Statistical Terminology

Correlation

What is correlation?

- A statistical measurement that shows the relationship between two variables.
- Example: Height & Weight

Pearson's Correlation Coefficient

Pearson's r, which measures a 'normalized' covariance (how changes in one value are associated with those of another), has a value between -1 and 1

- 1 perfect positive linear correlation
- 0 no linear correlation
- -1 perfect negative linear correlation

Correlation types

- Positive correlation
 - An increase in one variable will lead to an increase in the other
- Negative correlation
 - An increase in one variable will lead to a decrease in the other
- Note: In System Dynamics, these are called Positive and Negative Feedback loops

Knowledge check

- Height and weight
- Vehicle speed and travel time
- Gasoline prices and global oil production
- Caloric intake and weight
- Hours spent watching TV and school grades
- Car value and car mileage

In WWII, the US formed the Statistical Research Group to analyze situations like the following:

You don't want your planes shot down by enemy fighters, so you armor them. Armor makes the plane heavier, and heavier planes are slower and use more fuel. Too much armor and too little armor is bad. Where do you armor them?

Case Study (cont)

When planes returned from missions, damage was unevenly distributed. The fuselage and fuel system would often have many bullet holes whereas the engines would have few. Should you put more armor on the fuselage?

Case Study (cont)

Tip: Set a variable to zero to test the probability.

Ex.: By imagining that a plane is CERTAIN to be hit in the engine, the plane is CERTAIN to crash because planes can't fly without working engines.

Either German planes happen to hit every part of a plane but the engine, or the engine is a point of total vulnerability.

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Cloud cover. If there are too many clouds, fighters aren't launched and bombers are inaccurate.

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Adopting such a parental strategy indicates the parents are interested in the child's intelligence.

Economist recently announced that statistics prove the taller you are, the more you are likely to be paid. Why?

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The lurking variable is more likely gender, as typically men are on average taller than women.

Statistical Terminology

Sample

• A portion of a population

Stratified Sample

• The sample is chosen to reflect the population at large

Random Sample

• The sample is chosen by chance

Generalization

• Extending conclusions from the sample to the population. Only possible is sample is reflective.

Causation

- When changes in one variable affect the other Elasticity
- How much a change in one variable affects the other Bias or Skew

Margin of Error

Mean

- The average after adding and dividing all data Median
- The middle number of a dataset Mode
- Number(s) appearing most often in a dataset

Discrete variable

- A variable with a finite amount of values Continuous variable
- A variable with many different values in a range

Variance

"The average of the squared differences from the mean" \Box how different the data is

- Ex.: [12, 12, 12, 12, 12]
- Variance = 0
- Ex.: [12, 12, 12, 12, 13]
- Variance = 0.16
- Ex.: [12, 12, 12, 12, 13013]
- Variance = 27,044,160

Standard Deviation

The square root of the variance (more precise than variance) \Box This is the main reason for variance

Standard Deviation Example

Dataset of height of cats in cm: [600, 470, 170, 430, 300]

Find the variance (Find the mean, calculate the difference of each datum from the mean, square, then average).

• 21,704

Find the standard deviation (square root of the mean).

• ~147

Standard Deviation Example

If the standard deviation is 147, then a datum is "1 standard deviation from the mean". A datum "2 standard deviations is 296" and so on...

HOWEVER...

This is has been a 'population' standard deviation where each possible value was considered.

Sample Standard Deviation

How is the sample SD different from the population SD? How to correct the calculation?

Divide by 'n-1' instead of 'n' when finding both the variance and SD. Now find the sample SD and sample variance of the previous dataset.

Sample variance = 27,130 Sample SD = 164

- Regression Analysis: estimates relationships between X and Y variables
- Null hypothesis: Assumes no significant difference (states alternative hypothesis false)

Descriptive & Inferential Stats

- Descriptive statistics
 - Describes what's happening in a dataset
- Inferential statistics
 - Generalizes sample findings to population

Descriptive & Inferential Stats

- 50% of all Russian men are named Ivan.
- 20% of respondents are male
- From 2000 to 2005, 70% of the land cleared in the Amazon and recorded in Brazilian government data was transformed into pasture.
- Receive your college degree increases your lifetime earning by 50%.
- Teachers named Joshua demonstrate inferior intellect to teachers named Timmy.

Question Design

Open-ended vs. Closed-ended

- Open-ended
 No response options provided
- Closed-ended
 A list of options provided

Fewer People Mention Economy in Open-Ended Version

What one issue mattered most to you in deciding how you voted for president?

	Open- ended ¹	Closed- ended ²
The economy	35%	58%
The war in Iraq	5	10
Health care	4	8
Terrorism	6	8
Energy policy	*	6
Other	43	8
Candidate mentions	9	73
Moral values/social issue	s 7	7.8
Taxes/dist. of income	7	29
Other issues	5	÷3
Other political mentions	3	53
Change	3	7.8
Other	9	20
Don't know	7	2
	100	100

Data from Pew Research November 2008 Post-election survey

¹ Unprompted first responce to open-ended question.

² First choice from five options read to respondents.

Open-ended vs. Closed-ended

- Open-ended used in pilot studies to determine most common options
- Subjective closed-ended
 Fewer options
 - Satisfaction with economy
 - Fewer options avoids "recency effect"
 - Randomized order to ensure random bias
- Objective closed-ended
 More options fine
 - Religious affliation

Closed-ended example

Form a question asking about a student's satisfaction with their high school education (hint \Box use ordinal categories).

How can you mitigate the recency effect?

Question wording

Be aware of information and connotations in questions.

"Do you favor or oppose taking military action against Saddam Hussein?" Favor = 68%; Oppose = 25%

Question wording

Be aware of information and connotations in questions.

"Do you favor or oppose taking military action against Saddam Hussein even if it meant that U.S. forces might suffer thousands of casualties?"

Favor = 43%; Oppose = 48%

Question Structure

- All reasonable responses included if closed.
- Responses shouldn't overlap.
- One question at a time.
 - Bad: "How much confidence do you have in
 Obama to handle domestic and foreign policy?"

Question Structure

Leading questions

• Do you think that the new cafeteria lunch menu offers a better variety of healthy foods?

Neutral questions

 How do you feel about the new cafeteria lunch menu compared to the old one?

Social desirability bias

- Sensitive issues lead to misreporting
- Understated alcohol/drug use, tax evasion
- Overstated donations, church attendance
- SDB higher when interviewer is present
- Include 'Prefer Not to Answer' option

- Contrast effects
 - When order results in greater differences in responses
- Assimilation effects
 - When responses are similar because of order

More	People Favor	Civil	Unions	When	Asked
After	Gay Marriage				

Asked first	Legal agreements	%	Gay marriage	%
	Favor	37	Favor	33
	Oppose	55	Oppose	61
	Don't know	8	Don't know	6
		100		100
Asked second	Gay marriage		Legal agreements	
	Favor	30	Favor	45
	Oppose	58	Oppose	47
	Don't know	12	Don't know	8
		100		100
N		780		735

PEW RESEARCH CENTER Oct. 2003.

More Overall Dissatisfaction When Asked After Bush Approval

Asked first	Overall satisfaction	%	Bush approval	%
	Satisfied	17	Approve	25
	Dissatisfied	78	Disapprove	67
	Don't know	5	Don't know	8
		100		100
Asked second	Bush approval		Overall satisfaction	
	Approve	24	Satisfied	9
	Disapprove	68	Dissatisfied	88
	Don't know	8	Don't know	3
		100		100
N		766		723
PEW RESEARCH CE	NTER Dec. 2008.			

More Endorse Working Together When Asked Second

Asked first	Should Rep. leaders	%	Should Dem. leaders	%
	Work with Obama	66	Work with Rep. leaders	82
	Stand up to Obama	28	Stand up to Rep. leaders	13
	Don't know	6	Don't know	5
		100	and a local family of	100
Asked second	Should Dem. leaders		Should Rep. leaders	
and the second p	Work with Rep. leaders	71	Work with Obama	81
	Stand up to Rep. leaders	21	Stand up to Obama	15
	Don't know	8	Don't know	4
		100		100
N		744		756

PEW RESEARCH CENTER Nov. 2008 Post-election survey.

The Good, The Bad, & The Ugly

- How likely would you be to enroll in CookieDirect?
- How organized and interesting was the speaker?
- How helpful do you think our customer service representatives are?
- Should the government force you to pay higher taxes?
- How would you rate the career of legendary writer Dovlatov?

The Good, The Bad, & The Ugly

- What do you like to do for fun?
- How dumb is President Trump at making America great again?
- Should teachers named Joshua offer pizza parties to obedient students?
- In your opinion, how would you rate the quality of your work?
- How do you feel about the following statement? We should reduce military spending.

Create your own survey

- Select a dependent variable and at least two independent variables to test. Examples:
 - Playing Online Multiplayer games vs Multicultural Awareness & Open-mindedness
 - Amount of time spent on social media vs level of English & extroverted/introverted
 - Reading habits vs social media habits & cultural activities