
 \end{aligned}$$





# Payback Solution (#2)



Cumulative  
Cash Flows

$$\text{PBP} = 3 + (3\text{K}) / 10\text{K}$$
$$= 3.3 \text{ Years}$$

**Note: Take absolute value of last negative cumulative cash flow value.**



# ***PBP Acceptance Criterion***

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The management of *Basket Wonders* has set a maximum PBP of **3.5 years** for projects of this type.

**Should this project be accepted?**

**Yes!** The firm will receive back the initial cash outlay in less than 3.5 years. [**3.3 Years** < **3.5 Year Max.**]



# ***PBP Strengths and Weaknesses***

## **Strengths:**

- Easy to use and understand
- Can be used as a measure of liquidity
- Easier to forecast ST than LT flows

## **Weaknesses:**

- Does not account for TVM
- Does not consider cash flows beyond the PBP
- Cutoff period is subjective

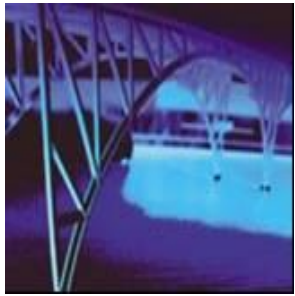


# *Internal Rate of Return (IRR)*

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**IRR** is the discount rate that equates the present value of the future net cash flows from an investment project with the project's initial cash outflow.

$$\text{ICO} = \frac{\text{CF}_1}{(1+\text{IRR})^1} + \frac{\text{CF}_2}{(1+\text{IRR})^2} + \dots + \frac{\text{CF}_n}{(1+\text{IRR})^n}$$



# *IRR Solution*

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$$\begin{aligned} \$40,000 = & \frac{\$10,000}{(1+IRR)^1} + \frac{\$12,000}{(1+IRR)^2} + \\ & \frac{\$15,000}{(1+IRR)^3} + \frac{\$10,000}{(1+IRR)^4} + \frac{\$7,000}{(1+IRR)^5} \end{aligned}$$

Find the interest rate (*IRR*) that causes the discounted cash flows to equal **\$40,000**.



# ***IRR Acceptance Criterion***

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The management of *Basket Wonders* has determined that the **hurdle rate** is **13%** for projects of this type.

**Should this project be accepted?**

**No!** The firm will receive **11.57%** for each dollar invested in this project at a cost of **13%**. [ **IRR < Hurdle Rate** ]



# ***IRR Strengths and Weaknesses***

## **Strengths:**

- **Accounts for TVM**
- **Considers all cash flows**
- **Less subjectivity**

## **Weaknesses:**

- **Assumes all cash flows reinvested at the IRR**
- **Difficulties with project rankings and Multiple IRRs**



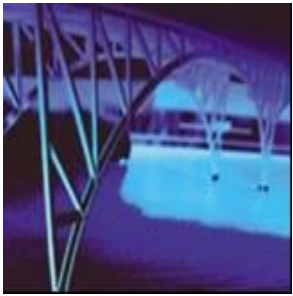
# *Net Present Value (NPV)*

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***NPV* is the present value of an investment project's net cash flows minus the project's initial cash outflow.**

$$\text{NPV} = \frac{\text{CF}_1}{(1+k)^1} + \frac{\text{CF}_2}{(1+k)^2} + \dots + \frac{\text{CF}_n}{(1+k)^n} - \text{ICO}$$





# NPV Solution

**Basket Wonders** has determined that the appropriate **discount rate (k)** for this project is **13%**.

$$\text{NPV} = \frac{\$10,000}{(1.13)^1} + \frac{\$12,000}{(1.13)^2} + \frac{\$15,000}{(1.13)^3} + \frac{\$10,000}{(1.13)^4} + \frac{\$7,000}{(1.13)^5} - \$40,000$$



# ***NPV Acceptance Criterion***

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The management of *Basket Wonders* has determined that the **required rate** is **13%** for projects of this type.

**Should this project be accepted?**

**No!** The **NPV** is negative. This means that the project is reducing shareholder wealth. [**Reject** as  **$NPV < 0$**  ]



# ***NPV Strengths and Weaknesses***

## **Strengths:**

- **Cash flows assumed to be reinvested at the hurdle rate.**
- **Accounts for TVM.**
- **Considers all cash flows.**

## **Weaknesses:**

- **May not include managerial options embedded in the project. See Chapter 14.**



# ***Profitability Index (PI)***

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**PI is the ratio of the present value of a project's future net cash flows to the project's initial cash outflow.**

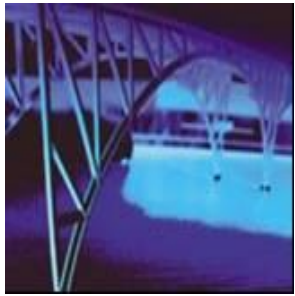
Method #1:

$$PI = \left[ \frac{CF_1}{(1+k)^1} + \frac{CF_2}{(1+k)^2} + \dots + \frac{CF_n}{(1+k)^n} \right] \div ICO$$

<< OR >>

Method #2:

$$PI = 1 + [ NPV / ICO ]$$



# ***PI Acceptance Criterion***

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$$\begin{aligned} \text{PI} &= \$38,572 / \$40,000 \\ &= .9643 \text{ (Method \#1, 13-34)} \end{aligned}$$

**Should this project be accepted?**

**No!** The **PI** is less than 1.00. This means that the project is not profitable.  
[*Reject as  $PI < 1.00$*  ]



# ***PI Strengths and Weaknesses***

## **Strengths:**

- **Same as NPV**
- **Allows comparison of different scale projects**

## **Weaknesses:**

- **Same as NPV**
- **Provides only relative profitability**
- **Potential Ranking Problems**



# ***Evaluation Summary***

## ***Basket Wonders Independent Project***

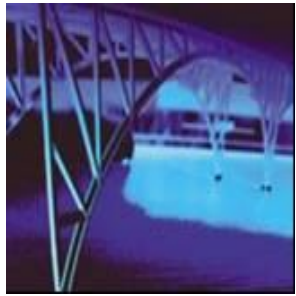
<b>Method</b>	<b>Project</b>	<b>Comparison</b>	<b>Decision</b>
PBP	3.3	3.5	<b>Accept</b>
IRR	11.47%	13%	<b>Reject</b>
NPV	-\$1,424	\$0	<b>Reject</b>
PI	.96	1.00	<b>Reject</b>



# ***Other Project Relationships***

- ***Dependent*** -- A project whose acceptance depends on the acceptance of one or more other projects.
- ***Mutually Exclusive*** -- A project whose acceptance precludes the acceptance of one or more alternative projects.





# ***Potential Problems Under Mutual Exclusivity***

**Ranking of project proposals *may* create contradictory results.**

**A. Scale of Investment**

**B. Cash-flow Pattern**

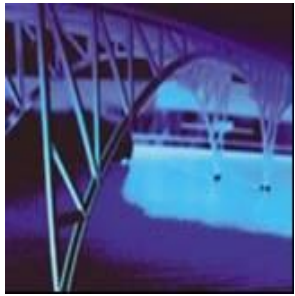
**C. Project Life**



## ***A. Scale Differences***

**Compare a small (S) and a large (L) project.**

<b>END OF YEAR</b>	<b>NET CASH FLOWS</b>	
	<b>Project S</b>	<b>Project L</b>
<b>0</b>	<b>-\$100</b>	<b>-\$100,000</b>
<b>1</b>	<b>0</b>	
<b>0</b> <b>2</b>	<b>\$400</b>	
<b>\$156,250</b>		



# ***Scale Differences***

**Calculate the PBP, IRR, NPV@10%,  
and PI@10%.**

**Which project is preferred? Why?**

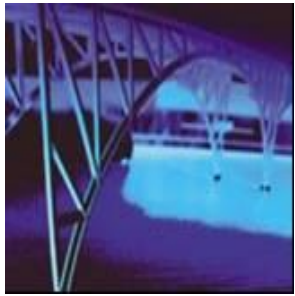
<b><u>Project</u></b>	<b><u>IRR</u></b>	<b><u>NPV</u></b>	<b><u>PI</u></b>
<b>S</b>	<b>100%</b>	<b>\$ 231</b>	<b>3.31</b>
<b>L</b>	<b>25%</b>	<b>\$29,132</b>	<b>1.29</b>



## ***B. Cash Flow Pattern***

Let us compare a *decreasing* cash-flow (D) project and an *increasing* cash-flow (I) project.

END OF YEAR	NET CASH FLOWS	
	Project D	Project I
0	-\$1,200	-\$1,200
1	1,000	
100 2	500	
600 3	100	
1,080		



# Cash Flow Pattern

Calculate the IRR, NPV@10%,  
and PI@10%.

Which project is preferred?

<u>Project</u>	<u>IRR</u>	<u>NPV</u>	<u>PI</u>
D	23%	\$198	1.17
I	17%	\$198	1.17



# ***Capital Rationing***

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***Capital Rationing*** occurs when a constraint (or budget ceiling) is placed on the total size of capital expenditures during a particular period.

**Example:** Julie Miller must determine what investment opportunities to undertake for ***Basket Wonders (BW)***. She is limited to a **maximum expenditure of \$32,500 only** for this capital budgeting period.



# *Available Projects for BW*

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<u>Project</u>	<u>ICO</u>	<u>IRR</u>	<u>NPV</u>	<u>PI</u>
A	\$ 500	18%	\$ 50	1.10 B
5,000	25	6,500	2.30 C	5,000 37
5,500	2.10	D 7,500	20	5,000
1.67 E	12,500	26	500	1.04 F
15,000	28	21,000	2.40	G 17,500
19	7,500	1.43 H	25,000	15
6,000	1.24			



# Choosing by IRRs for BW

Project	ICO	IRR	NPV	PI	
C	\$ 5,000	37%	\$ 5,500	2.10	F
15,000	28	21,000	2.40	E	12,500
500	1.04	B	5,000	25	6,500
2.30					

Projects C, F, and E have the three largest IRRs.

The resulting *increase* in shareholder wealth is \$27,000 with a \$32,500 outlay.





# Choosing by NPVs for BW

<u>Project</u>	<u>ICO</u>	<u>IRR</u>	<u>NPV</u>	<u>PI</u>		
F	\$15,000	28%	\$21,000	2.40	G	
17,500	19	7,500	1.43	B	5,000	25
6,500	2.30					

Projects F and G have the two  
*largest NPVs.*

The resulting *increase* in *shareholder wealth*  
is *\$28,500* with a *\$32,500 outlay.*



# Choosing by PIs for BW

Project	ICO	IRR	NPV	PI
F	\$15,000	28%	\$21,000	2.40
B	5,000	25	6,500	2.30
C	37	5,500	2.10	D
D	5,000	1.67	G	17,500
G	1.43		19	7,500

Projects F, B, C, and D have the four *largest PIs*.

The resulting *increase* in *shareholder wealth* is **\$38,000** with a **\$32,500** outlay.



# *Summary of Comparison*

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<u>Method</u>	<u>Projects Accepted</u>	<u>Value Added</u>
PI	F, B, C, and D	\$38,000
NPV	F and G	\$28,500
IRR	C, F, and E	\$27,000

**PI** generates the *greatest increase* in *shareholder wealth* when a limited capital budget exists for a *single period*.



# ***Single-Point Estimate and Sensitivity Analysis***

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**Sensitivity Analysis**: A type of “what-if” uncertainty analysis in which variables or assumptions are changed from a base case in order to determine their impact on a project’s measured results (such as NPV or IRR).

- Allows us to change from “*single-point*” (i.e., revenue, installation cost, salvage, etc.) estimates to a “*what if*” analysis
- Utilize a “base-case” to compare the impact of individual variable changes
  - E.g., Change forecasted sales units to see impact on the project’s NPV



# ***Post-Completion Audit***

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## **Post-completion Audit**

**A formal comparison of the actual costs and benefits of a project with original estimates.**

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- **Identify any project weaknesses**
- **Develop a possible set of corrective actions**
  - **Provide appropriate feedback**

**Result: Making better future decisions!**



## ***Multiple IRR Problem\****

Let us assume the following cash flow pattern for a project for Years 0 to 4:

**-\$100 +\$100 +\$900 -\$1,000**

**How many *potential* IRRs could this project have?**

**Two!!** There are as many potential IRRs as there are sign changes.

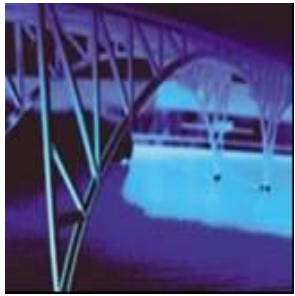
***\* Refer to Appendix A***



# Modified rate of return

- The modified internal rate of return (MIRR) is a financial measure of an investment's attractiveness. It is used in capital budgeting to rank alternative investments of equal size. As the name implies, MIRR is a modification of the internal rate of return (IRR) and as such aims to resolve some problems with the IRR.

$$\left( \frac{-\text{NPV}(rrate, values[positive]) * (1 + rrate)^n}{\text{NPV}(frate, values[negative]) * (1 + frate)} \right)^{\frac{1}{n-1}} - 1$$



# MIRR

- To calculate the MIRR, we will assume a finance rate of 10% and a reinvestment rate of 12%. First, we calculate the present value of the negative cash flows (discounted at the finance rate):  $PV(\text{negative cash flows, finance rate}) = -1000 - 4000 \cdot (1+10\%)^{-1} = -4636.36$ .
- Second, we calculate the future value of the positive cash flows (reinvested at the reinvestment rate):  $FV(\text{positive cash flows, reinvestment rate}) = 5000 \cdot (1+12\%) + 2000 = 7600$ .