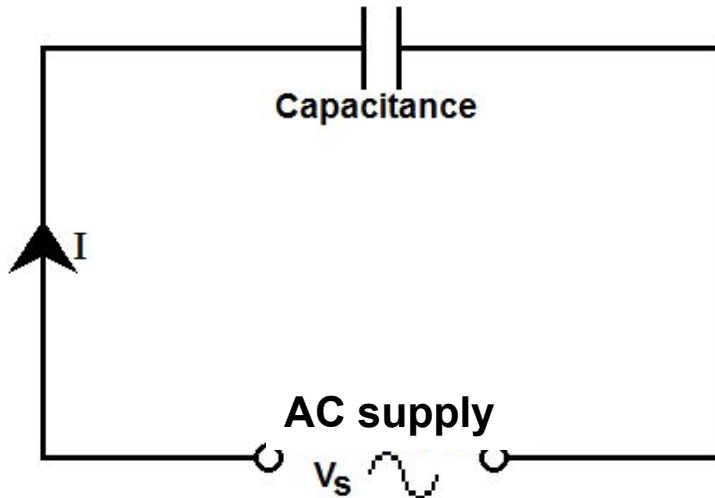


Unit 302: Principles of electrical science

Capacitance in an AC circuit



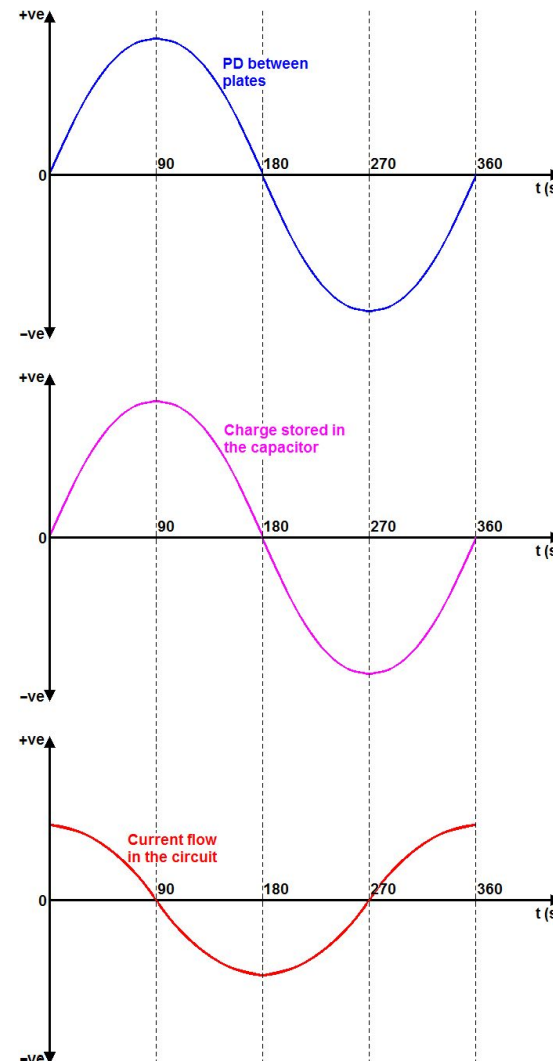
$$Q = V.C$$

Where:

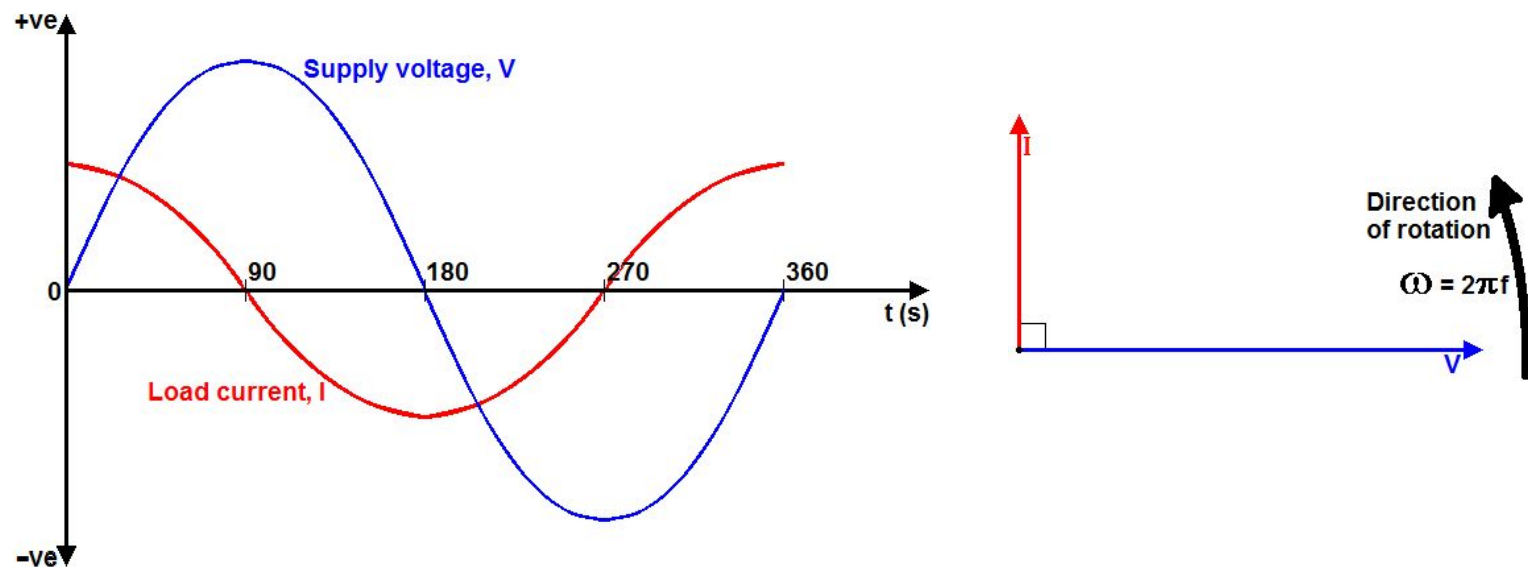
Q = Charge in coulombs

V = Voltage in volts

C = Capacitance in farads



In a purely capacitive circuit, the current must flow before the pd can be established across the capacitor and therefore the current leads the voltage by 90°



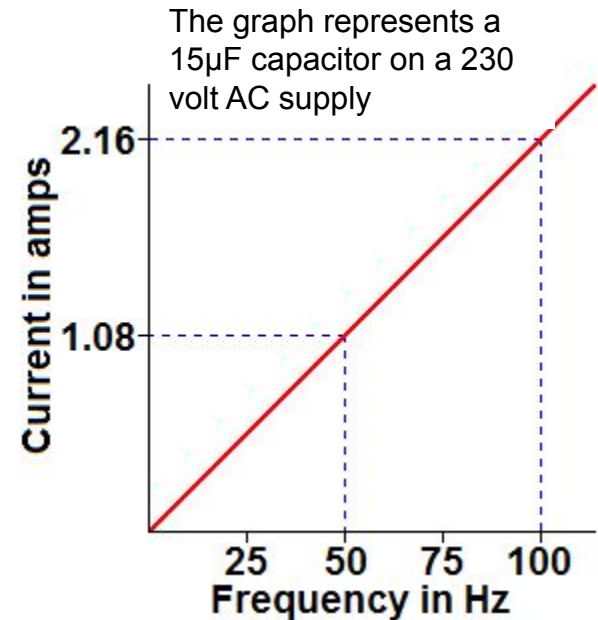
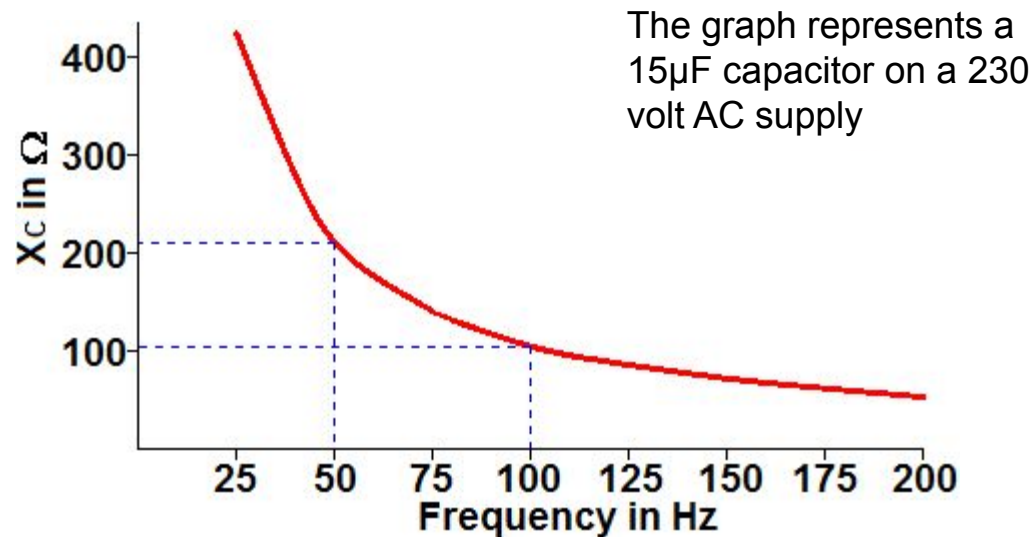
In a purely capacitive circuit, the current must flow before the pd can be established across the capacitor and therefore the current leads the voltage by 90°

$$X_c = \frac{V}{I}$$

$$X_c = \frac{1}{2\pi fC}$$

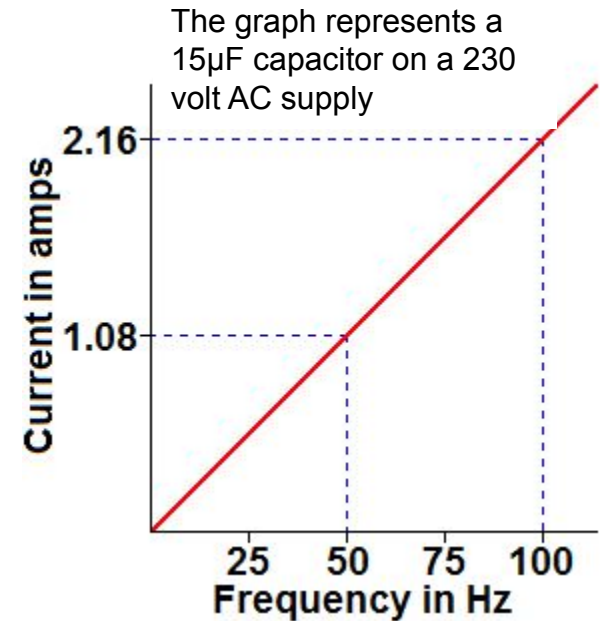
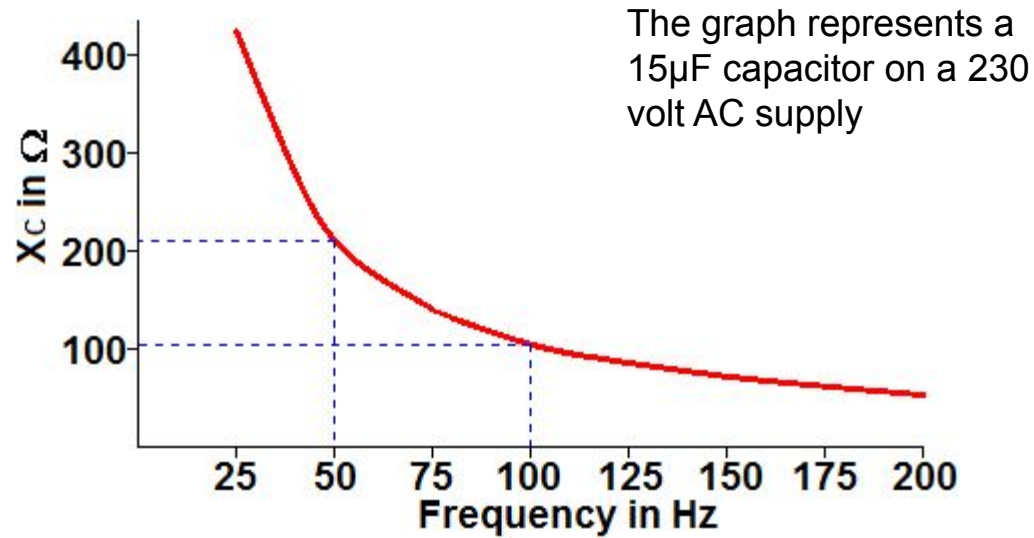
$$X_c = \frac{1}{\omega C}$$

Where: X_c = Reactance of the capacitor in ohms
 V = Voltage across the capacitor
 I = Resulting current flow
 f = Supply frequency in Hz
 C = Capacitance in Farads
 ω = $2\pi f$



The current flowing through a capacitor is proportional to:

- size of the capacitor in microfarads (μ F)
- the voltage applied to the capacitor (V_C)
- the frequency (f).



$$W = \frac{1}{2} CV^2 \text{ (joules)}$$

EXAMPLE – Calculate the capacitive reactance and current that will flow to a $2\mu\text{F}$ capacitor, when connected to a 230 volt supply at:

- a) 50Hz.
- b) 200Hz.

a)

$$X_C = \frac{1}{2\pi fC}$$

$$X_C = \frac{1}{2 \times 3.14 \times 50 \times 2 \times 10^{-6}}$$

$$X_C = 1592.4\Omega$$

$$I = \frac{V}{X_C}$$

$$I = \frac{230}{1592.4}$$

$$I = 0.14\text{A}$$

EXAMPLE – Calculate the capacitive reactance and current that will flow to a $2\mu\text{F}$ capacitor, when connected to a 230 volt supply at:

- a) 50Hz.
- b) 200Hz.

$$X_C = \frac{1}{2\pi fC}$$

b)

$$X_C = \frac{1}{2 \times 3.14 \times 200 \times 2 \times 10^{-6}}$$

$$X_C = 398.1\Omega$$

$$I = \frac{V}{X_C}$$

$$I = \frac{230}{398.1}$$

$$I = 0.58\text{A}$$

EXAMPLE – Calculate the capacitive reactance and current that will flow to an $8\mu\text{F}$ capacitor, when connected to a 230 volt supply at:

- a) 50Hz.
- b) 200Hz.

a)

$$X_C = \frac{1}{2\pi fC}$$

$$X_C = \frac{1}{2 \times 3.14 \times 50 \times 8 \times 10^{-6}}$$

$$X_C = 398.1\Omega$$

$$I = \frac{V}{X_C}$$

$$I = \frac{230}{398.1}$$

$$I = 0.58\text{A}$$

EXAMPLE – Calculate the capacitive reactance and current that will flow to an $8\mu\text{F}$ capacitor, when connected to a 230-volt supply at:

- a) 50Hz.
- b) 200Hz.

b)

$$X_C = \frac{1}{2\pi fC}$$

$$X_C = \frac{1}{2 \times 3.14 \times 200 \times 8 \times 10^{-6}}$$

$$X_C = 99.5\Omega$$

$$I = \frac{V}{X_C}$$

$$I = \frac{230}{99.5}$$

$$I = 2.3\text{A}$$

EXAMPLE – Calculate the capacitive reactance and current that will flow to a $16\mu\text{F}$ capacitor, when connected to a 230-volt supply at:

- a) 50Hz.
- b) 200Hz.

a)

$$X_C = \frac{1}{2\pi fC}$$

$$X_C = \frac{1}{2 \times 3.14 \times 50 \times 16 \times 10^{-6}}$$

$$X_C = 199\Omega$$

$$I = \frac{V}{X_C}$$

$$I = \frac{230}{199}$$

$$I = 1.16\text{A}$$

EXAMPLE – Calculate the capacitive reactance and current that will flow to a $16\mu\text{F}$ capacitor, when connected to a 230-volt supply at:

- a) 50Hz.
- b) 200Hz.

b)

$$X_C = \frac{1}{2\pi fC}$$

$$X_C = \frac{1}{2 \times 3.14 \times 200 \times 16 \times 10^{-6}}$$

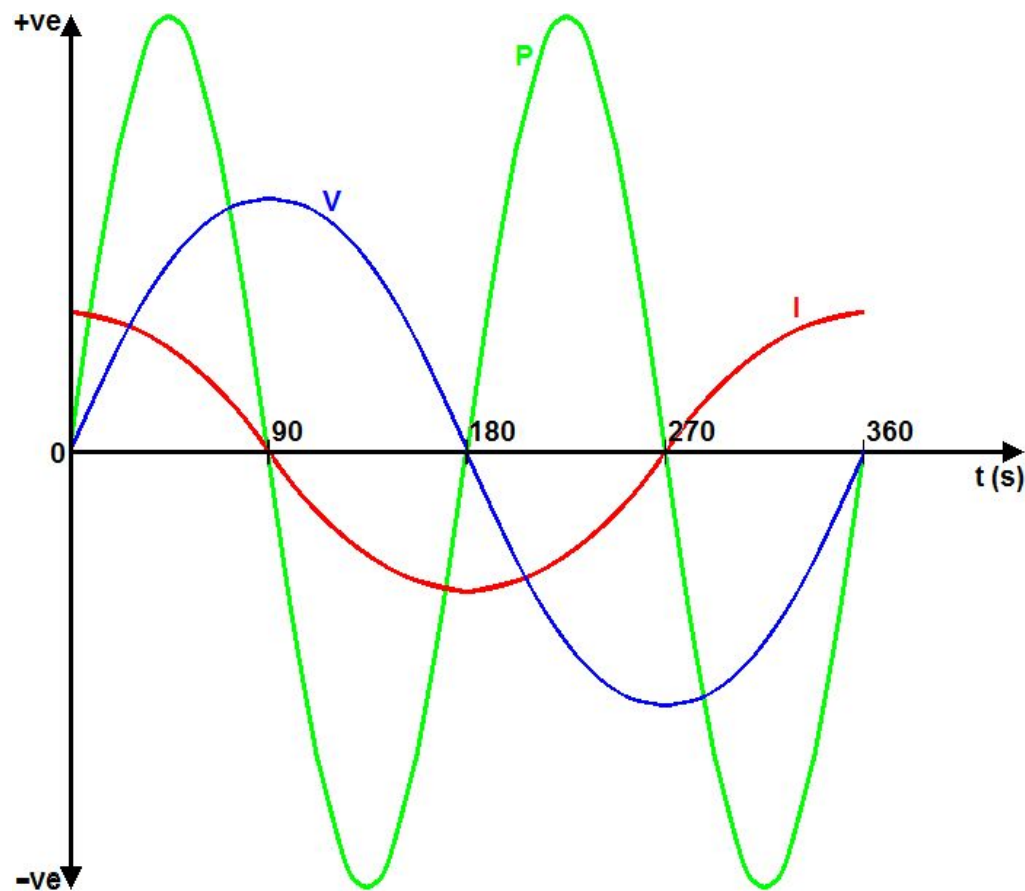
$$X_C = 49.8\Omega$$

$$I = \frac{V}{X_C}$$

$$I = \frac{230}{49.8}$$

$$I = 4.6\text{A}$$

$P = I^2 R$ therefore $p = \text{zero watts}$



Any questions?