



Present Value Essentials



Basic Assumptions:

- All cash payments (receipts)
- Certainty regarding:
 - Amount of cash flows
 - Timing of cash flows
- All cash flows are immediately reinvested at designated interest rate



Basic Concepts:

- For Accounting almost always Present value. I.e.: Answer the question:
- Some amount of money is to be paid or received in the future (or a series of payments), how much is it worth now, given a certain required rate of return



Basic Concepts I:

- Time Value of Money:
 - Invested money earns interest (if in bank) or some rate of return (if invested in something else)
- Compound interest:
 - Money earned on investment is reinvested immediately at required rate of return (interest earned on interest received)



Basic Concepts II:

- Interest; rate of return; discount rate:
 - For PV analysis they mean the same. From now, only “interest” will be used
- Future Value:
 - Value of an investment after a designated period of time, given a specified interest rate



Present Value vs. Future Value

- Present value is based on future value, specifically the compound interest formula. Therefore
- Future value discussion to help you understand present value



Basic Future Value Concepts:

- Invested money earns more money
- \$1,000 today is worth more than \$1,000 one year from today because:
- \$1,000 invested at 10% grows to \$1,100 in one year
- \$1,100 is the future value of \$1,000 @ 10% after one year



Future Value Example:

	Investment	interest rate	interest earned
year 1	\$100.00	10%	\$10.00
year 2	\$110.00	10%	\$11.00
year 3	\$121.00	10%	\$12.10
Value of investment after three years:	\$133.10		



FV Example (alternate view):

- \$ 1,000 @ 10% grows to
 - \$1,100 in one year
 - \$1,210 in two years
 - \$1,331 in three years OR
- $\$1,000 * 1.1 * 1.1 * 1.1 = \$1,331$



Future Value Example:

Another way to determine the future value of \$100 invested to earn 10%, interest compounded annually: Use the Compound interest formula:

$(1 + r)^n$ Where r = interest rate/compounding period
and n = number of compounding periods

$$(1 + .1)^3 = 1.331 * 100 = \$133.10$$



Compounding:

- Number of times **per year** interest is calculated
- May be annually, semi-annually, quarterly, etc.
- **However:** Interest rate is expressed on annual basis, unless stated to be for another period. Therefore: if annual interest rate is 10% ----



Compounding:

- Semi-annual: 5% twice a year
- Quarterly: 2.5% four times a year
- Monthly: $10/12\%$ 12 times a year
- In other words: If more than one compounding period/year, interest rate is divided by # of periods. # of years multiplied by # of periods



Compounding:

- Why does it matter? Because interest adds up faster. E.g.:
- 10%, 3 years, semi-annual compounding: $(1 + .1/2)^{3*2} = 1.34 > (1 + .1)^3 = 1.31$



Future Value Calculation:

- FV of $r = 10\%$, annual compounding and $n = 3$ years:
- **$FV(r, n) = FV(10\%, 3) = 1.331$**
- \$100 invested for 3 years at 10% =
- $\$100 * FV(10\%, 3) = X$
- $\$100 * 1.331 = X = \133.10



Present Value (PV):

- Accounting almost always wants to know what something is worth **now**
- PV asks: If \$133.10 will be received in 3 years, how much is it worth today if 10% is the appropriate discount rate?
- Use FV formula to answer the question:

PV of \$133.10

(to be paid or received in 3 years)

- $X * FV(10\%,3) = \$ 133.10$
- $X * 1.331 = \$ 133.10$
- $(X * 1.331)/1.331 = \$133.10/1.331 = \100
- **PV = Reciprocal of FV OR $1/FV$**
- **therefore: $PV(10\%,3) = 1/FV(10\%,3)$**
- **$= 1/(1+.1)^3 = .75132$**



PV of \$133.10

(to be paid or received in 3 years (again))

- $\$ 133.10 * PV(10\%,3) = X$
- $\$ 133.10 * .75132 = X = \100
- This is the equation you must use
- Do not use the formula, use table instead (p. C10)



Part II Annuities

- Basic PV used for single sum payments
 - E.g. a note payable due in 5 years
- **PV of Annuity** used for questions relating to a series of **equal payments at regular intervals**
 - E.g. car payments, payments on a student loan



PV of 3 payments of \$ 100 each?

- Payments made at end of each of the next three years, 10% interest rate:
- $PVA \$100 (10\%, 3)$



PV annuity (PVA) \$100, 10%, 3 years:

Option 1:	we could express the above as follows:			
	receive	PV	Factor	answer:
end of year 1	\$100.00	(10%, 1)	0.9091	\$90.91
end of year 2	\$100.00	(10%, 2)	0.8264	\$82.64
end of year 3	\$100.00	(10%, 3)	0.7513	\$75.13
				\$248.68



PV annuity (PVA) \$100, 10%,
3 years:

Option 2: Use simple algebra, factor out constant:

Restated equation:

$$\mathbf{\$100 * (.9091 + .8264 + .7531) = X}$$

$$\mathbf{\$100 * 2.4868 = X = \$248.68}$$



PV annuity (PVA)

**Present value of an annuity (PVA) 3 periods,
10% = (.9091 + .8264 + .7531) = 2.4868**

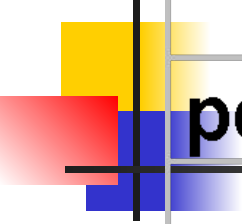
Libby ordinary annuity table, page 748:

$$\text{PVA (10\%,3)} = 2.4869$$

Kimmel ordinary annuity table, Appendix C:

$$\text{PVA (10\%,3)} = 2.48685$$

Present Value (PV) of \$ 1



period	1%	2%	10%
1	0.99	0.98	0.909
2	0.98	0.961	0.826
3	0.971	0.942	0.751

PV of an ordinary annuity of \$1

period	1%	2%	10%
1	0.99	0.98	0.909
2	1.97	1.942	1.736
3	2.941	2.884	2.487



PV annuity due (PVA due)

- **Difference:** 1st payment is at beginning of period compared to at the end for an ordinary annuity
 - Example: Rent or lease payments
- Libby does not have table for it
- However: not a big problem



PVA due: 3 payments, 10%

Option 1: we could express the above as follows:

	receive	PV	Factor	answer:
beginning of	\$100.00	(10%,0)	1	\$100.00
beginning of	\$100.00	(10%,1)	0.9091	\$90.91
beginning of	\$100.00	(10%,2)	0.8264	\$82.64
				\$273.55



PVA due: 3 payments, 10%

Option 2: Calculate the factor:

PVA due (10%,3)

= 1 + PVA(10%,2)

= 1 + 1.73554

= **2.73554** * \$ 100 = **\$2.73.55**

Compared to ordinary annuity: 2.4868