

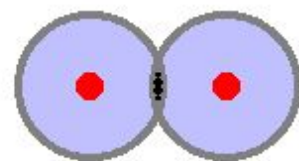
# PROTEIN PHYSICS

## LECTURES 3-4

Elementary interactions:  
Van der Waals  
&  
H-bonds



**repulsion at  
small distances**

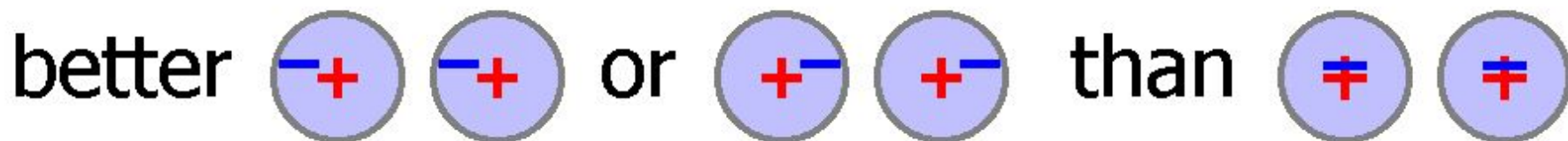


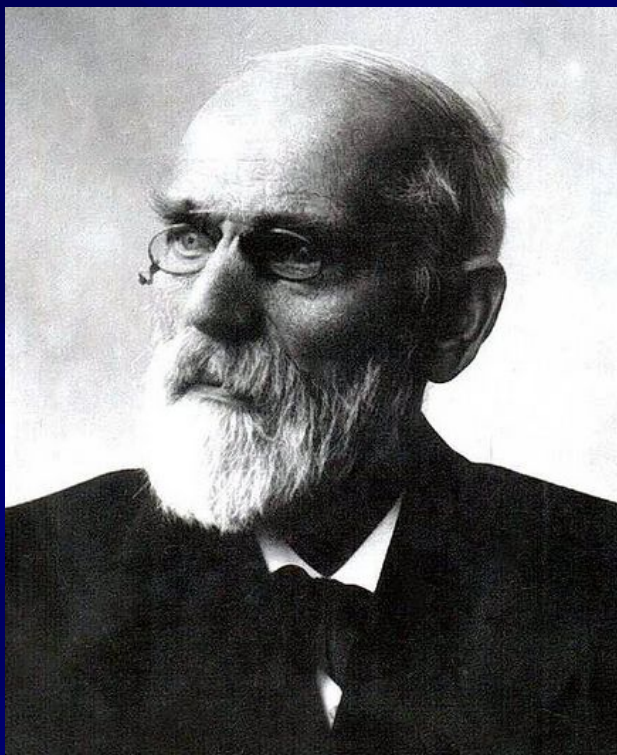
**BUT:**

**Van der Waals**

**attraction at larger distances**

**due to coordination of  $e$  vibrations**





Johannes Diderik van der Waals  
(1837 – 1923)  
— Nobel Prize 1910

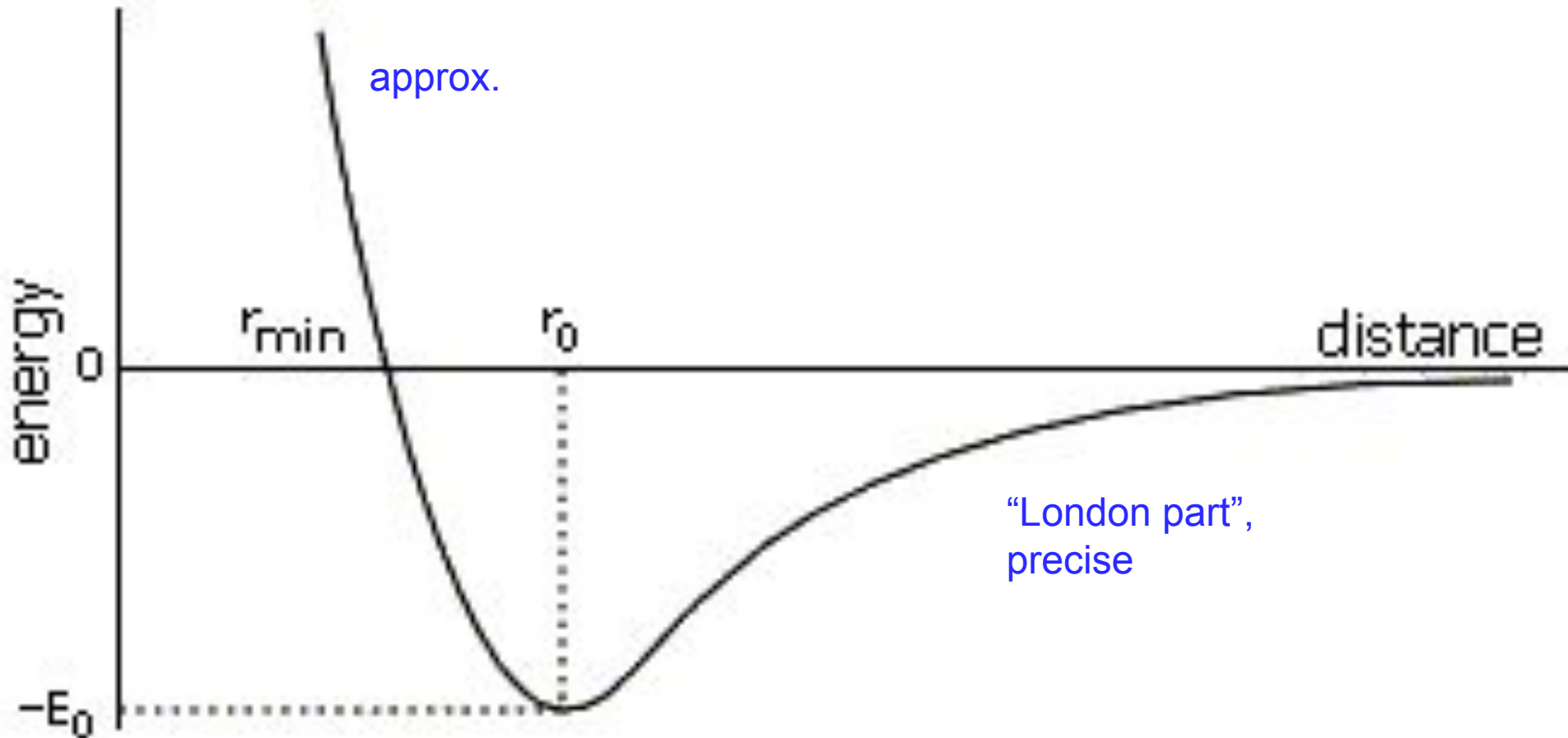


Fritz Wolfgang London  
(1900 – 1954)

# Lennard-Jones potential:

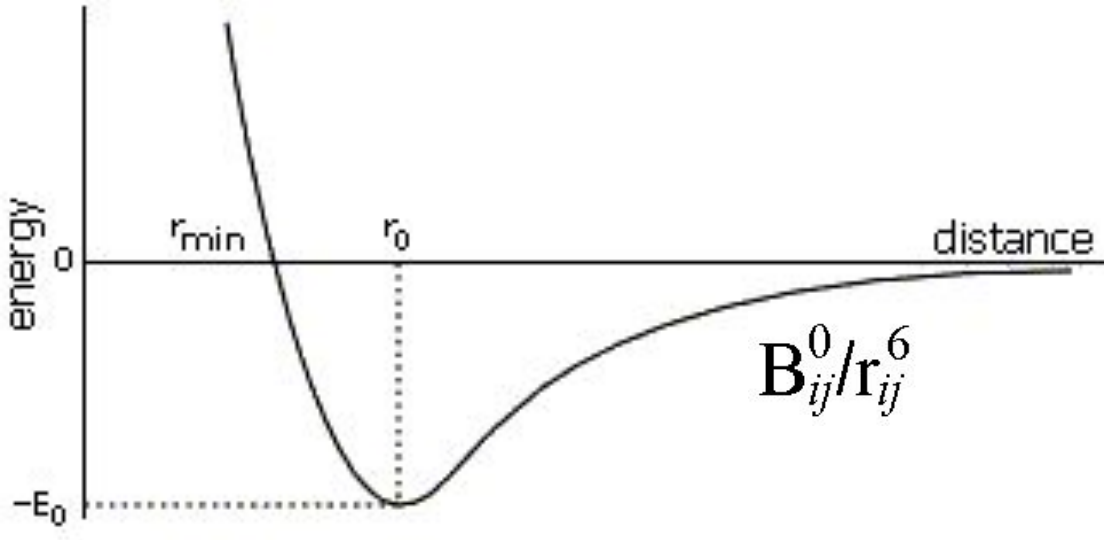
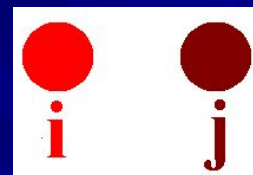
$$U_{\text{LJ}}(r) = E_0 \left[ \left( \frac{r_0}{r} \right)^{12} - 2 \left( \frac{r_0}{r} \right)^6 \right]$$

The simplest form



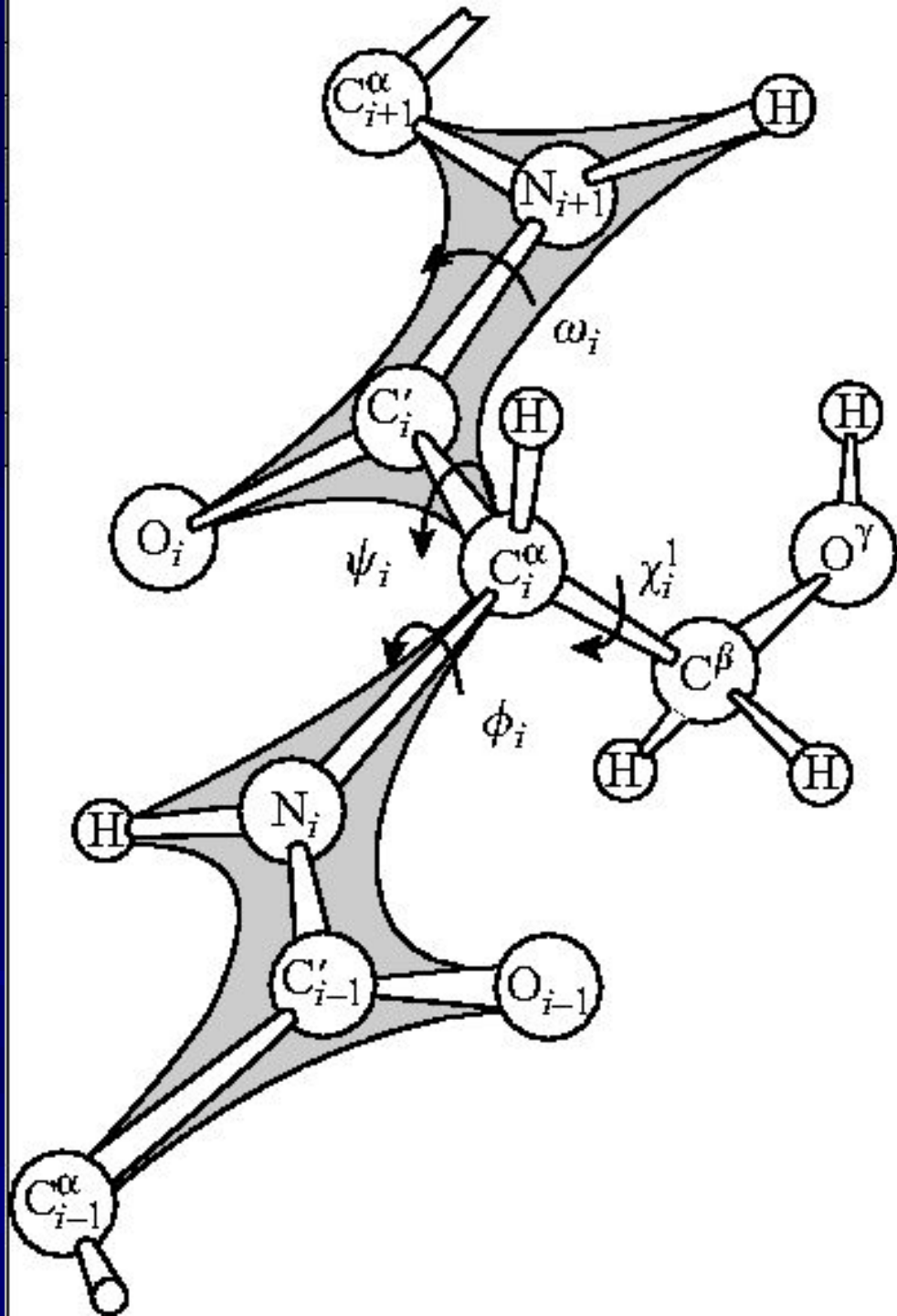
In vacuum

$$B_{ij}^0 = \beta_i \beta_j$$



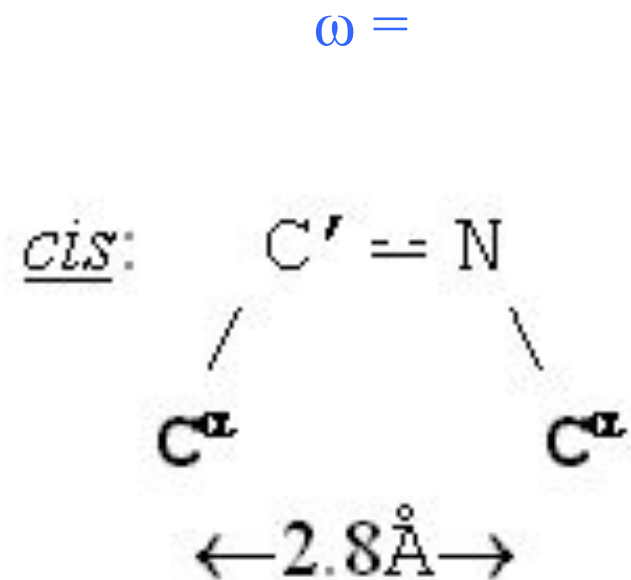
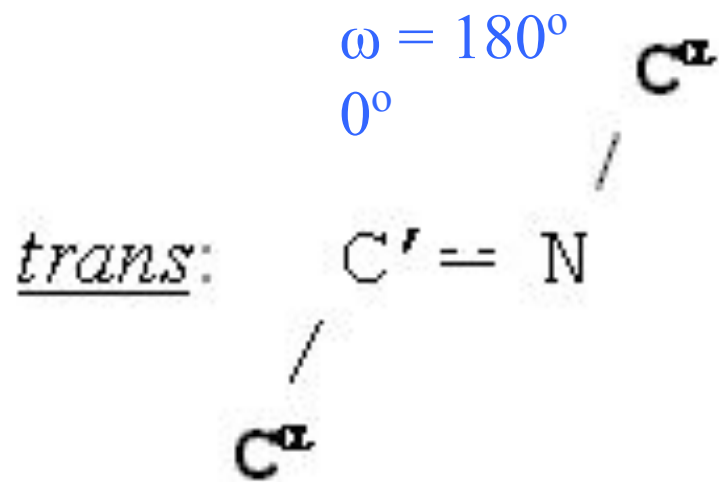
Typical parameters of van der Waals interaction potentials.

Interaction	$E_0, \frac{\text{kcal}}{\text{mol}}$	$r_0, \text{\AA}$	$r_{\min}, \text{\AA}$	Min. v. d. Waals radii of atoms, $\text{\AA}$
H . . . . H	0.12	2.4	2.0	H: 1.0
H . . . . C	0.11	2.9	2.4	
C . . . . C	0.12	3.4	3.0	C: 1.5
O . . . . O	0.23	3.0	2.7	O: 1.35
N . . . . N	0.20	3.1	2.7	N: 1.35
CH <sub>2</sub> . . . CH <sub>2</sub>	$\approx 0.5$	$\approx 4.0$	$\approx 3.0$	CH <sub>2</sub> : $\approx 1.5$

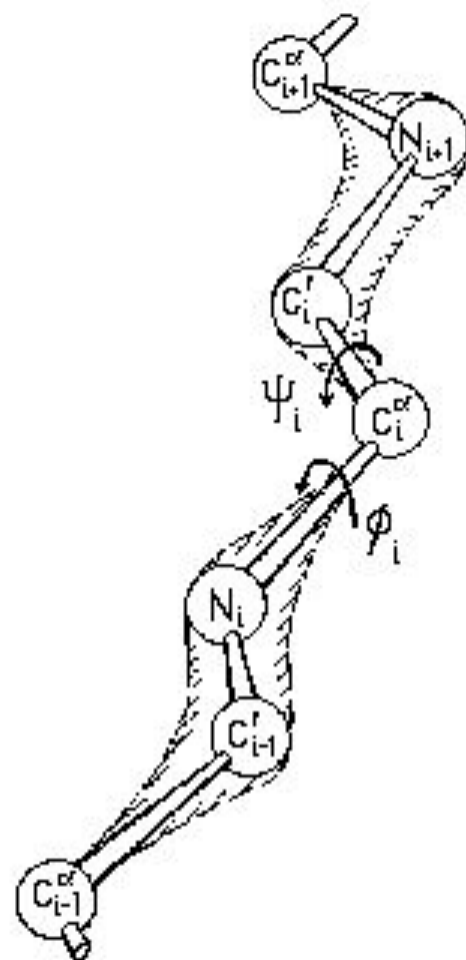
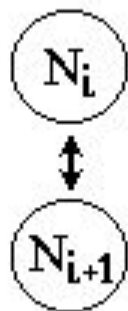
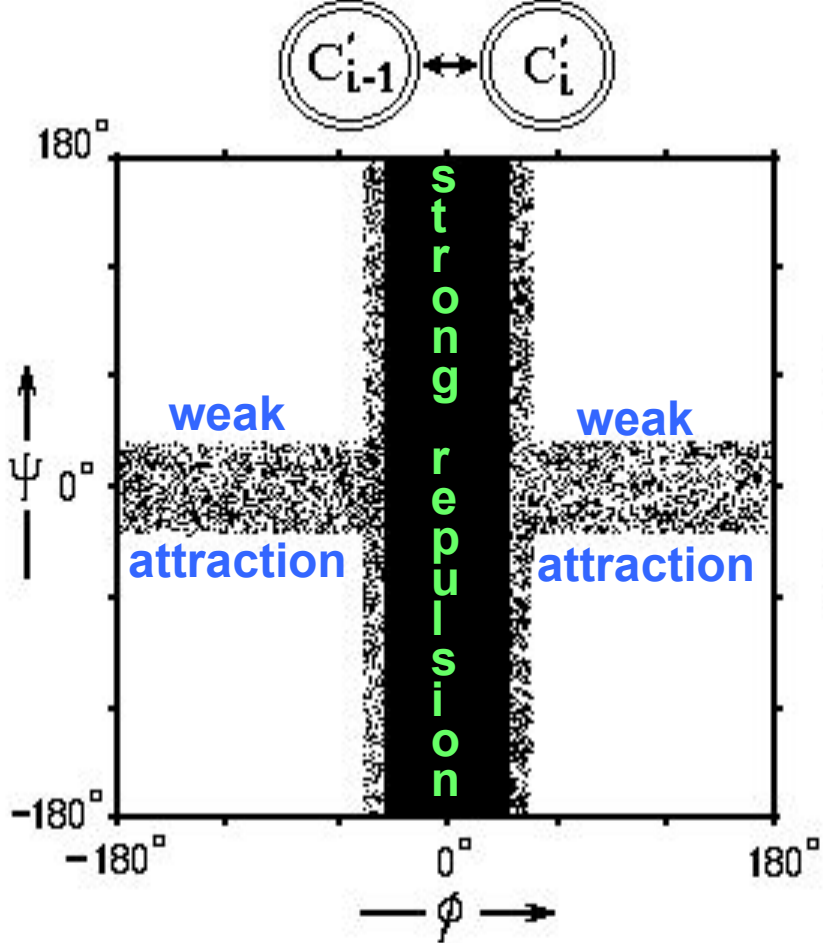


Main-chain:

$\phi$  (N-C $\alpha$ ),  
 $\psi$  (C $\alpha$ -C')

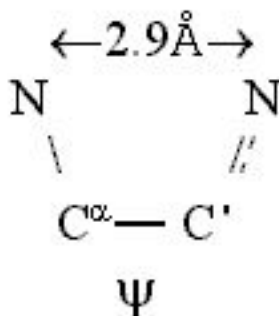
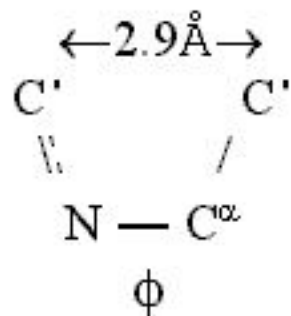


$2.8 \text{ \AA} < r_{\min}(\text{C} \dots \text{C}) = 3.0 \text{ \AA}$   
 strong repulsion



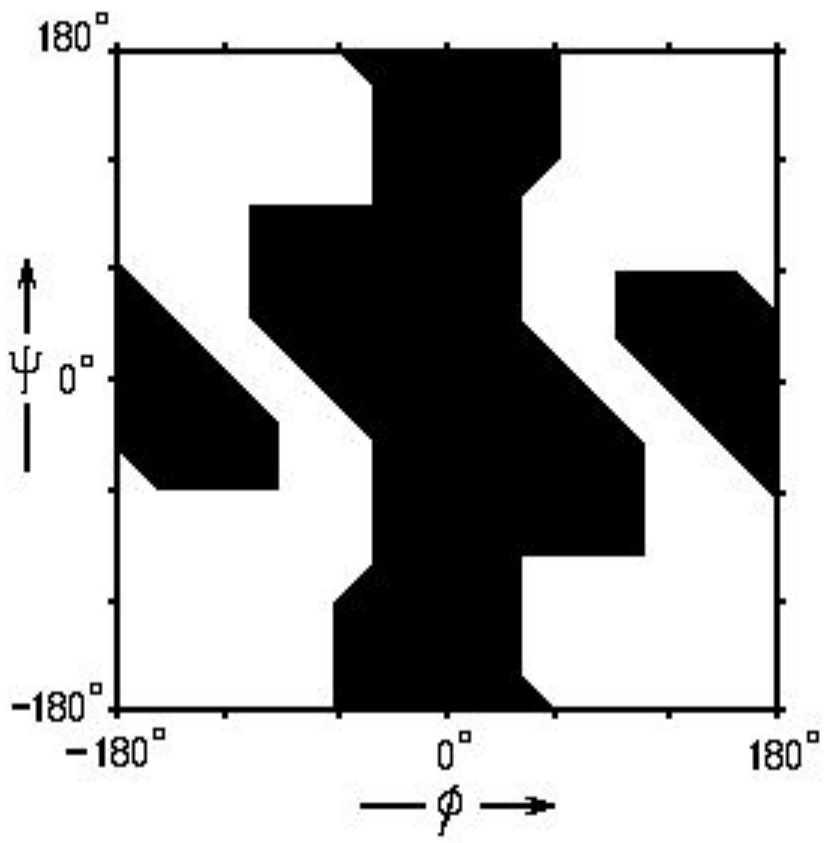
$$2.9\text{\AA} < r_{\min}(C\dots C) = 3.0\text{\AA}$$

$$2.9\text{\AA} > r_{\min}(N\dots N) = 2.7\text{\AA}$$

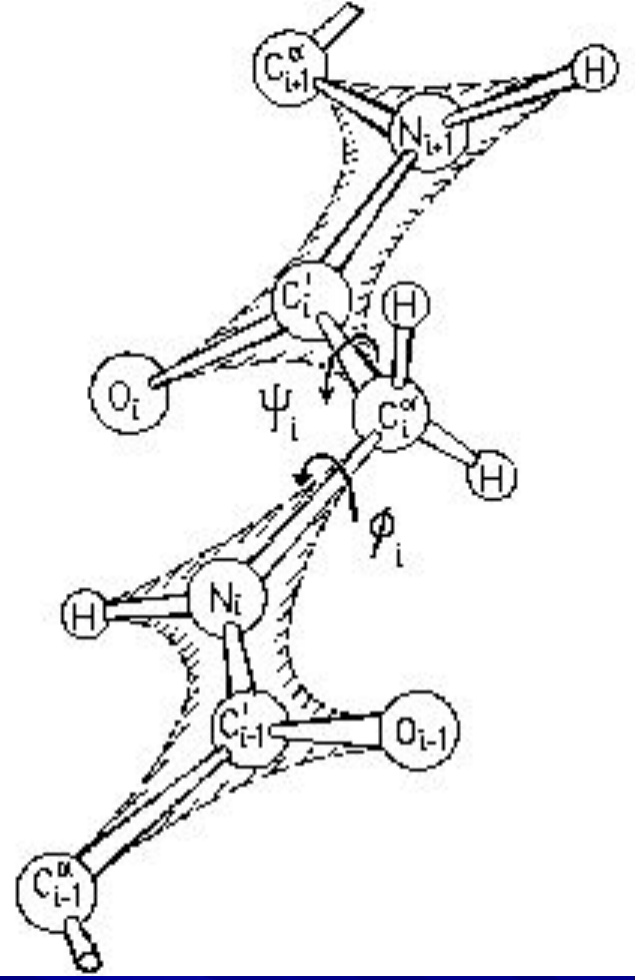


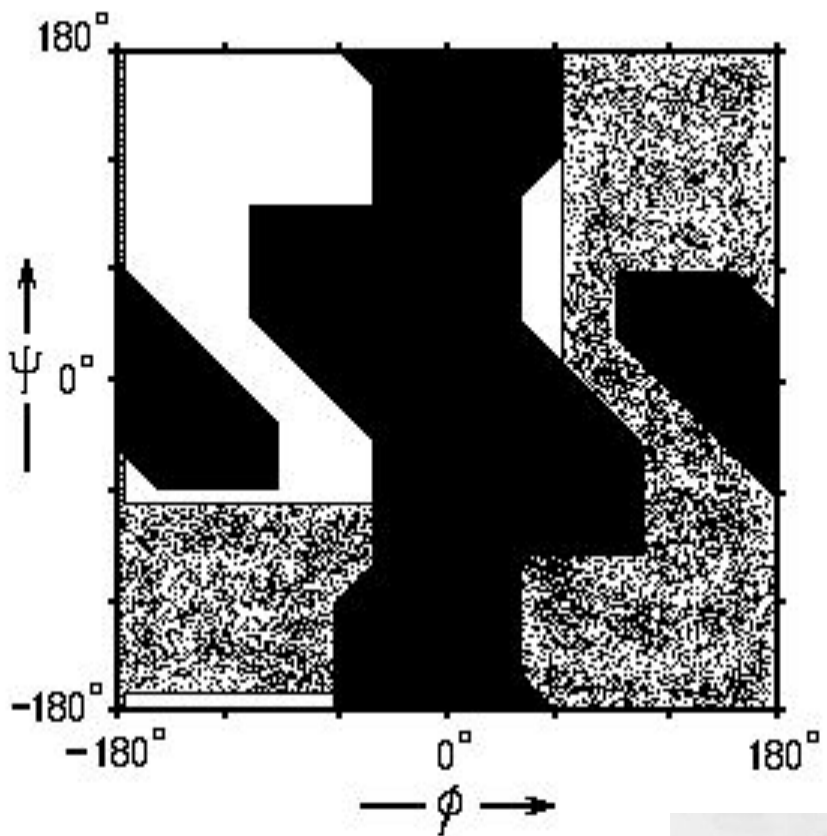
$$r_0(N\dots N) = 3.1\text{\AA}$$



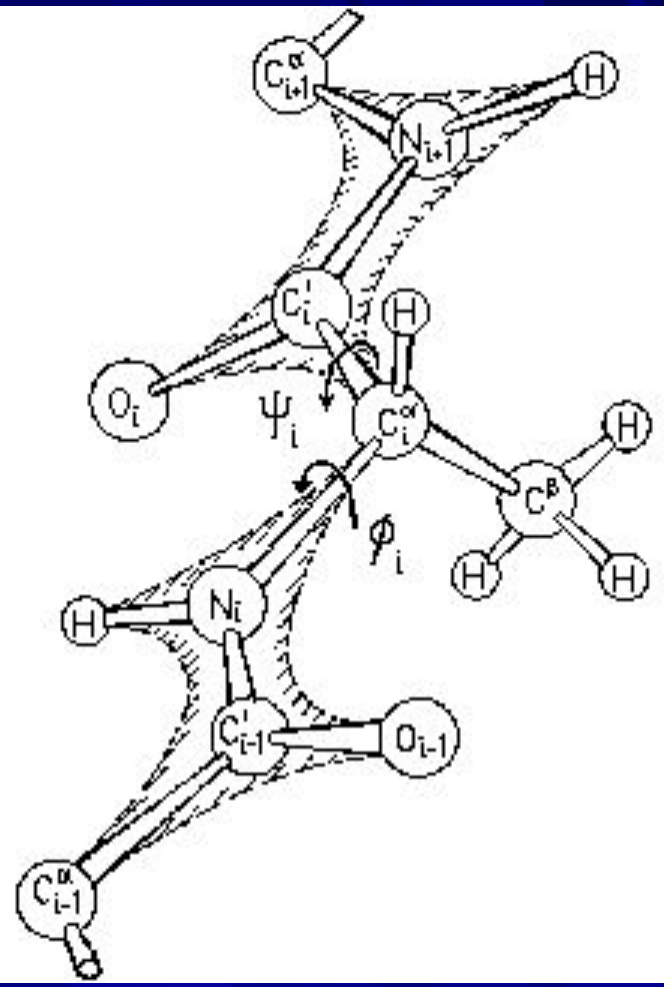


GLY

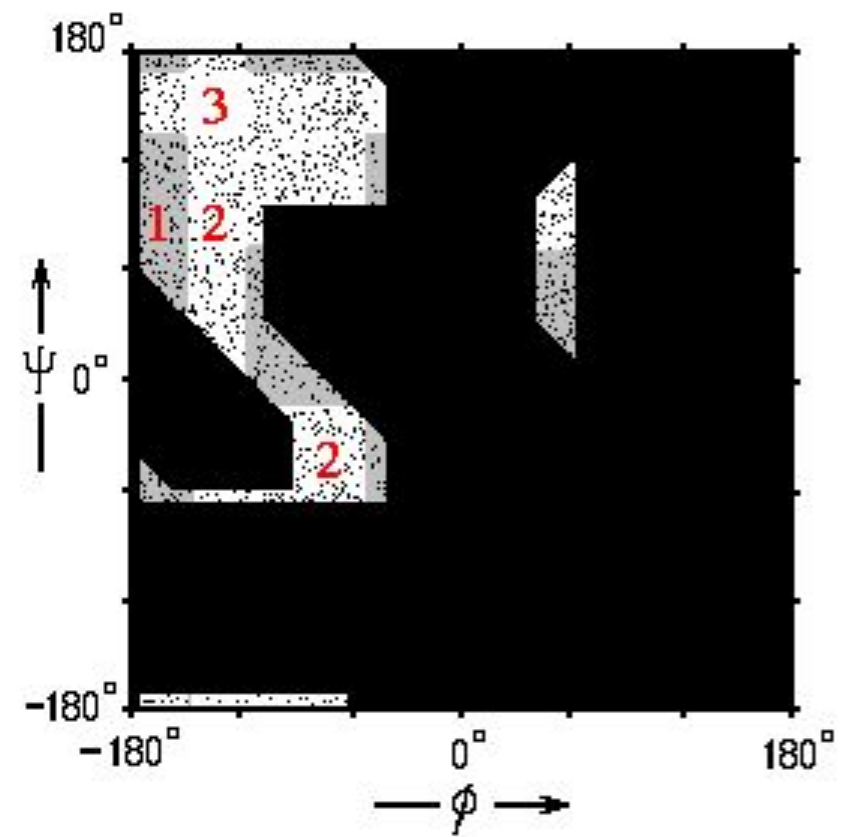




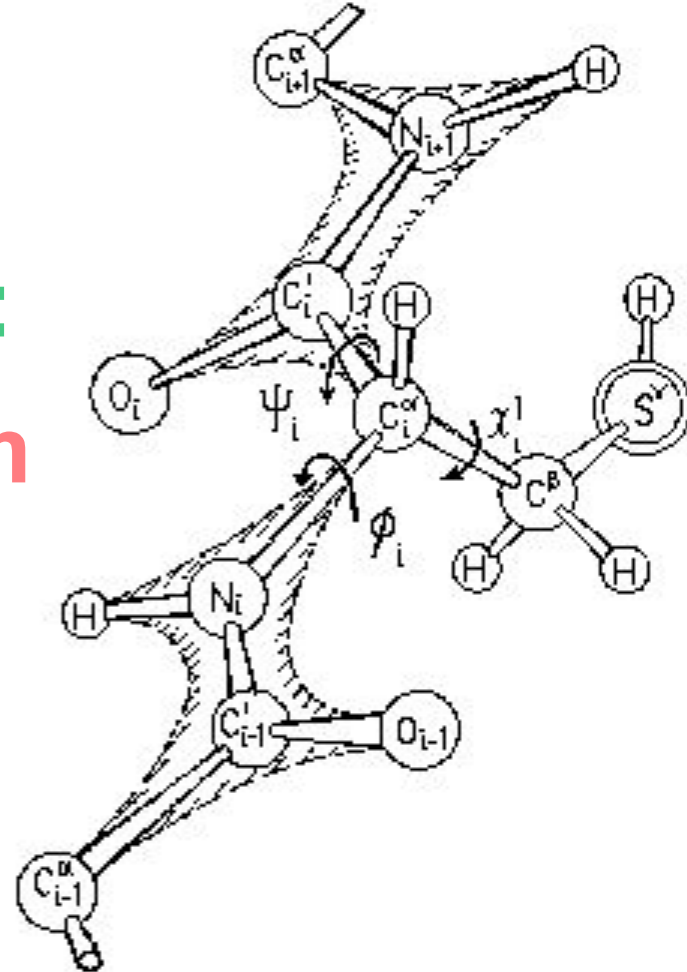
ALA



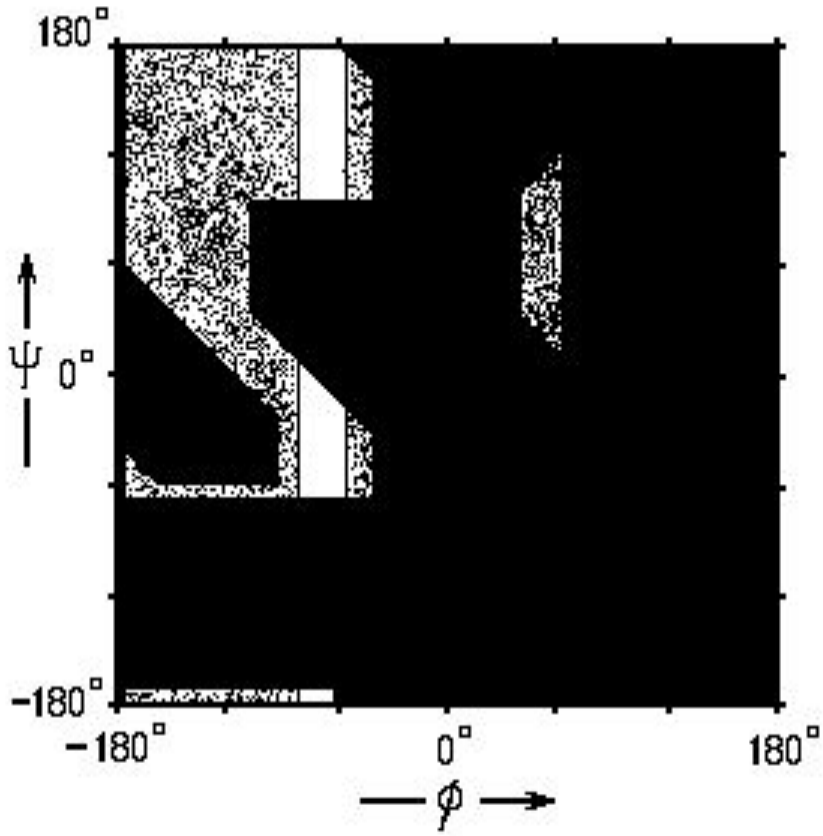
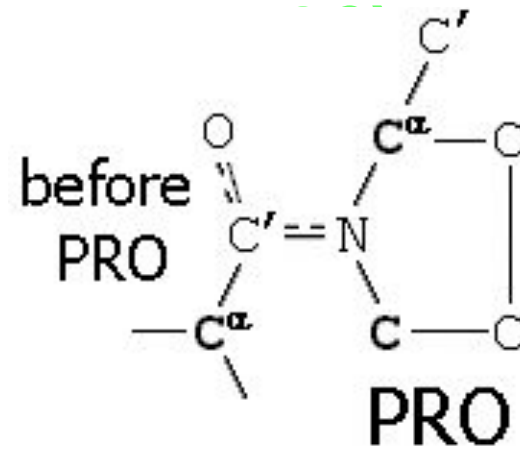
Gopalamudram Narayana Iyer  
Ramachandran(1922-2001)



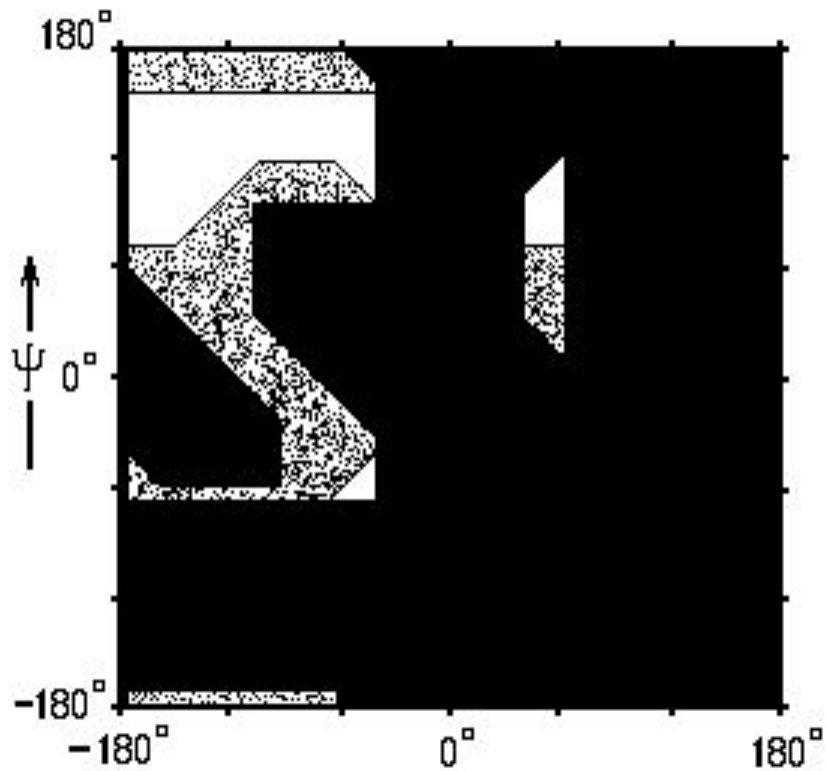
>ALA:  
 $\gamma$ -atoms



PRO ( $\phi =$

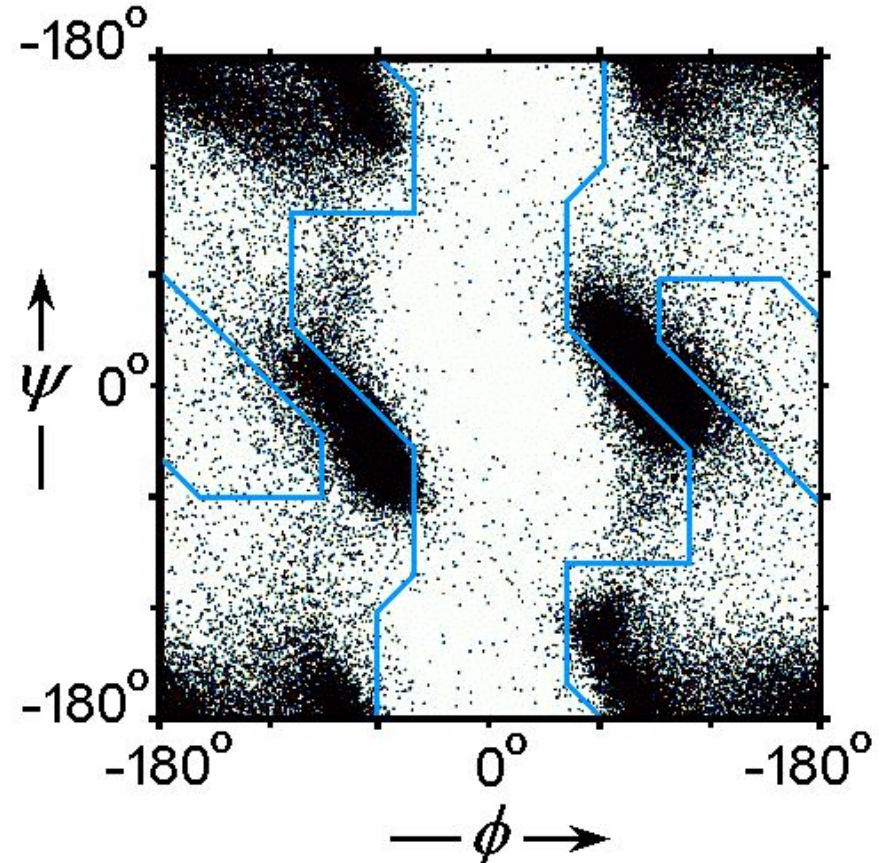
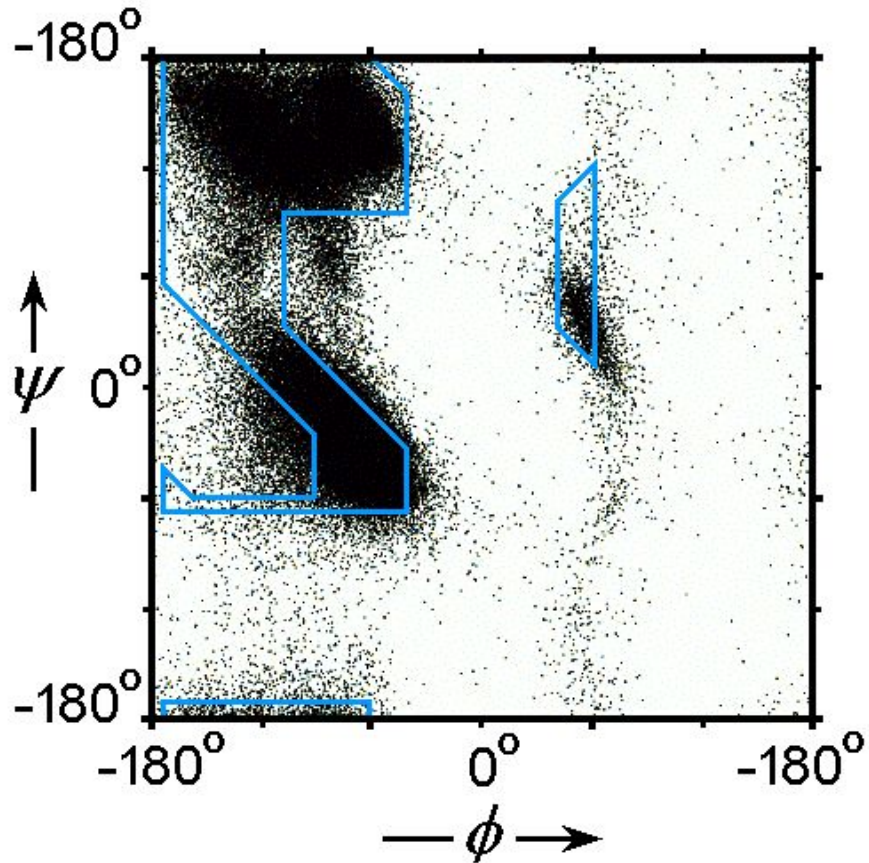


Before PRO



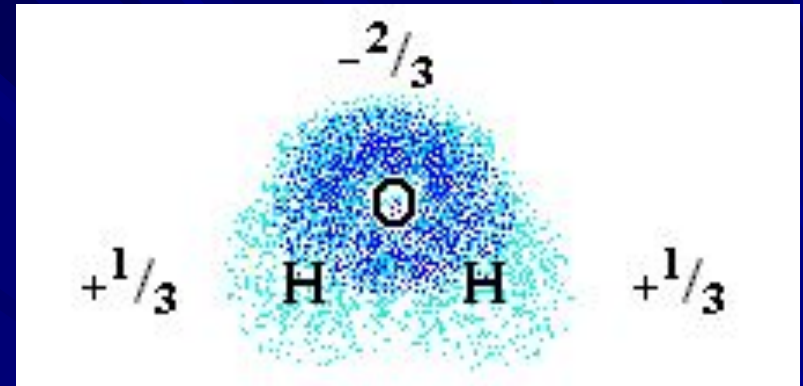
ALA, etc.

GLY only



# HYDROGEN BONDS

**WATER molecule:**



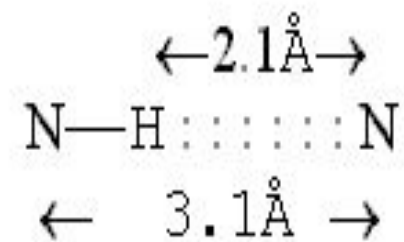
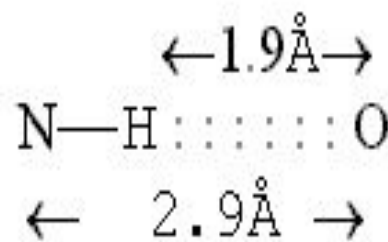
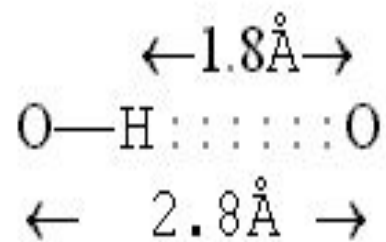
**H-bond energy: 5 kcal/mol**

**ICE sublimation: (12 kcal/mol - 2 kcal/mol[vdW])/2**  
**10 kcal/mol[CH<sub>3</sub>-CH<sub>2</sub>-OH] - 5 kcal/mol[CH<sub>3</sub>-O-CH<sub>3</sub>]**

$$U = q_1 q_2 / r$$

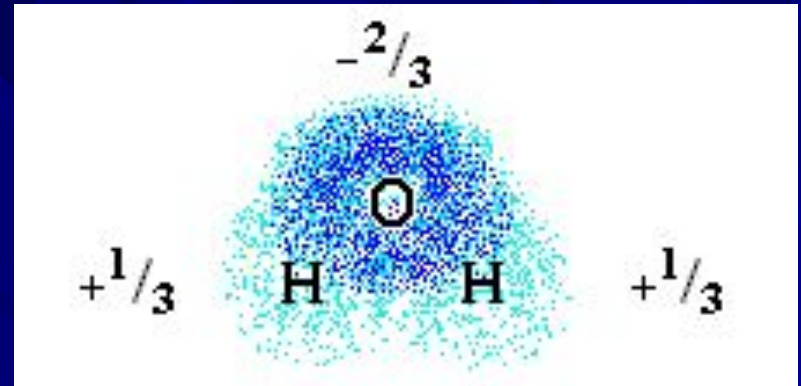
$$\epsilon = e \cdot e / 1\text{\AA} = 330 \text{ kcal/mol}$$

$$(\text{HO})^{-1/3} - \text{H}^{+1/3} \text{ : : : : } \text{O}^{-2/3} - \text{H}_2^{+2/3} : \quad \epsilon \cdot \frac{1}{3} \cdot \frac{2}{3} \cdot \left( -\frac{1}{2} - \frac{1}{4} + 2 \cdot \frac{1}{3} \right) \sim 6 \text{ kcal/mol}$$



# HYDROGEN BONDS

**WATER molecule:**



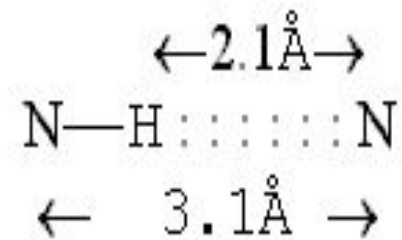
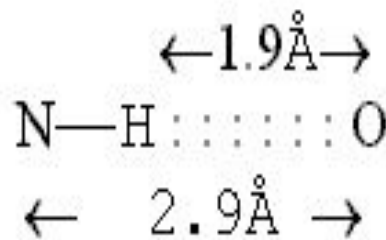
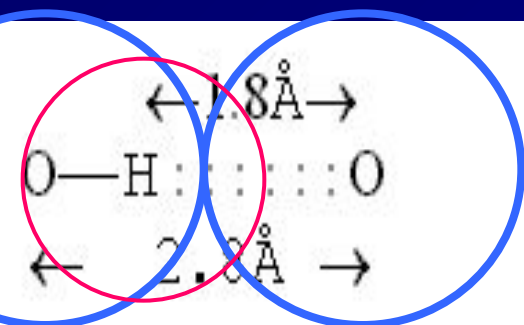
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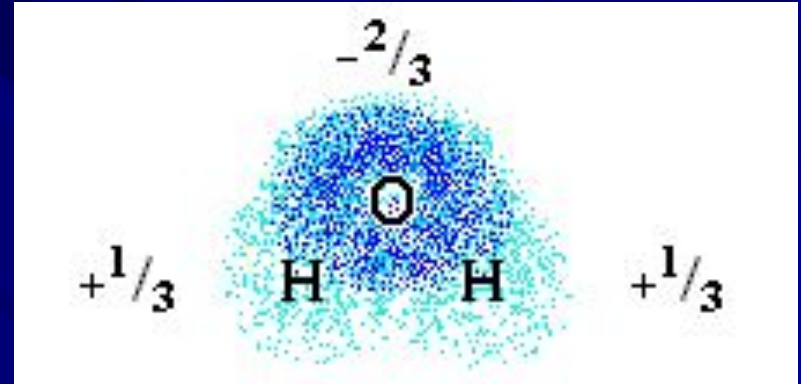
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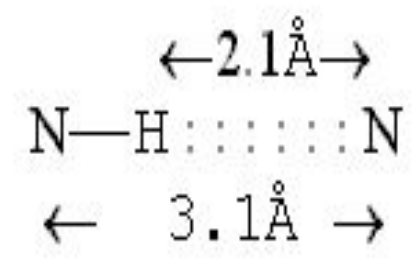
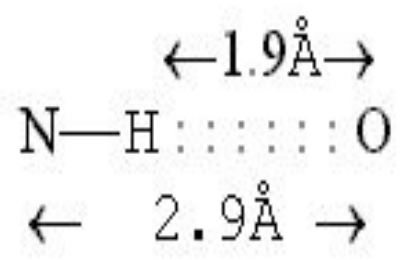
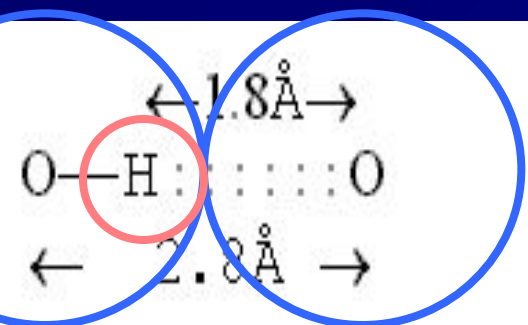
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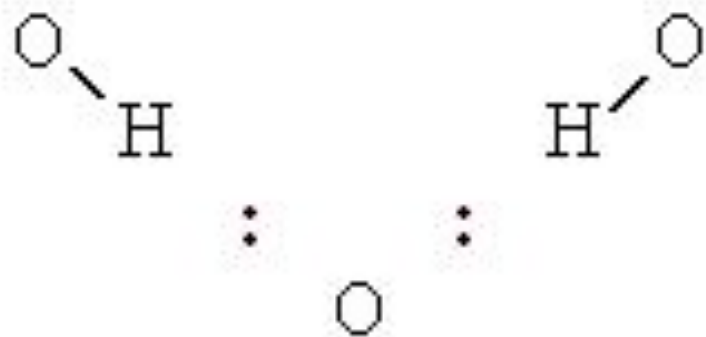
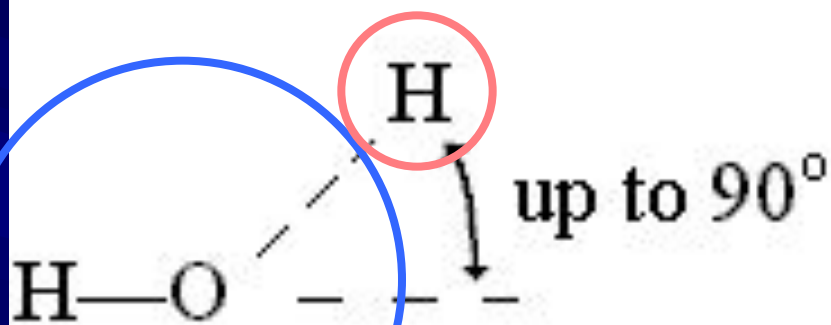
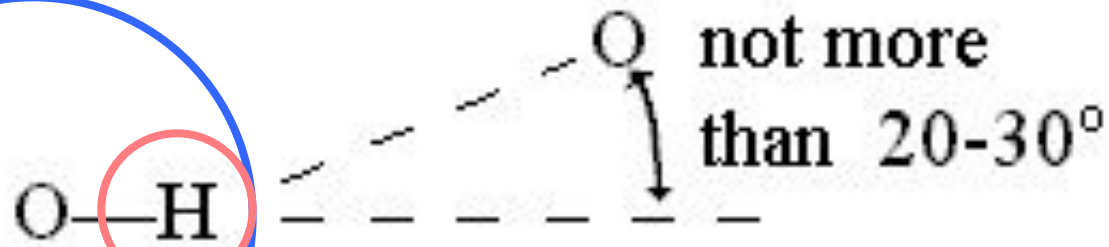
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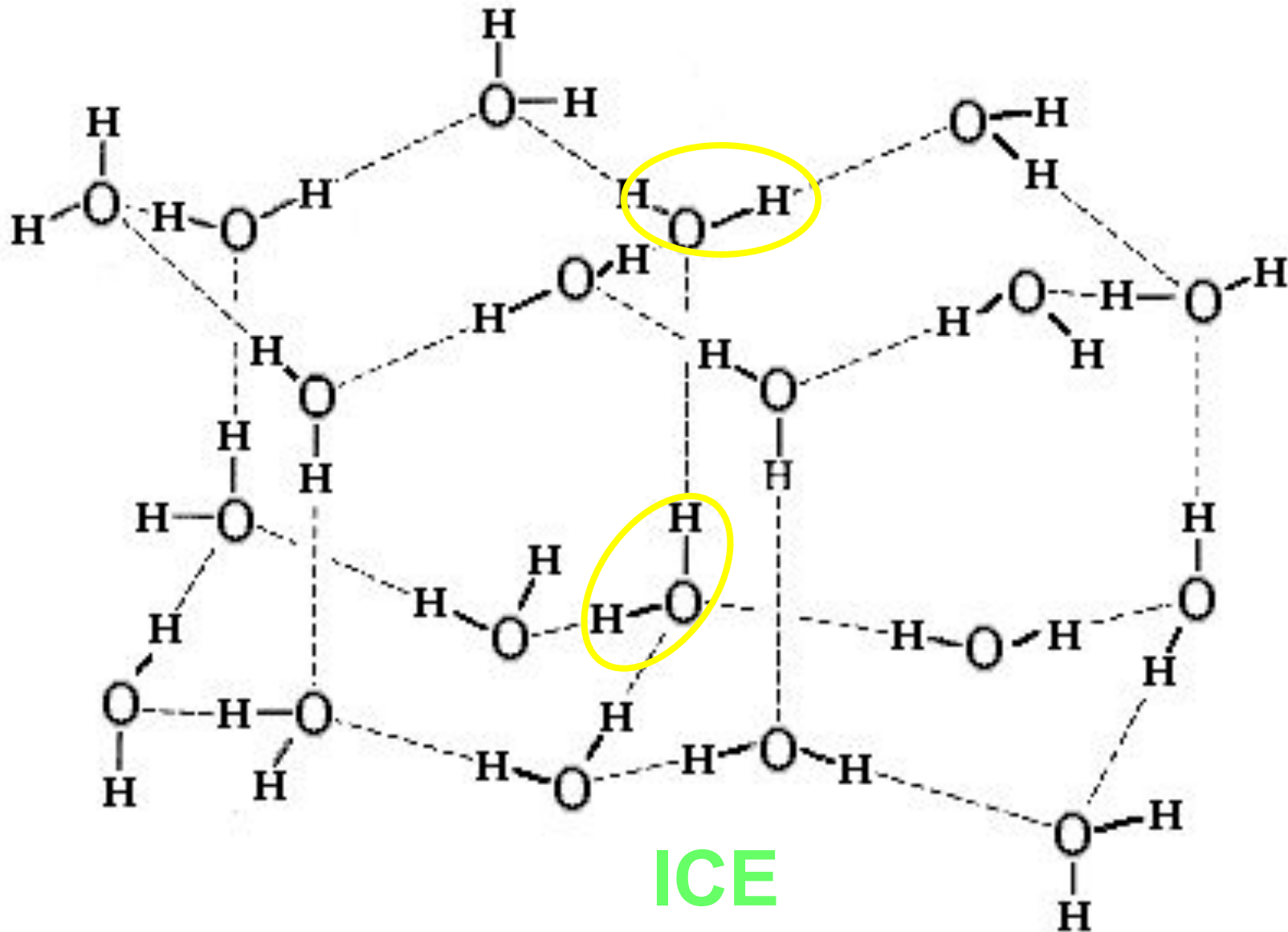
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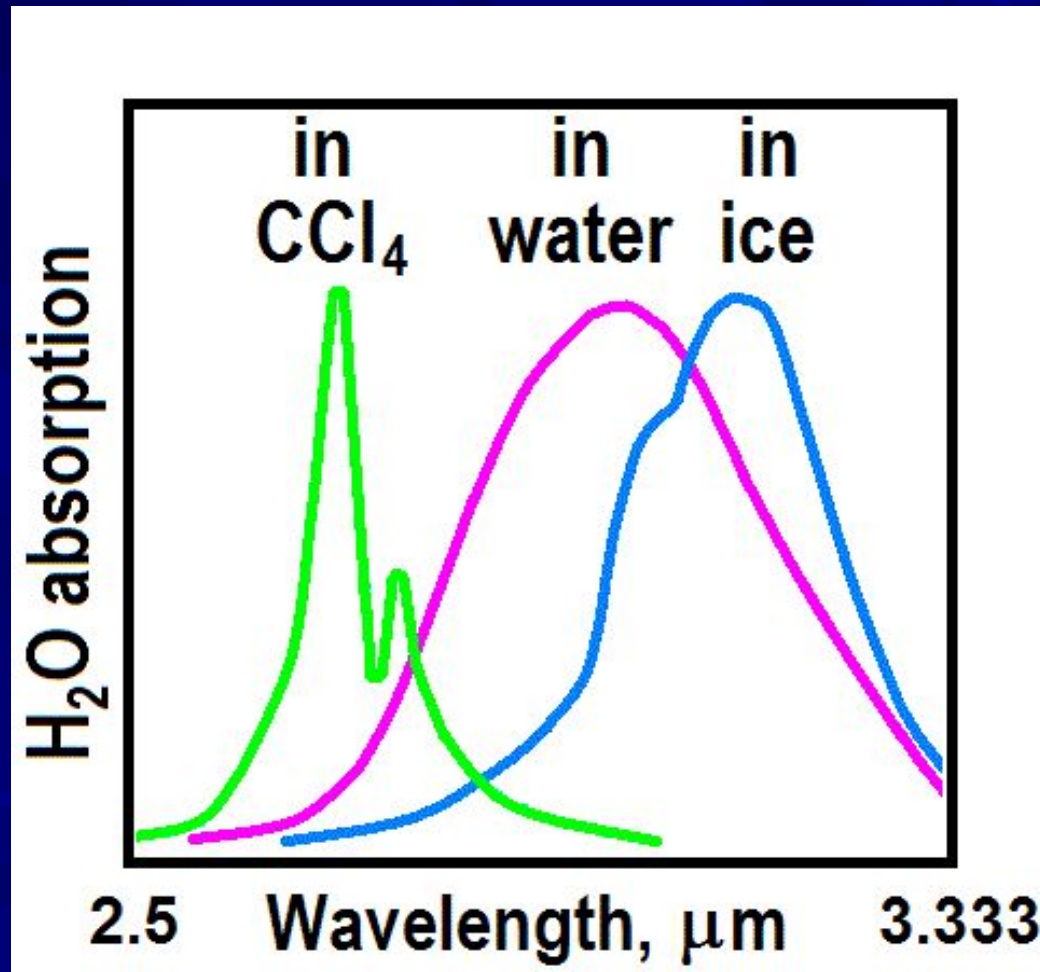




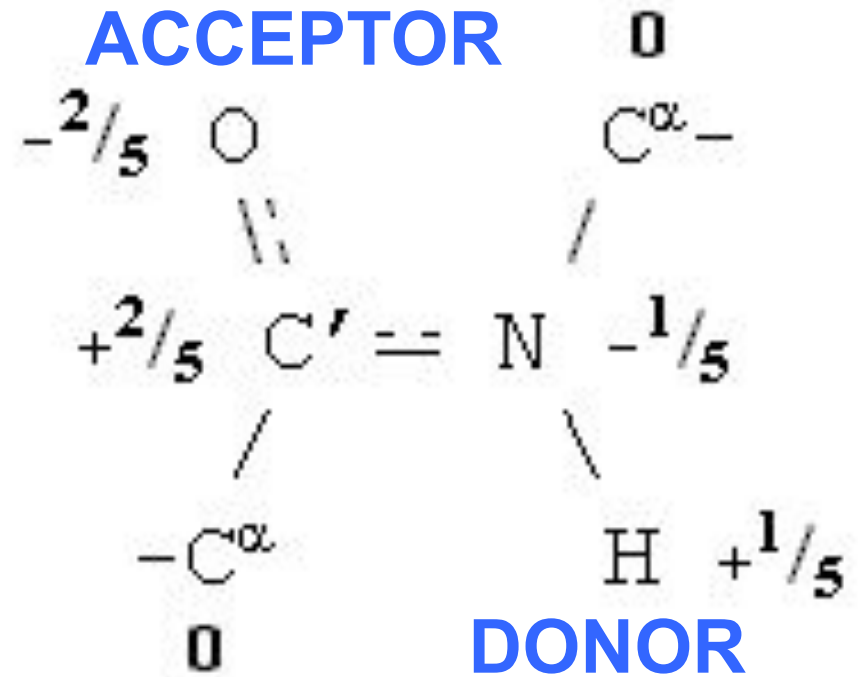




# MODEL OF “FORMED” and “BROKEN” H-BONDS IN WATER IS VERY ROUGH



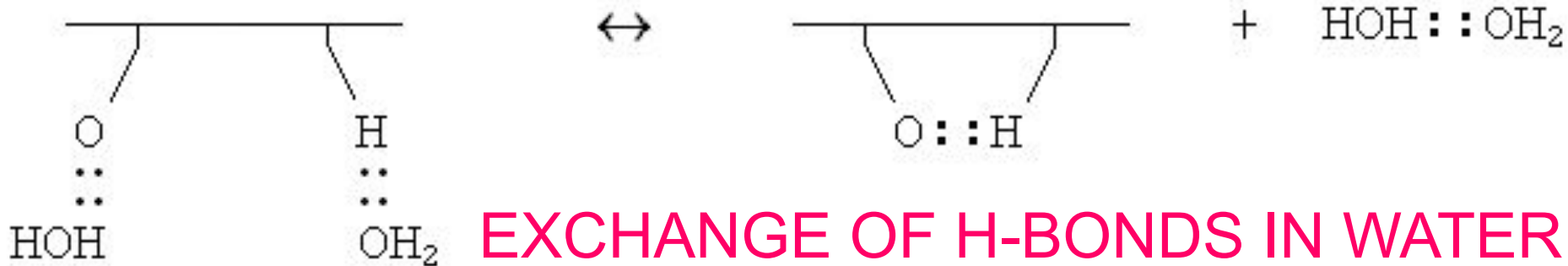
# PEPTIDE GROUP ALSO FORMS H-BONDS





FORMATION OF H-BOND IN VACUUM

ENERGY  $E$  decreases



EXCHANGE OF H-BONDS IN WATER

ENERGY  $E = \text{const}$       ENTROPY  $S \sim \ln(\text{pos.})$  increases

FREE ENERGY  $F = E - TS$  decreases: water moves

**Just because H-bonds have large energy,  
only their ENTROPIC part  
plays a role in water surrounding**