

**Introduction to
Effective Permeability
and
Relative Permeability**

Review: Absolute Permeability

- Absolute permeability: is the permeability of a porous medium saturated with a single fluid (e.g. $S_w=1$)
- Absolute permeability can be calculated from the steady-state flow equation (1D, Linear Flow; Darcy Units):

$$q = \frac{k A \Delta p}{\mu L}$$

Multiphase Flow in Reservoirs

Commonly, reservoirs contain 2 or 3 fluids

- **Water-oil systems**
- **Oil-gas systems**
- **Water-gas systems**
- **Three phase systems (water, oil, and gas)**

To evaluate multiphase systems, must consider the effective and relative permeability

Effective Permeability

Effective permeability: is a measure of the conductance of a porous medium for one fluid phase when the medium is saturated with more than one fluid.

- The porous medium can have a distinct and measurable conductance to each phase present in the medium
- Effective permeabilities: (k_o, k_g, k_w)

Effective Permeability

- Oil

$$q_o = \frac{k_o A \Delta\Phi_o}{\mu_o L}$$

Steady state, 1D, linear flow equation (Darcy units):

q_n = volumetric flow rate for a specific phase, n

- Water

$$q_w = \frac{k_w A \Delta\Phi_w}{\mu_w L}$$

A = flow area

$\Delta\Phi_n$ = flow potential drop for phase, n (including pressure, gravity and capillary pressure terms)

- Gas

$$q_g = \frac{k_g A \Delta\Phi_g}{\mu_g L}$$

μ_n = fluid viscosity for phase n

L = flow length

Relative Permeability

Relative Permeability is the ratio of the effective permeability of a fluid at a given saturation to some base permeability

- **Base permeability is typically defined as:**
 - absolute permeability, k
 - air permeability, k_{air}
 - effective permeability to non-wetting phase at irreducible wetting phase saturation [e.g. $k_o(S_w = S_{wi})$]
 - because definition of base permeability varies, the definition used must always be:
 - confirmed before applying relative permeability data
 - noted along with tables and figures presenting relative permeability data

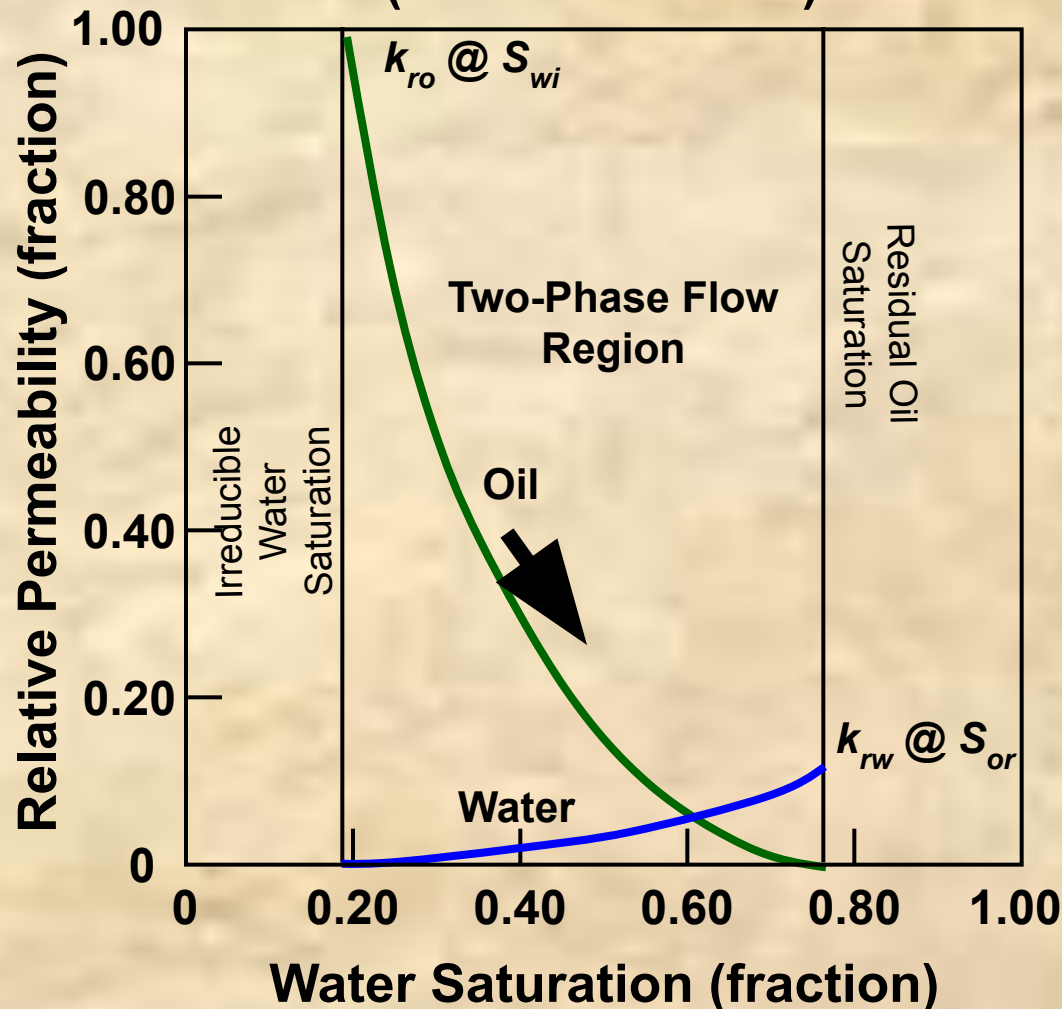
Relative Permeability

- **Oil** $k_{ro(0.5,0.3)} = \frac{k_{o(0.5,0.3)}}{k}$
- **Water** $k_{rw(0.5,0.3)} = \frac{k_{w(0.5,0.3)}}{k}$
- **Gas** $k_{rg(0.5,0.3)} = \frac{k_{g(0.5,0.3)}}{k}$

$S_o = 0.5$
 $S_w = 0.3$
 $\therefore S_g = 0.2$

Relative Permeability Functions

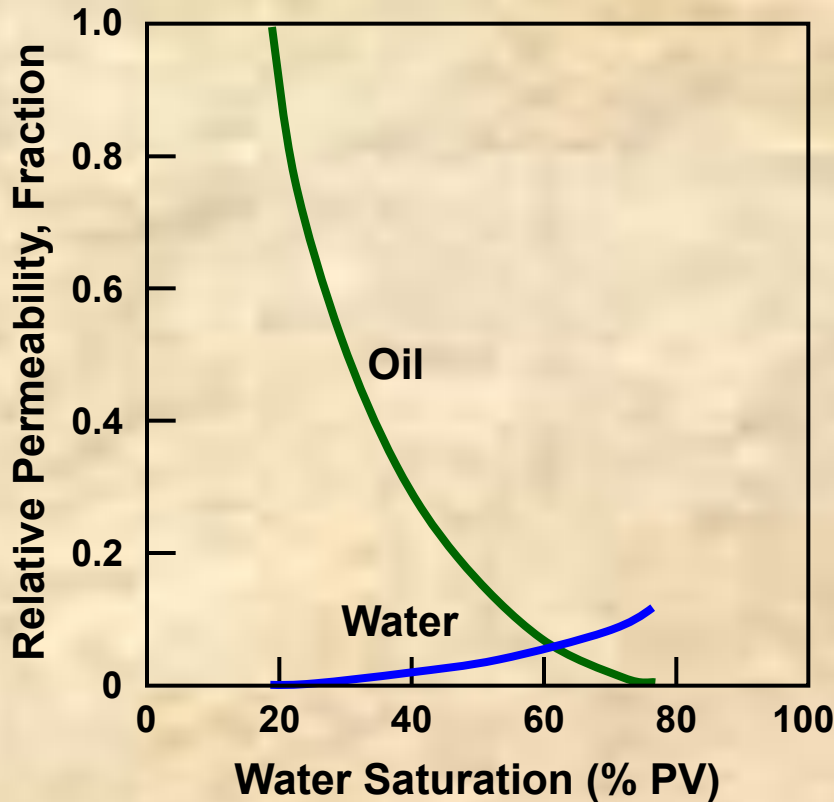
Imbibition Relative Permeability (Water Wet Case)



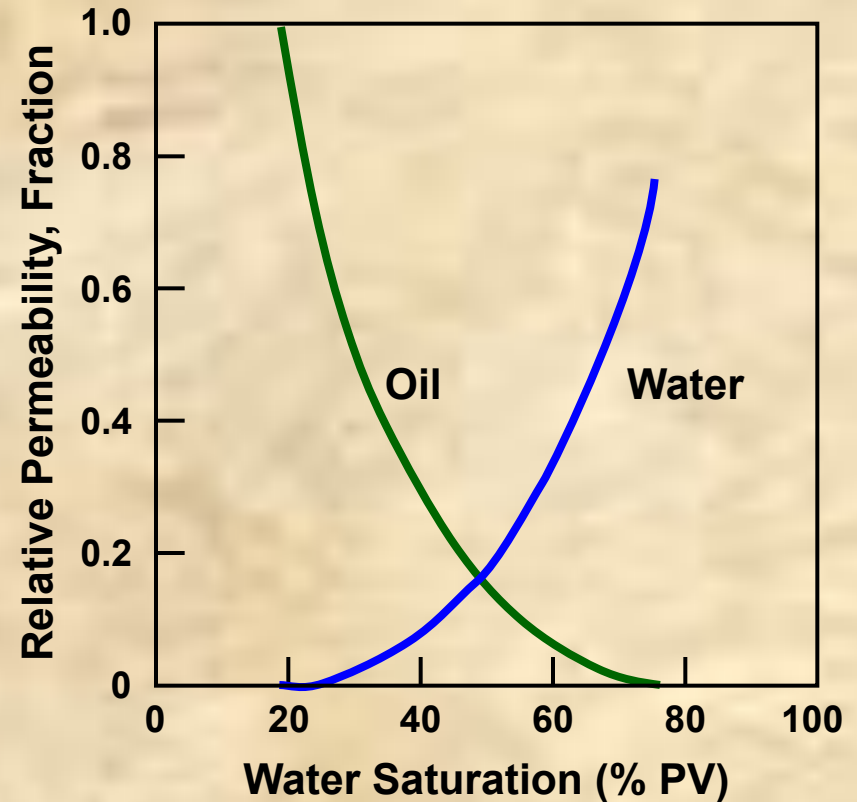
- Wettability and direction of saturation change must be considered
 - drainage
 - imbibition
- Base used to normalize this relative permeability curve is $k_{ro} @ S_{wi}$
- As S_w increases, k_{ro} decreases and k_{rw} increases until reaching residual oil saturation

Modified from NExT, 1999

Effect of Wettability for Increasing S_w



Strongly Water-Wet Rock



Strongly Oil-Wet Rock

Modified from NExT, 1999

- Water flows more freely
- Higher residual oil saturation

Factors Affecting Relative Permeabilities

- **Fluid saturations**
- **Geometry of the pore spaces and pore size distribution**
- **Wettability**
- **Fluid saturation history (i.e., imbibition or drainage)**

Characteristics of Relative Permeability Functions

- **Relative permeability is unique for different rocks and fluids**
- **Relative permeability affects the flow characteristics of reservoir fluids.**
- **Relative permeability affects the recovery efficiency of oil and/or gas.**

Applications of Relative Permeability Functions

- **Reservoir simulation**
- **Flow calculations that involve multi-phase flow in reservoirs**
- **Estimation of residual oil (and/or gas) saturation**