



# Chapter 16

## *Scheduling*

***Operations Management - 5<sup>th</sup> Edition***

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# Lecture Outline

- ◆ Objectives in Scheduling
- ◆ Loading
- ◆ Sequencing
- ◆ Monitoring
- ◆ Advanced Planning and Scheduling Systems
- ◆ Theory of Constraints
- ◆ Employee Scheduling

# What is Scheduling?

- ◆ Last stage of planning before production occurs
- ◆ Specifies when labor, equipment, facilities are needed to produce a product or provide a service

# Scheduled Operations

Scheduling function differs based on the type of operation

- ◆ Process Industry
  - Linear programming
  - EOQ with non-instantaneous replenishment
- ◆ Mass Production
  - Assembly line balancing
- ◆ Project
  - Project -scheduling techniques (PERT, CPM)
- ◆ Batch Production
  - Aggregate planning
  - Master scheduling
  - Material requirements planning (MRP)
  - Capacity requirements planning (CRP)

# Objectives in Scheduling

- ◆ Meet customer due dates
- ◆ Minimize job lateness
- ◆ Minimize response time
- ◆ Minimize completion time
- ◆ Minimize time in the system
- ◆ Minimize overtime
- ◆ Maximize machine or labor utilization
- ◆ Minimize idle time
- ◆ Minimize work-in-process inventory

# Shop Floor Control

- ◆ Loading
  - Check availability of material, machines and labor
- ◆ Sequencing
  - Release work orders to shop and issue dispatch lists for individual machines
- ◆ Monitoring
  - Maintain progress reports on each job until it is complete

# Loading

- ◆ Process of assigning work to limited resources
- ◆ Perform work on most efficient resources
- ◆ Use assignment method of linear programming to determine allocation

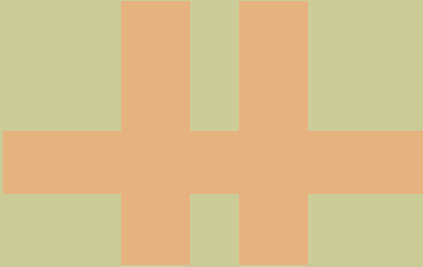
# Assignment Method

1. Perform row reductions
  - subtract minimum value in each row from all other row values
2. Perform column reductions
  - subtract minimum value in each column from all other column values
3. Cross out all zeros in matrix
  - use minimum number of horizontal and vertical lines
4. If number of lines equals number of rows in matrix then optimum solution has been found. Make assignments where zeros appear
5. Else modify matrix
  - subtract minimum uncrossed value from all uncrossed values
  - add it to all cells where two lines intersect
  - other values in matrix remain unchanged
6. Repeat steps 3 through 5 until optimum solution is reached



# Assignment Method: Example

Initial Matrix	PROJECT			
	1	2	3	4
Bryan	10	5	6	10
Kari	2	4	6	
Noah	7	6	5	6
Chris	9	5	4	10

Row reduction				Column reduction				Cover all zeros				
5	0	1	5	3	0	1	4	3	0	1	4	
4	0	2	4	2	0	2	3	2	0	2	3	
2	1	0	1	0	1	0	0	0	1	0	0	
5	1	0	6	3	1	0	5	3	1	0	5	
<p>Number lines <math>\neq</math> number of rows so modify matrix</p>												

# Assignment Method: Example (cont.)

Modify matrix

1	0	1	2	1
0	0	2	1	0
0	3	2	0	0
1	1	0	3	1

Cover all zeros

0	1	2		
0	2	1		
3	2	0		
1	0	3		

Number of lines = number of rows so at optimal solution

PROJECT

	1	2	3	4
Bryan	1	0	1	2
Kari	0	2	1	
Noah	0	3	2	0
Chris	1	1	0	3

PROJECT

	1	2	3	4
Bryan	10	5	6	10
Kari	6	2	4	6
Noah	7	6	5	6
Chris	9	5	4	10

$$\text{Project Cost} = (5 + 6 + 6 + 4) \times \$100 = \$2,100$$

# Sequencing

- Prioritize jobs assigned to a resource
- If no order specified use first-come first-served (FCFS)
- Many other sequencing rules exist
- Each attempts to achieve to an objective

# Sequencing Rules

- FCFS - first-come, first-served
- LCFS - last come, first served
- DDATE - earliest due date
- CUSTPR - highest customer priority
- SETUP - similar required setups
- SLACK - smallest slack
- CR - critical ratio
- SPT - shortest processing time
- LPT - longest processing time

# Critical Ratio Rule

CR considers both time and work remaining

$$CR = \frac{\text{time remaining}}{\text{work remaining}} = \frac{\text{due date} - \text{today's date}}{\text{remaining processing time}}$$

If  $CR > 1$ , job ahead of schedule

If  $CR < 1$ , job behind schedule

If  $CR = 1$ , job on schedule

# Sequencing Jobs Through One Process

- ◆ Flowtime (completion time)
  - Time for a job to flow through the system
- ◆ Makespan
  - Time for a group of jobs to be completed
- ◆ Tardiness
  - Difference between a late job's due date and its completion time

# Simple Sequencing Rules

JOB	PROCESSING TIME	DUE DATE
A	5	10
B	10	15
C	2	5
D	8	12
E	6	8

# Simple Sequencing Rules: FCFS

FCFS SEQUENCE	START TIME	PROCESSING TIME	COMPLETION DATE	DUE TARDINESS	
A	0	5	5	10	0
B	5	10	15	15	0
C	15	2	17	5	12
D	17	8	25	12	13
E	25	6	31	8	23



# Simple Sequencing Rules: DDATE

DDATE	START	PROCESSING	COMPLETION	DUE
SEQUENCE	TIME	TIME	DATE	TARDINESS
C	0	2	5	0
E	2	6	8	0
A	8	5	13	3
D	13	8	21	9
B	21	10	31	16

# Simple Sequencing Rules: SLACK

$$A \quad (10-0) - 5 =$$

5

$$B \quad (15-0) - 10 =$$

5

$$C \quad (5-0) - 2 = 3$$

$$D \quad (12-0) - 8 =$$

	SLACK	START	PROCESSING	COMPLETION	DUE
	SEQUENCE	TIME	TIME	DATE	TARDINESS

E	0	6	6	8	0
---	---	---	---	---	---

C	6	2	8	5	3
---	---	---	---	---	---

D	8	8	16	12	4
---	---	---	----	----	---

A	16	5	21	10	11
---	----	---	----	----	----

B	21	10	31	15	16
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# Simple Sequencing Rules: CR

$$A \quad (10)/5 = 2.00$$

$$B \quad (15)/10 = 1.50$$

$$C \quad (5)/2 =$$

CR	START	PROCESSING	COMPLETION	DUE
SEQUENCE	TIME	TIME	TIME	TARDINESS

E	0	6	6	8	0
D	6	8	14	12	2
B	14	10	24	15	9
A	24	5	29	10	19
C	29	2	31	5	26

# Simple Sequencing Rules: SPT

SPT	START	PROCESSING	COMPLETION	DUE	
SEQUENCE	TIME	TIME	TIME	DATE	TARDINESS
C	0	2	2	5	0
A	2	5	7	10	0
E	7	6	13	8	5
D	13	8	21	12	9
B	21	10	31	15	16

# Simple Sequencing Rules: Summary

	AVERAGE RULE	AVERAGE COMPLETION TIME	AVERAGE NO. OF TARDINESS	MAXIMUM JOBS TARDY
<b>TARDINESS</b>				
FCFS	18.60	9.6	3	23
DDATE	15.00	5.6	3	16
SLACK	16.40	6.8	4	16
CR	20.80	11.2	4	26
SPT	14.80	6.0	3	16

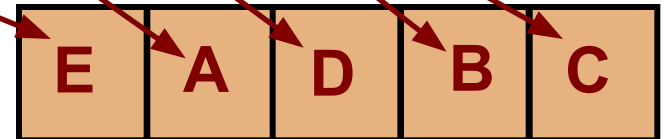
# Sequencing Jobs Through Two Serial Process

## Johnson's Rule

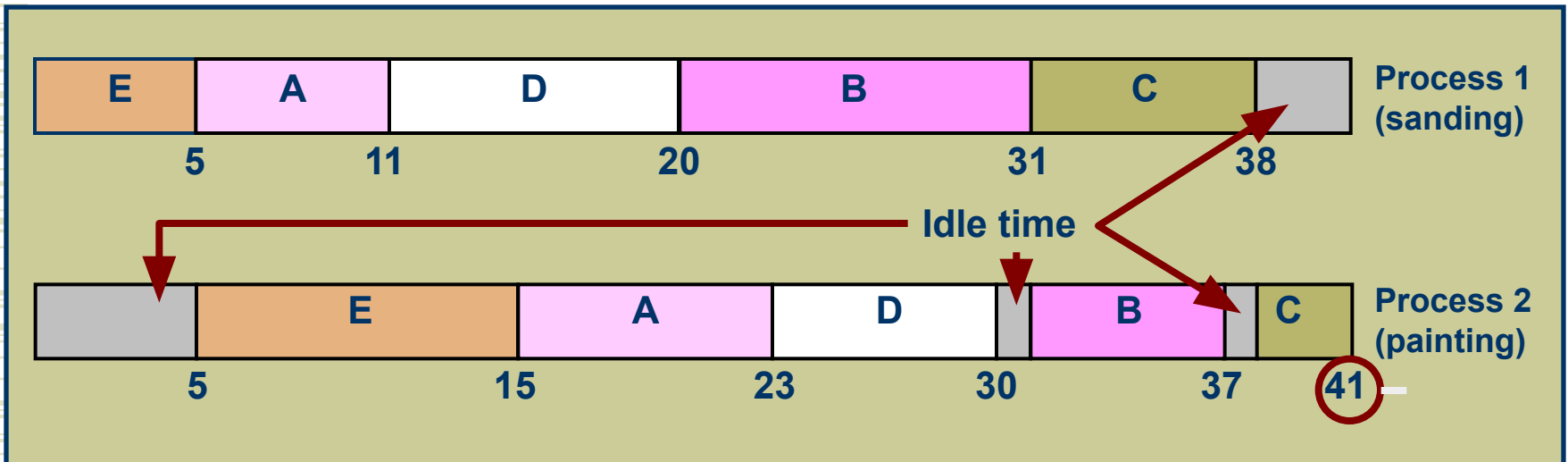
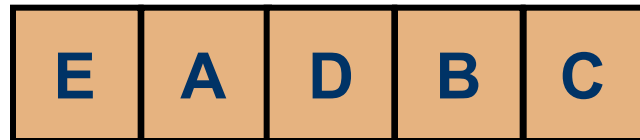
1. List time required to process each job at each machine. Set up a one-dimensional matrix to represent desired sequence with # of slots equal to # of jobs.
2. Select smallest processing time at either machine. If that time is on machine 1, put the job as near to beginning of sequence as possible.
3. If smallest time occurs on machine 2, put the job as near to the end of the sequence as possible.
4. Remove job from list.
5. Repeat steps 2-4 until all slots in matrix are filled and all jobs are sequenced.

# Johnson's Rule

JOB	PROCESS 1	PROCESS 2
A	6	8
B	11	6
C	7	3
D	9	7
E	5	10



# Johnson's Rule (cont.)



Completion time = 41

Idle time =  $5+1+1+3=10$



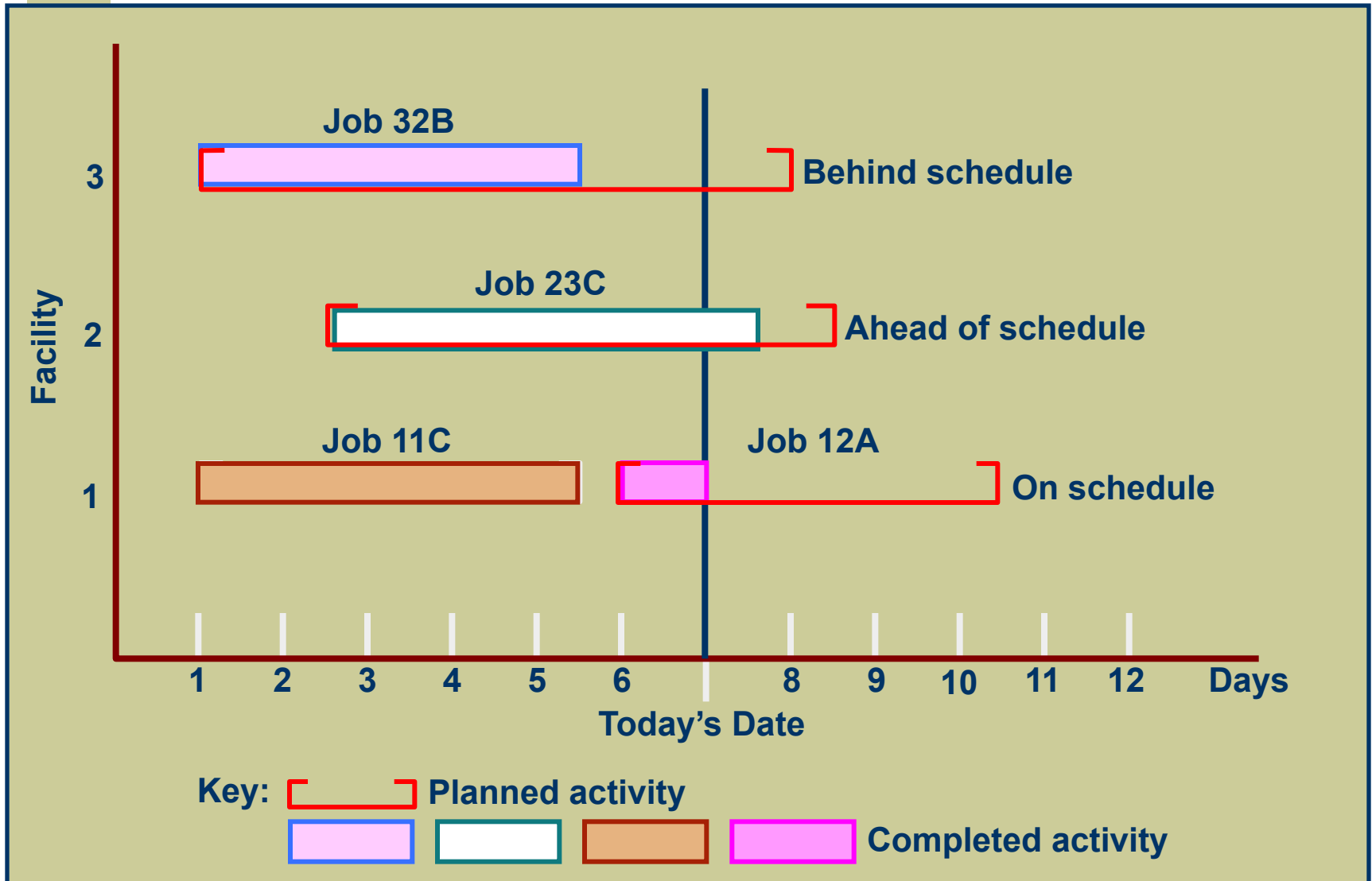
# Guidelines for Selecting a Sequencing Rule

1. SPT most useful when shop is highly congested
2. Use SLACK for periods of normal activity
3. Use DDATE when only small tardiness values can be tolerated
4. Use LPT if subcontracting is anticipated
5. Use FCFS when operating at low-capacity levels
6. Do not use SPT to sequence jobs that have to be assembled with other jobs at a later date

# Monitoring

- ◆ Work package
  - Shop paperwork that travels with a job
- ◆ Gantt Chart
  - Shows both planned and completed activities against a time scale
- ◆ Input/Output Control
  - Monitors the input and output from each work center

# Gantt Chart



# Input/Output Control

## Input/Output Report

PERIOD	1	2	3	4	TOTAL
--------	---	---	---	---	-------

---

Planned input				65	65	70	70
---------------	--	--	--	----	----	----	----

Actual input			60	60	65	65	
--------------	--	--	----	----	----	----	--

Deviation

Planned output				75	75	75	75
----------------	--	--	--	----	----	----	----

Actual output			70	70	65	65	
---------------	--	--	----	----	----	----	--

Deviation

Backlog	30						
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# Input/Output Control (cont.)

## Input/Output Report

PERIOD	1	2	3	4	TOTAL	
Planned input				60 65 70 75	270	
Actual input			60 60	65 65	250	
Deviation	0	-5	-5	-10	-20	
Planned output				75 75 75 75	300	
Actual output			70 70	65 65	270	
Deviation		-5	-5	-10	-10	-30
Backlog	30	20	10	10	10	

# Advanced Planning and Scheduling Systems

- ◆ Infinite - assumes infinite capacity
  - Loads without regard to capacity
  - Then levels the load and sequences jobs
- ◆ Finite - assumes finite (limited) capacity
  - Sequences jobs as part of the loading decision
  - Resources are never loaded beyond capacity

# Advanced Planning and Scheduling Systems (cont.)

- ◆ Advanced planning and scheduling (APS)
  - Add-ins to ERP systems
  - Constraint-based programming (CBP) identifies a solution space and evaluates alternatives
  - Genetic algorithms based on natural selection properties of genetics
  - Manufacturing execution system (MES) monitors status, usage, availability, quality

# Theory of Constraints

- ◆ Not all resources are used evenly
- ◆ Concentrate on the” bottleneck” resource
- ◆ Synchronize flow through the bottleneck
- ◆ Use process and transfer batch sizes to move product through facility



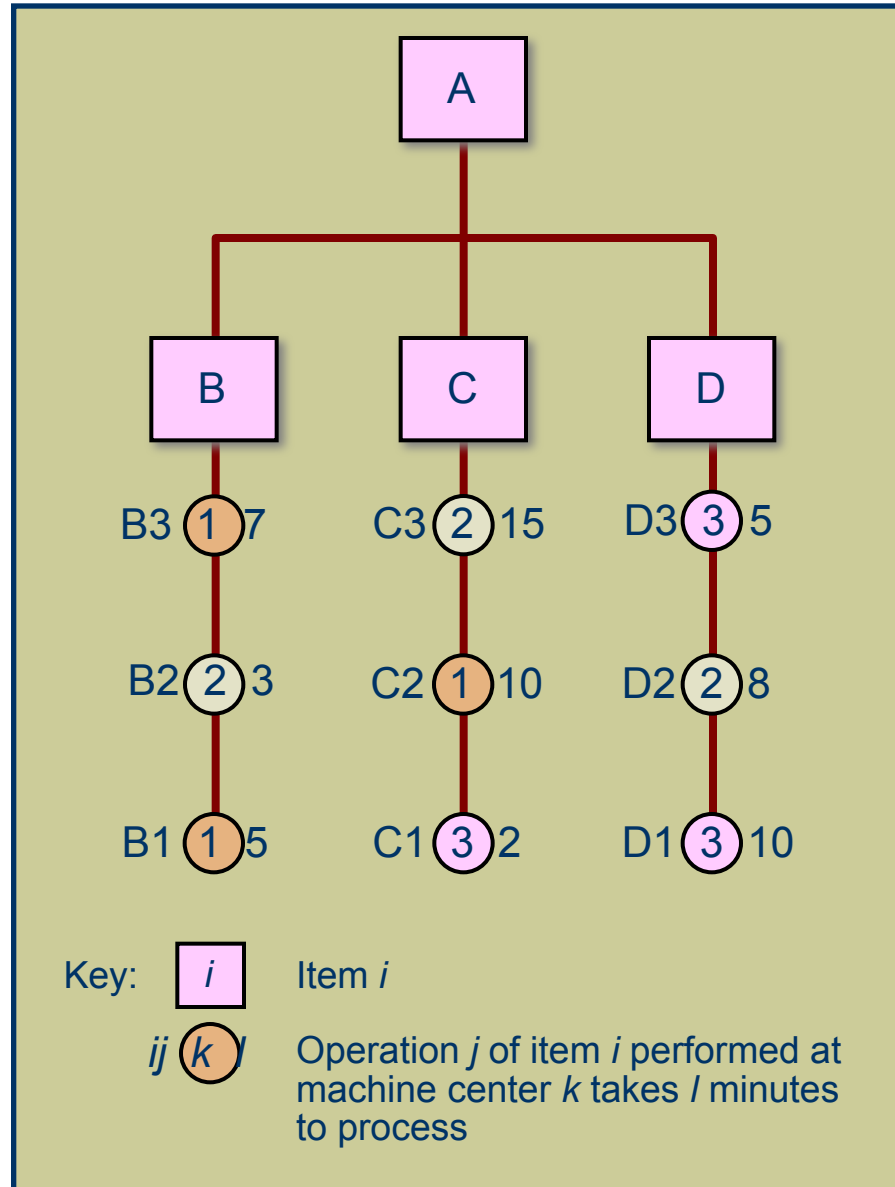
# Drum-Buffer-Rope

- ◆ Drum
  - Bottleneck, beating to set the pace of production for the rest of the system
- ◆ Buffer
  - Inventory, placed in front of the bottleneck to ensure it is always kept busy
  - Determines output or throughput of the system
- ◆ Rope
  - Communication signal, tells processes upstream when they should begin production

# TOC Scheduling Procedure

- ◆ Identify bottleneck
- ◆ Schedule job first whose lead time to the bottleneck is less than or equal to the bottleneck processing time
- ◆ Forward schedule the bottleneck machine
- ◆ Backward schedule the other machines to sustain the bottleneck schedule
- ◆ Transfer in batch sizes smaller than the process batch size

# Synchronous Manufacturing



# Synchronous Manufacturing (cont.)

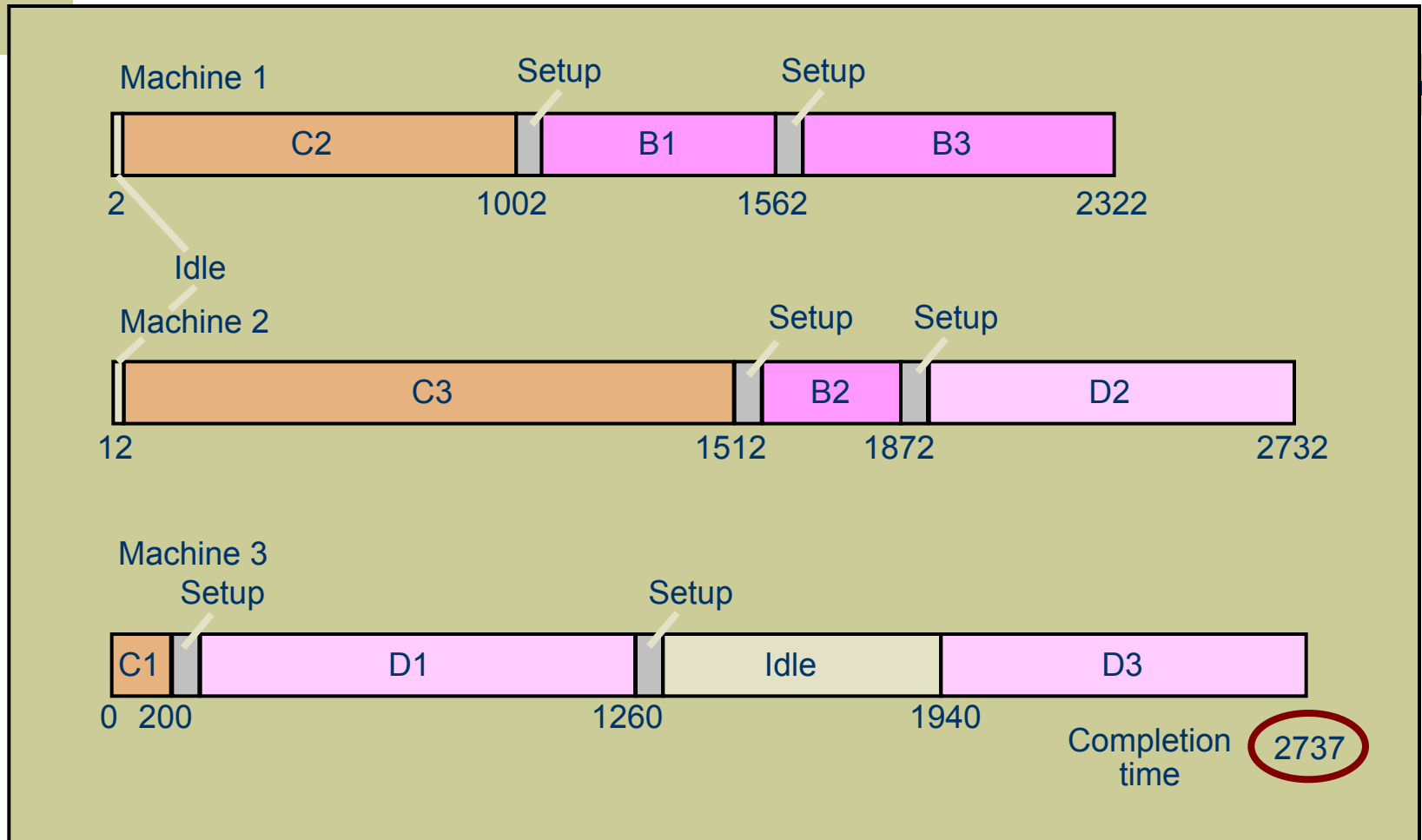
Demand = 100 A's

Machine setup time = 60 minutes

	MACHINE 1	MACHINE 2		
<del>MACHINE 3</del>				
B1	5	B2 3	C1	2
B3	7	C3 15	D3	5
C2	10	D2 8	D1	10
Sum	22	26*		17

\* Bottleneck

# Synchronous Manufacturing (cont.)



# Employee Scheduling

- ◆ Labor is very flexible resource
- ◆ Scheduling workforce is complicated repetitive task
- ◆ Assignment method can be used
- ◆ Heuristics are commonly used



# Employee Scheduling Heuristic

1. Let  $N$  = no. of workers available  
 $D_i$  = demand for workers on day  $i$   
 $X$  = day working  
 $O$  = day off
2. Assign the first  $N - D_1$  workers day 1 off. Assign the next  $N - D_2$  workers day 2 off. Continue in a similar manner until all days are have been scheduled
3. If number of workdays for full time employee  $< 5$ , assign remaining workdays so consecutive days off are possible
4. Assign any remaining work to part-time employees
5. If consecutive days off are desired, consider switching schedules among days with the same demand requirements

# Employee Scheduling

DAY OF WEEK	M	T	W	TH	F	SA	SU		
MIN NO. OF WORKERS REQUIRED			3	3	4	3	4	5	3

Taylor

Smith

Simpson

Allen

Dickerson



# Employee Scheduling (cont.)

DAY OF WEEK	M	T	W	TH	F	SA	SU		
MIN NO. OF WORKERS REQUIRED			3	3	4	3	4	5	3
Taylor	O	X	X	O	X	X	X		
Smith	O	X	X	O	X	X	X		
Simpson	X	O	X	X	O	X	X		
Allen	X	O	X	X	X	X	O		
Dickerson	X	X	O	X	X	X	O		

Completed schedule satisfies requirements but has no consecutive days off

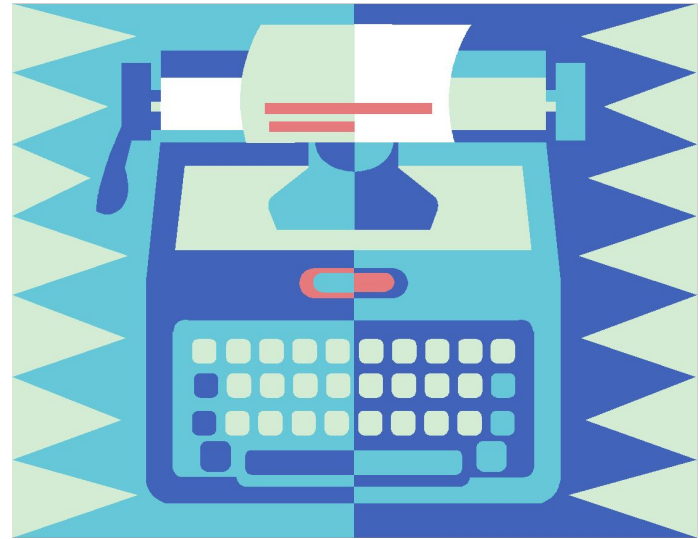
# Employee Scheduling (cont.)


DAY OF WEEK	M	T	W	TH	F	SA	SU		
MIN NO. OF WORKERS REQUIRED			3	3	4	3	4	5	3
Taylor	O	O	X	X	X	X	X		
Smith	O	O	X	X	X	X	X		
Simpson	X	X	O	O	X	X	X		
Allen	X	X	X	O	X	X	O		
Dickerson	X	X	X	X	O	X	O		

Revised schedule satisfies requirements with consecutive days off for most employees

# Automated Scheduling Systems

- ◆ Staff Scheduling
- ◆ Schedule Bidding
- ◆ Schedule Optimization





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