

# Programming Paradigms

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# Reading Assignment

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- Mitchell, Chapter 2.1

# What Is a Programming Language?

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- Formal notation for specifying computations, independent of a specific machine
  - Example: a factorial function takes a single non-negative integer argument and computes a positive integer result
    - Mathematically, written as  $\text{fact}: \text{nat} \rightarrow \text{nat}$
- Set of imperative commands used to direct computer to do something useful
  - Print to an output device: `printf("hello world\n");`
    - What mathematical function is “computed” by `printf`?

# Partial and Total Functions

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- Value of an expression may be undefined
  - Undefined operation, e.g., division by zero
    - $3/0$  has no value
    - Implementation may halt with error condition
  - Nontermination
    - $f(x) = \text{if } x=0 \text{ then } 1 \text{ else } f(x-2)$
    - This is a partial function: not defined on all arguments
    - Cannot be detected by inspecting expression (why?)
- These two cases are “mathematically” equivalent, but operationally different (why?)

Subtle: “undefined” is not the name of a function value ...

# Partial and Total: Definitions

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- **Total function**  $f:A \rightarrow B$  is a subset  $f \subseteq A \times B$  with
  - $\forall x \in A$ , there is some  $y \in B$  with  $\langle x, y \rangle \in f$   
(total)
  - If  $\langle x, y \rangle \in f$  and  $\langle x, z \rangle \in f$  then  $y = z$   
(single-valued)
- **Partial function**  $f:A \rightarrow B$  is a subset  $f \subseteq A \times B$  with
  - If  $\langle x, y \rangle \in f$  and  $\langle x, z \rangle \in f$  then  $y = z$   
(single-valued)
- Programs define partial functions for two reasons
  - What are these reasons?

# Computability

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- Function  $f$  is **computable** if some program  $P$  computes it
  - For any input  $x$ , the computation  $P(x)$  halts with output  $f(x)$
  - Partial recursive functions: partial functions (int to int) that are computable

# Halting Problem

Ettore Bugatti: "I make my cars to go, not to stop"



# Halting Function

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- Decide whether program halts on input
  - Given program P and input x to P,

$$\underline{\text{Halt}}(P,x) = \begin{cases} \text{yes} & \text{if } P(x) \text{ halts} \\ \text{no} & \text{otherwise} \end{cases}$$

## Clarifications

- Assume program P requires one string input x
- Write  $P(x)$  for output of P when run in input x
- Program P is string input to Halt

Fact: There is no program for Halt



# Unsolvability of the Halting Problem

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- Suppose  $P$  solves variant of halting problem
  - On input  $Q$ , assume  $P(Q) = \begin{cases} \text{yes} & \text{if } Q(Q) \text{ halts} \\ \text{no} & \text{otherwise} \end{cases}$
- Build program  $D$ 
  - $D(Q) = \begin{cases} \text{run forever} & \text{if } Q(Q) \text{ halts} \\ \text{halt} & \text{if } Q(Q) \text{ runs forever} \end{cases}$
- If  $D(D)$  halts, then  $D(D)$  runs forever
- If  $D(D)$  runs forever, then  $D(D)$  halts
- **Contradiction!** Thus  $P$  cannot exist.

# Main Points About Computability

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- Some functions are computable, some are not
  - Example: halting problem
- Programming language implementation
  - Can report error if program result is undefined due to an undefined basic operation (e.g., division by zero)
  - Cannot report error if program will not terminate

# Computation Rules

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- The factorial function type declaration does not convey how the computation is to proceed
- We also need a computation rule
  - $\text{fact}(0) = 1$
  - $\text{fact}(n) = n * \text{fact}(n-1)$
- This notation is more computationally oriented and can almost be executed by a machine

# Factorial Functions

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- C, C++, Java:

```
int fact (int n) { return (n == 0) ? 1 : n * fact (n-1); }
```

- Scheme:

```
(define fact  
  (lambda (n) (if (= n 0) 1 (* n (fact (- n 1))))))
```

- ML:

```
fun fact n = if n=0 then 1 else n*fact(n-1);
```

- Haskell:

- `fact :: Integer->Integer`
- `fact 0 = 1`
- `fact n = n*fact(n-1)`

# Principal Paradigms

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- Imperative / Procedural
- Functional / Applicative
- Object-Oriented
- Concurrent
- Logic
- Scripting
  
- In reality, very few languages are “pure”
  - Most combine features of different paradigms

# Where Do Paradigms Come From?



- **Paradigms** emerge as the result of social processes in which people develop ideas and create principles and practices that embody those ideas
  - Thomas Kuhn. "The Structure of Scientific Revolutions."
- Programming paradigms are the result of people's ideas about how programs should be constructed
  - ... and formal linguistic mechanisms for expressing them
  - ... and software engineering principles and practices for using the resulting programming language to solve problems

# Imperative Paradigm

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- Imperative (procedural) programs consists of actions to effect **state change**, principally through assignment operations or side effects
  - Fortran, Algol, Cobol, PL/I, Pascal, Modula-2, Ada, C
  - Why does imperative programming dominate in practice?
- OO programming is not always imperative, but most OO languages have been imperative
  - Simula, Smalltalk, C++, Modula-3, Java
  - Notable exception: CLOS (Common Lisp Object System)

# Functional and Logic Paradigms

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- Focuses on function evaluation; avoids updates, assignment, mutable state, side effects
- Not all functional languages are “pure”
  - In practice, rely on non-pure functions for input/output and some permit assignment-like operators
    - E.g., `(set! x 1)` in Scheme
- Logic programming is based on predicate logic
  - Targeted at theorem-proving languages, automated reasoning, database applications
  - Recent trend: declarative programming



# Concurrent and Scripting Languages

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- Concurrent programming cuts across imperative, object-oriented, and functional paradigms
- Scripting is a very “high” level of programming
  - Rapid development; glue together different programs
  - Often dynamically typed, with only int, float, string, and array as the data types; no user-defined types
  - Weakly typed: a variable 'x' can be assigned a value of any type at any time during execution
- Very popular in Web development
  - Especially scripting active Web pages

# Unifying Concepts

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- Unifying language concepts
  - Types (both built-in and user-defined)
    - Specify constraints on functions and data
    - Static vs. dynamic typing
  - Expressions (e.g., arithmetic, boolean, strings)
  - Functions/procedures
  - Commands
- We will study how these are defined syntactically, used semantically, and implemented pragmatically

# Design Choices

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- **C**: Efficient imperative programming with static types
- **C++**: Object-oriented programming with static types and ad hoc, subtype and parametric polymorphism
- **Java**: Imperative, object-oriented, and concurrent programming with static types and garbage collection
- **Scheme**: Lexically scoped, applicative-style recursive programming with dynamic types
- **Standard ML**: Practical functional programming with strict (eager) evaluation and polymorphic type inference
- **Haskell**: Pure functional programming with non-strict (lazy) evaluation.

# Abstraction and Modularization

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- Re-use, sharing, extension of code are critically important in software engineering
- Big idea: **detect errors at compile-time**, not when program is executed
- **Type** definitions and declarations
  - Define intent for both functions/procedures and data
- **Abstract data types** (ADT)
  - Access to local data only via a well-defined interface
- Lexical **scope**

# Static vs. Dynamic Typing

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- Static typing
  - Common in compiled languages, considered “safer”
  - Type of each variable determined at compile-time; constrains the set of values it can hold at run-time
- Dynamic typing
  - Common in interpreted languages
  - Types are associated with a variable at run-time; may change dynamically to conform to the type of the value currently referenced by the variable
  - Type errors not detected until a piece of code is executed

# Billion-Dollar Mistake

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## Failed launch of Ariane 5 rocket (1996)

- \$500 million payload; \$7 billion spent on development

## Cause: software error in inertial reference system

- Re-used Ariane 4 code, but flight path was different
- 64-bit floating point number related to horizontal velocity converted to 16-bit signed integer; the number was larger than 32,767; inertial guidance crashed

# Program Correctness

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- Assert formal correctness statements about critical parts of a program and reason effectively
  - A program is intended to carry out a specific computation, but a programmer can fail to adequately address all data value ranges, input conditions, system resource constraints, memory limitations, etc.
- Language features and their interaction should be clearly specified and understandable
  - If you do not or can not clearly understand the semantics of the language, your ability to accurately predict the behavior of your program is limited

# Language Translation

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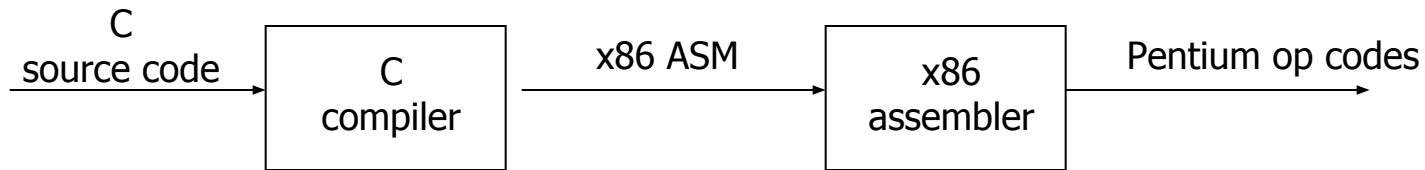
- **Native-code compiler:** produces machine code
  - Compiled languages: Fortran, C, C++, SML ...
- **Interpreter:** translates into internal form and immediately executes (read-eval-print loop)
  - Interpreted languages: Scheme, Haskell, Python ...
- **Byte-code compiler:** produces portable bytecode, which is executed on virtual machine (e.g., Java)
- Hybrid approaches
  - Source-to-source translation (early C++ → C → compile)
  - Just-in-time Java compilers convert bytecode into native machine code when first executed



# Language Compilation

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- **Compiler:** program that translates a source language into a target language
  - Target language is often, but not always, the assembly language for a particular machine

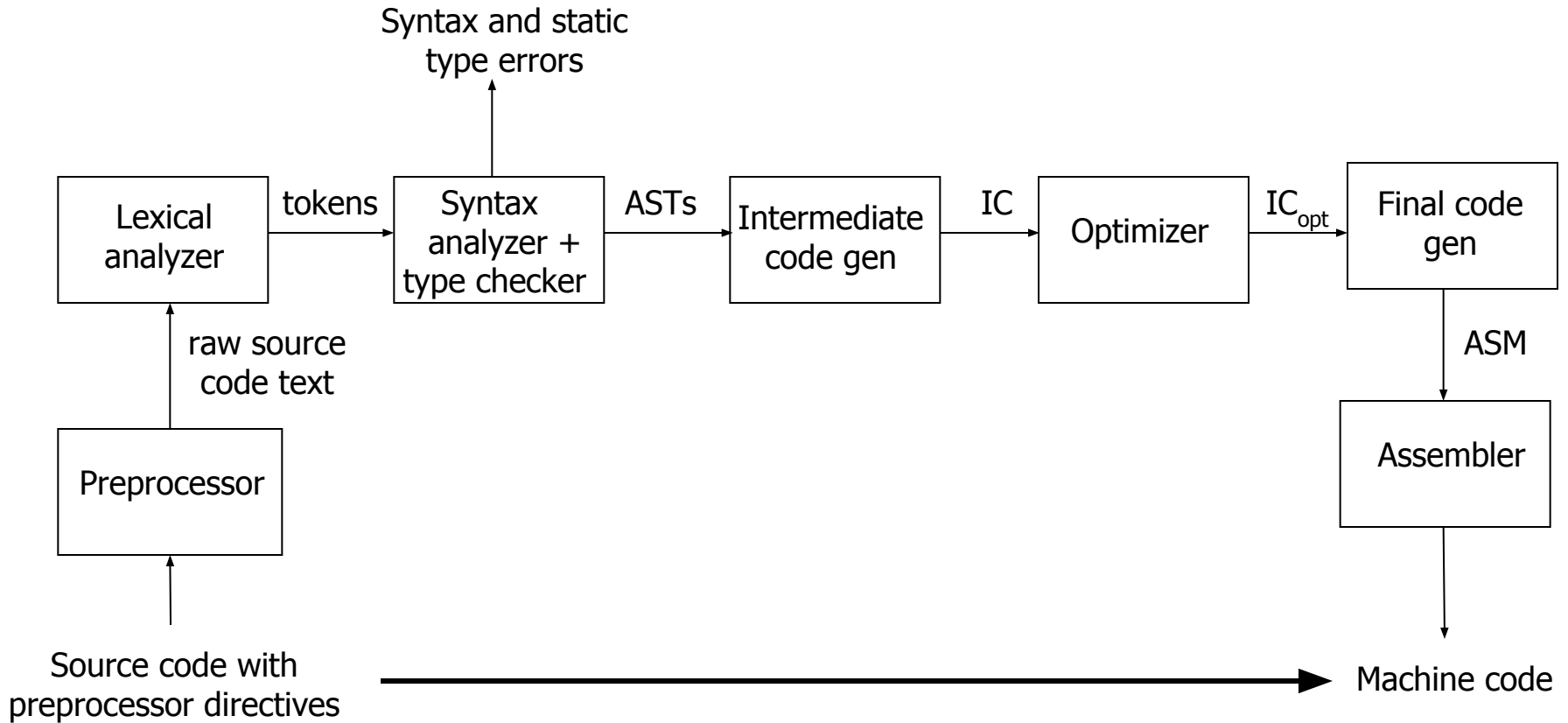


# Checks During Compilation

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- Syntactically invalid constructs
- Invalid type conversions
  - A value is used in the “wrong” context, e.g., assigning a float to an int
- Static determination of type information is also used to generate more efficient code
  - Know what kind of values will be stored in a given memory region during program execution
- Some programmer logic errors
  - Can be subtle: `if (a = b) ...` instead of `if (a == b) ...`

# Compilation Process



# Phases of Compilation

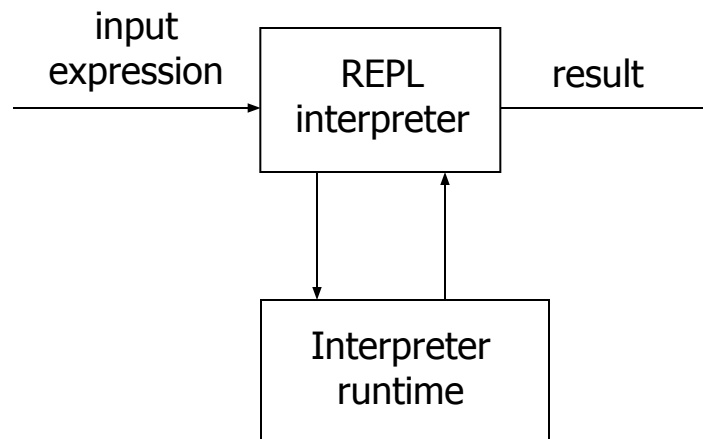
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- **Preprocessing:** conditional macro text substitution
- **Lexical analysis:** convert keywords, identifiers, constants into a sequence of tokens
- **Syntactic analysis:** check that token sequence is syntactically correct
  - Generate abstract syntax trees (AST), check types
- **Intermediate code generation:** “walk” the ASTs and generate intermediate code
  - Apply optimizations to produce efficient code
- **Final code generation:** produce machine code

# Language Interpretation

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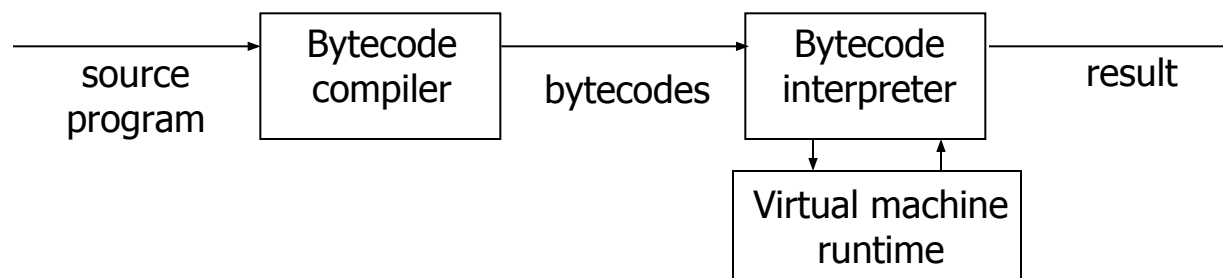
- Read-eval-print loop
  - Read in an expression, translate into internal form
  - Evaluate internal form
    - This requires an abstract machine and a “run-time” component (usually a compiled program that runs on the native machine)
  - Print the result of evaluation
  - Loop back to read the next expression



# Bytecode Compilation

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- Combine compilation with interpretation
  - Idea: remove inefficiencies of read-eval-print loop
- Bytecodes are conceptually similar to real machine opcodes, but they represent compiled instructions to a virtual machine instead of a real machine
  - Source code statically compiled into a set of bytecodes
  - Bytecode interpreter implements the virtual machine
  - In what way are bytecodes "better" than real opcodes?



# Binding

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- **Binding** = association between an object and a property of that object
  - Example: a variable and its type
  - Example: a variable and its value
- A language element is bound to a property at the time that property is defined for it
  - **Early binding** takes place at compile-time
  - **Late binding** takes place at run-time