

$$\begin{cases} 5x + 3y + 2z = -4 \\ x - 10y + 5z = 2 \\ -9x - y - 8z = 0 \end{cases}$$

 $b_1 \neq 0 \& b_2 \neq 0 \Rightarrow \text{nonhomogeneous system}$ Δ=-716≠0=> nondegenerate matrix & consistent system (has solution) & definite system (has the

$$\begin{cases} 5x + 3y + 2z = -1 & b_1 \neq 0 \& b_2 \neq 0 \Rightarrow \text{nonhomogeneous system } \Delta = -716 \neq 0 \Rightarrow \text{nondegenerate matrix } 8 \\ x - 10y + 5z = 2 & \text{system (has solution) } \& \text{ definite system (has solution)} \\ -9x - y - 8z = 0 & 5 & 3 & 2 & -1 \\ \widetilde{A} = \begin{pmatrix} 5 & 3 & 2 & -1 \\ 1 & -10 & 5 & 2 \\ -9 & -1 & -8 & 0 \end{pmatrix} \end{cases}$$

$$\approx \begin{pmatrix} 1 & -10 & 5 & 2 \\ 5 & 3 & 2 & -1 \\ -9 & -1 & -8 & 0 \end{pmatrix}$$

$$\begin{array}{c} I \leftrightarrow II \\ \approx & \begin{array}{c} 1 & -10 & 5 & 2 \\ 5 & 3 & 2 & -1 \\ -9 & -1 & -8 & 0 \end{array} \end{array} \right) \xrightarrow{I:5-II \to II} \left(\begin{array}{c} 1 & -10 & 5 & 2 \\ 0 & -53 & 23 & 11 \\ 0 & 91 & -37 & -18 \end{array} \right) \\ II.91-III.(-53) \to III \\ \approx & \begin{array}{c} 1 & -10 & 5 & 2 \\ 0 & -53 & 23 & 11 \\ 0 & 0 & 132 & 47 \end{array} \right) \xrightarrow{I32} \begin{array}{c} 132z = 47 \\ -53y + 23z = 11 \\ y = \frac{47}{132} \\ -53 \\ x = 2 - 5 \cdot \frac{47}{132} + 10 \cdot \left(-\frac{7}{132} \right) \end{array} \\ x = -\frac{41}{132} \\ x = -\frac{41}{132} \\ y = \frac{11 - 23 \cdot \frac{47}{132}}{-53} \xrightarrow{\text{nonhomogeneous solution } 0 \times \frac{47}{132} \times \frac{$$

$$\begin{cases} 9a - 2b + 7c + d = 8 \\ -7a - 9b + 7c + 4d = 3 & \text{nonhomogeneous} \\ -9a + 4b + 9c + 5d = 1 & \Delta = 0 = > \\ -15a - 2c + 2d = -6 \end{cases}$$

$$\begin{vmatrix} 9 & -2 & 7 & 1 & 8 \\ -7 & -9 & 7 & 4 & 3 \\ -9 & 4 & 9 & 5 & 1 \\ -15 & 0 & -2 & 2 & -6 \end{vmatrix}$$

$$\begin{vmatrix} 9 & -2 & 7 & 1 & 8 \\ 0 & 95 & -112 & -43 & -83 \\ 1 & 1.15 + IV.9 & 0 & 2 & 16 & 6 & 9 \\ 0 & 2 & 16 & 6 & 9 & 1.30 + IV.95 \\ 0 & 20 & 87 & 32 & 66 & 0 & 4905 & 1845 & 3780 \\ 0 & 0 & 4905 & 1845 & 3780 \\ 0 & 3780 & 3780 & 1845 & 3780 \\ 0 & 1845 & 3780 & 1845 & 3780 \\ 0 & 1845 & 3780 & 1845 & 3780 \\ 0 & 1845 & 3780 & 1845 & 3780 \\ 0 & 1845 & 3780 & 1845 & 3780 \\ 0 & 1845 & 3780 & 1845 & 3780 \\ 0 & 1845 & 3780 & 1845 & 3780 \\ 0 & 1845 & 3780 & 1845 & 3780 \\ 0 & 1845 & 3780 & 1845 & 3780 \\ 0 & 1845 & 3780 & 1845 & 3780 \\ 0 & 1845 & 3780 & 1845 & 3780 \\ 0 & 1845 & 3780 & 1845 & 3780 \\ 0 & 1845 & 3780 & 1845 & 3780 \\ 0 & 1845 & 3780 & 1845 & 3780 \\ 0 & 1845 & 3780 & 1845 & 3780 \\ 0 & 1845 & 3780 & 1845 & 3780 \\ 0 & 1845 & 3780 & 1845 & 3780 \\ 0 & 1845 & 3780 & 1845 & 3780 \\ 0 & 1845 & 3780 & 1845 & 3780 \\ 0 & 1845 & 1845 & 1845 \\ 0 & 1845 & 1845 & 1845 \\ 0 & 1845 & 1845 & 1845 \\ 0 & 1845 & 1845 & 1845 \\ 0 & 1845 & 1845 & 1845 \\ 0 & 1845 & 1845 & 1845 \\ 0 & 1845 & 1845 & 1845 \\ 0 & 1845 & 1845 & 1845 \\ 0 & 1845 & 1845 & 1845 \\ 0 & 1845 & 1845 & 1845 \\ 0 & 1845 & 1845 & 1845 \\ 0 & 1845 & 1845 & 1845 \\ 0 & 1845 & 1845 & 1845 \\ 0 & 1845 & 1845 & 1845 \\ 0 & 1845 & 1845 & 1845 \\ 0 & 1845$$

$$0 \cdot d = 1584315$$

inconsistent system (has no solution)

$$\begin{cases}
-4x_1 + 9x_2 + 9x_3 + 5x_4 = -6 \\
-9x_1 + 9x_2 - 2x_3 - 9x_4 = 0
\end{cases}$$

$$\begin{cases}
-3x_1 - 9x_2 - 6x_3 = 3 \\
-27x_1 - 3x_2 - 4x_3 + x_4 = -2
\end{cases}$$

 $b_1 \neq 0 \& b_2 \neq 0 =>$ nonhomogeneous system ∆=0=>

matrix

$$_{4} = -2$$

$$0 \cdot x_4 = 0$$

$$\begin{cases} a+8b-3c=6 & | 1 & 8 & -3 & 0 & | 6 \\ 7a+b-c-d=8 & | 7 & 1 & -1 & -1 & | 8 \\ & | 1 & 8 & -3 & 0 & | 6 \\ 3 & 1 & 1 & 1 & 1 & 3 \\ 7 & 1 & -1 & -1 & | 8 \\ & | 1 & 8 & -3 & 0 & | 6 \\ 0 & 23 & -10 & -1 & | 15 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0 & 0 & -90 & -78 & | 43 \\ 0$$

 $\begin{pmatrix} 3 & 1 & 1 & 1 & 3 \\ 1 & 8 & -3 & 0 & 6 \end{pmatrix}$

3a + b + c + d = 3