

# How managers can make a decision in certainty environment? 

Search for options with the maximum benefit or minimum costs is called the optimization analysis

3 optimization methods:

- marginal analysis
- linear programming
- Incremental profit analysis

How managers can make a decision in risk - and uncertainty environment?



In conditions of risk and uncertainty typical decision task is quite difficult, because there are many possible outcomes

## Solutions matrix

Necessary
systematization

## Payment matrix




This tool:
Formalizes the process of decision-making
Provides a summary of return for different purposes and state of environment

(Risk - probability of undesired occurense)

Здесь тоже слишком мелко. Попробуем



## A priori (deductive method)

No experiment and analysis of past experience
characteristics of possible cases are known in advance
Ex:

## Aposteriori (statistical analysis of empirical data)

past experience will continue in the future


## Frequency distribution can be converted into a probability distribution

If a certain load factor appeared 20 times for 50 flights, we can say that the probability of this factor during the next flight 20/50 $=40$


Determine and minimize the risks inherent to a particular project

One of the methods: the calculation of the probability distribution of possible outcomes, then the calculation of expected value

## Expected value

$$
\begin{aligned}
& E(X)=P_{1} X_{1}+P_{2} X_{2}+\ldots+P_{n} X_{n}=\sum_{i=1}^{n} P_{i} X_{i} \\
& \quad X_{i}-\text { Value of } \text { i outcome } \\
& \quad P_{i}-\text { Probability of } i \text { outcome }
\end{aligned}
$$

The expected value of the strategy is the weighted average cost, which uses the probability of return as weights

Manager choose strategy with the highest expected value


| Decision matrix |  |  |  |  | Expected value$E(S)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Alternative strategies | The state of the external environment |  |  |  |  |
|  | $\begin{aligned} & \text { N1 } \\ & P=0,20 \end{aligned}$ | N2 $P=0,65$ | N3 $P=0,10$ | N4 $P=0,05$ |  |
| S1 | 6 | 6 | 6 | 4 | $9,50$ |
| S2 | 25 | 7 | 7 | -15 | 17,65 |
| S3 | 20 | 20 | 7 | -1 | 15,00 |
| S4 | 19 | 16 | 9 | -2 | 15,10 |
| S5 | 20 | 15 | 15 | -3 |  |
| Optimum strategy |  |  |  |  |  |

Suppose that expected value of alternatives strategies are equal

| Decision matrix |  |  |  |
| :---: | :---: | :---: | :---: |
| Alternative strategies | The state of the external envir |  |  |
|  | $\begin{aligned} & \text { N1 } \\ & P=0,25 \end{aligned}$ | N2 $P=0,50$ | $\begin{aligned} & \text { N3 } \\ & \mathrm{P}=0,25 \end{aligned}$ |
| S1 | 20 | 10 | 20 |
| S2 | 40 | 10 | 0 |
| S3 | 10 | 10 | 10 |

How can we choose between S1 and S2?

## New criteria - degree of risk

May be determined as deviation scope of probable outcome from expected value


| Decision matrix |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :---: |
| Alternative <br> strategies | The state of the external environment |  |  |  |  |
|  | N 1 <br> $P=0,25$ | N 2 <br> $\mathrm{P}=0,50$ | N 3 <br> $\mathrm{P}=0,25$ | Expected value <br> $\mathrm{E}(\mathrm{S})$ |  |
|  | 20 | 10 | 20 | 15 |  |
| S 2 | 40 | 10 | 0 | 15 |  |

By intuition we feel that the further away from the average value will be the actual outcome, the riskier the project will be

One way of calculating risk - calculation of swing (amplitude)
swing (amplitude)

- the difference between the extreme values of probable outcomes

| Decision matrix |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :---: |
| Alternative <br> strategies | The state of the external environment |  |  |  |  |
|  | N 1 <br> $\mathrm{P}=0,25$ | N 2 <br> $\mathrm{P}=0,50$ | N 3 <br> $\mathrm{P}=0,25$ | Предполагаемая <br> стоимость <br> $\mathrm{E}(\mathrm{S})$ |  |
|  | 20 | 10 | 20 | 15 |  |
| S 2 | 40 | 10 | 0 | 15 |  |

Swing for S1-10, for S2-40.

## root-mean-square deviation

## $\square$



The higher root-mean-square deviation - the higher risk
|Пойдёмте обратно в наш класс алгебры工...
Calculation of the root-mean-square deviation:


## Вычисление среднего квадратичного отклонения

Таблица 4.4
Вычисление среднего квадратичного отклонения

| Стратегия | $\left(X_{i}-\mu\right)$ | $\left(X_{i}-\mu\right)^{2}$ | $P_{i}$ | $\left(X_{i}-\mu\right)^{2 P_{i}}$ |  |
| :---: | :---: | :---: | :---: | :---: | :--- |
| $S_{1}$ | 5 | 25 | 0,25 | 6,25 |  |
|  | -5 | 25 | 0,50 | 12,50 |  |
|  | 5 | 25 | 0,25 | $\frac{6,25}{\sigma_{1}{ }^{2}=25,00}$ | $\sigma_{1}=5$ |
|  |  |  |  | 156,25 |  |
| $S_{2}$ | 25 | 625 | 0,25 | 12,50 |  |
|  | -5 | 25 | 0,50 | $\frac{56,25}{}$ |  |
|  | -15 | 225 | 0,25 | $\frac{\sigma_{2}{ }^{2}=225,00}{\sigma_{2}=15}$ |  |

S 2 is $\mathbf{3}$ times more risky than S 1

