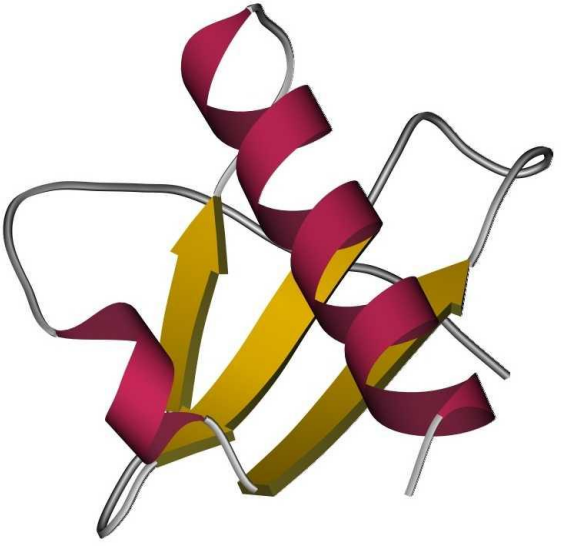


# PROTEIN PHYSICS

## LECTURE 13-16

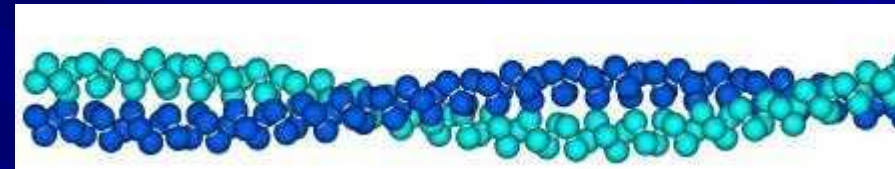
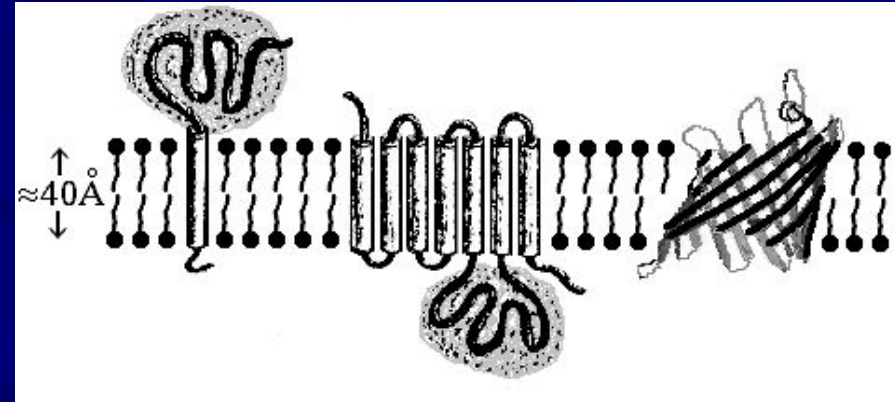
- Structures of water-soluble globular proteins
- Physical selection of protein structures
- Structural classification of proteins

# Globular proteins (water-soluble)


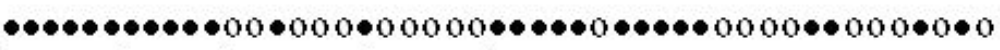
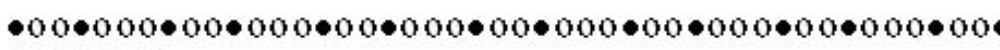


# Membrane

# Fibrous



# H-bonds & hydrophobics

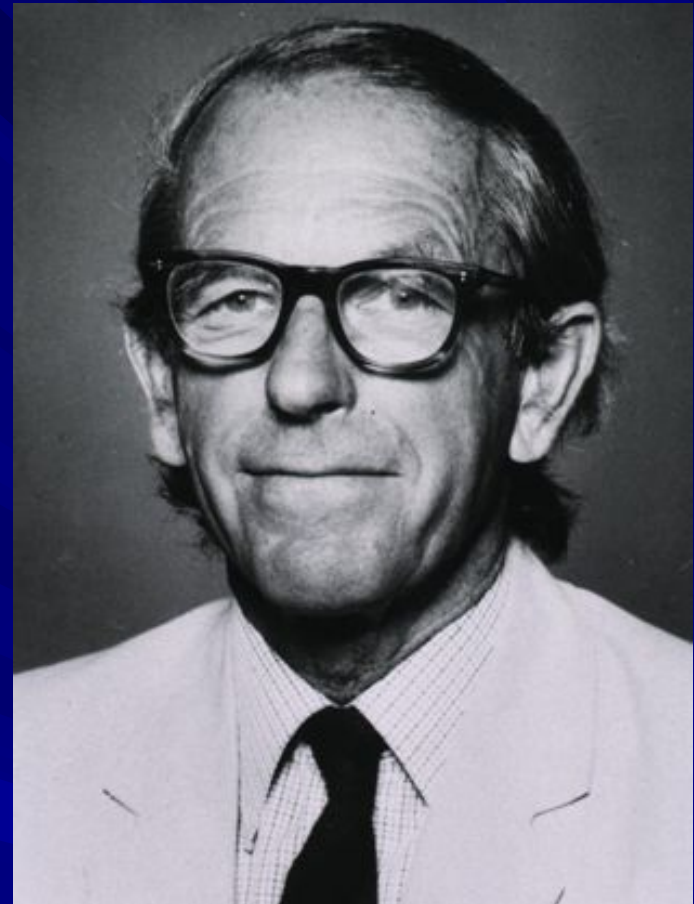
PROTEINS	SEQUENCES	
<u>Globular</u>		<i>quasi-random</i>
<u>Membrane</u>		<i>blocks</i>
<u>Fibrous</u>		<i>repeats</i>

## Protein chain

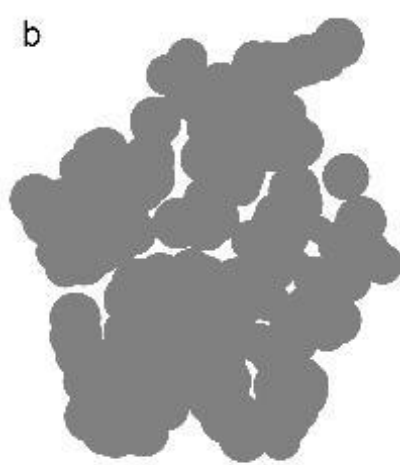
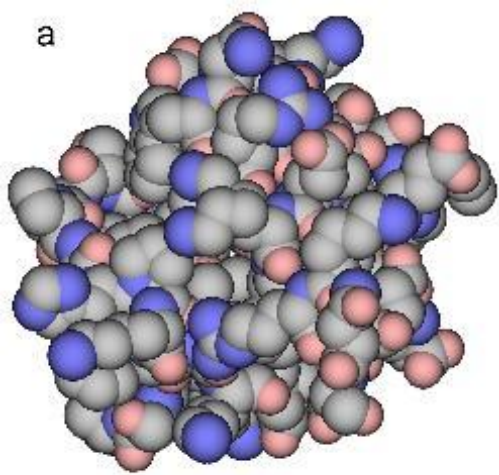


Hermann Emil Louis  
**Fischer**  
(1852 –1919)  
Nobel Prize 1902

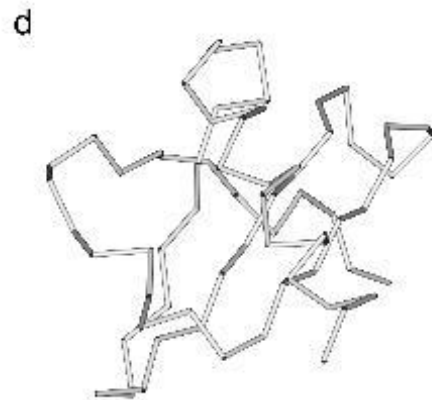
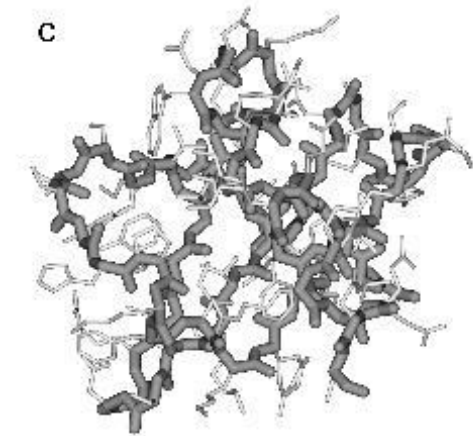
## Protein sequence



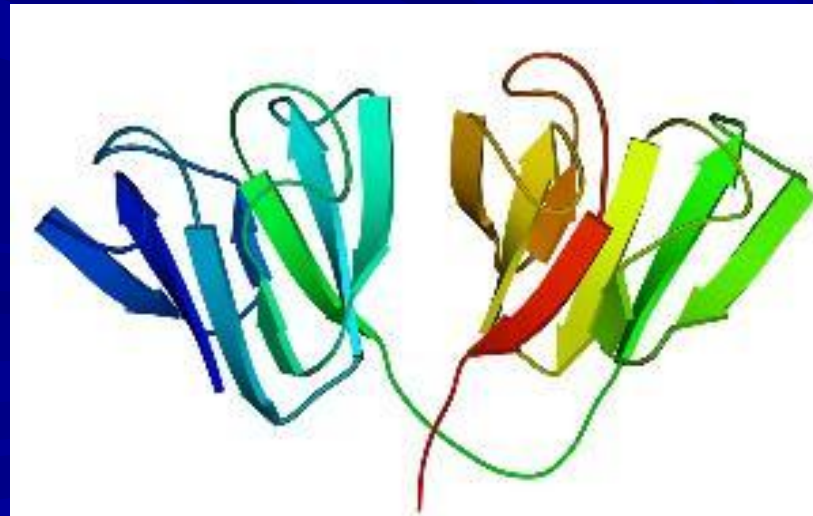
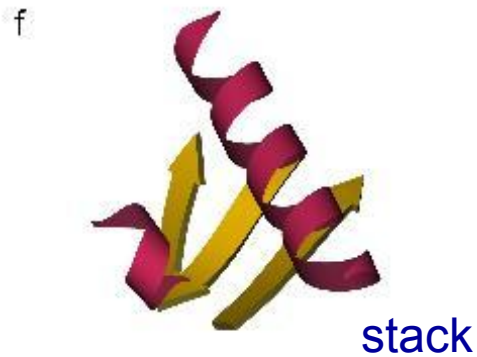
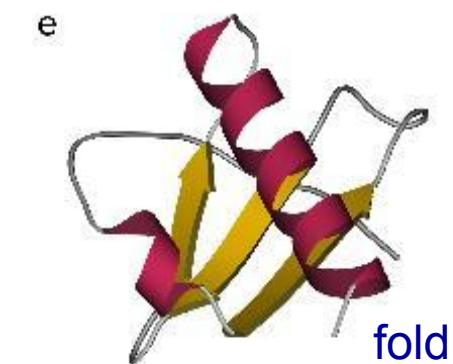
Frederick **Sanger**  
(1918 –2013)  
Nobel Prizes: 1958, 1980



← **single-domain  
globular protein**



**domain 1    domain 2**





## X-RAY

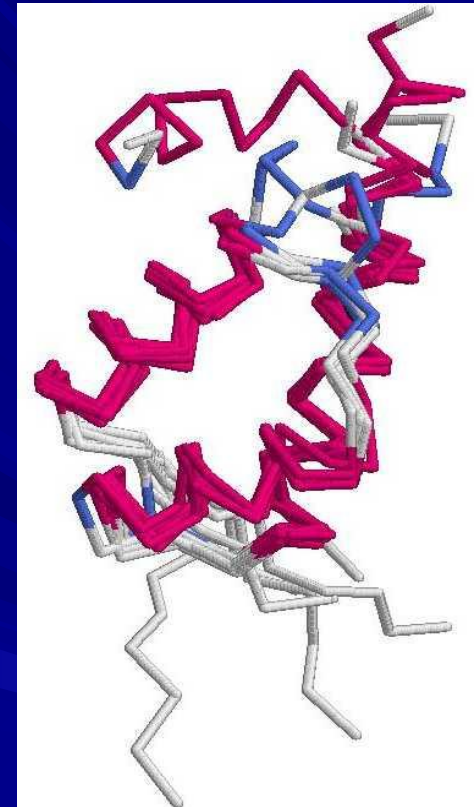
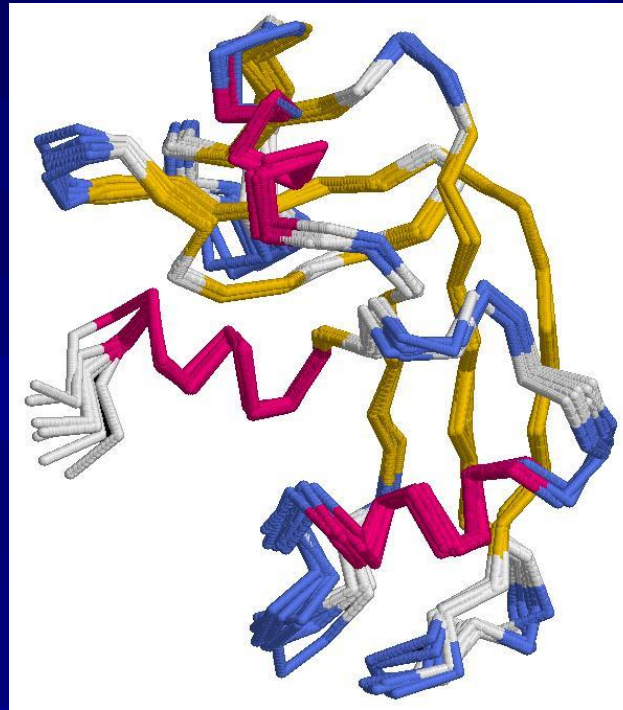
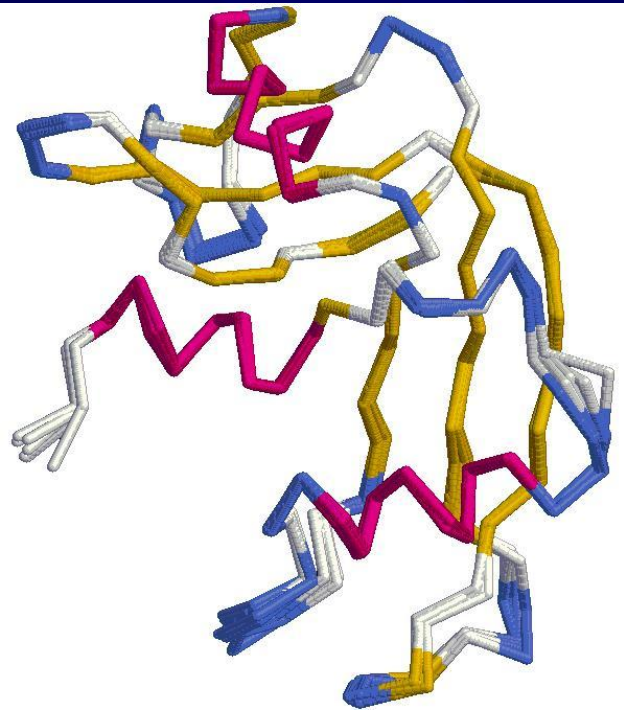
One protein, various crystallizations

## NMR

Structures, compatible with one NMR experiment

## Homologous

(closely related) proteins



Secondary structures ( $\alpha$ -helices,  $\beta$ -strands) are the most rigid and conserved details of proteins; they are determined with the smallest errors and form a basis of protein classification

## X-ray 3D protein structure

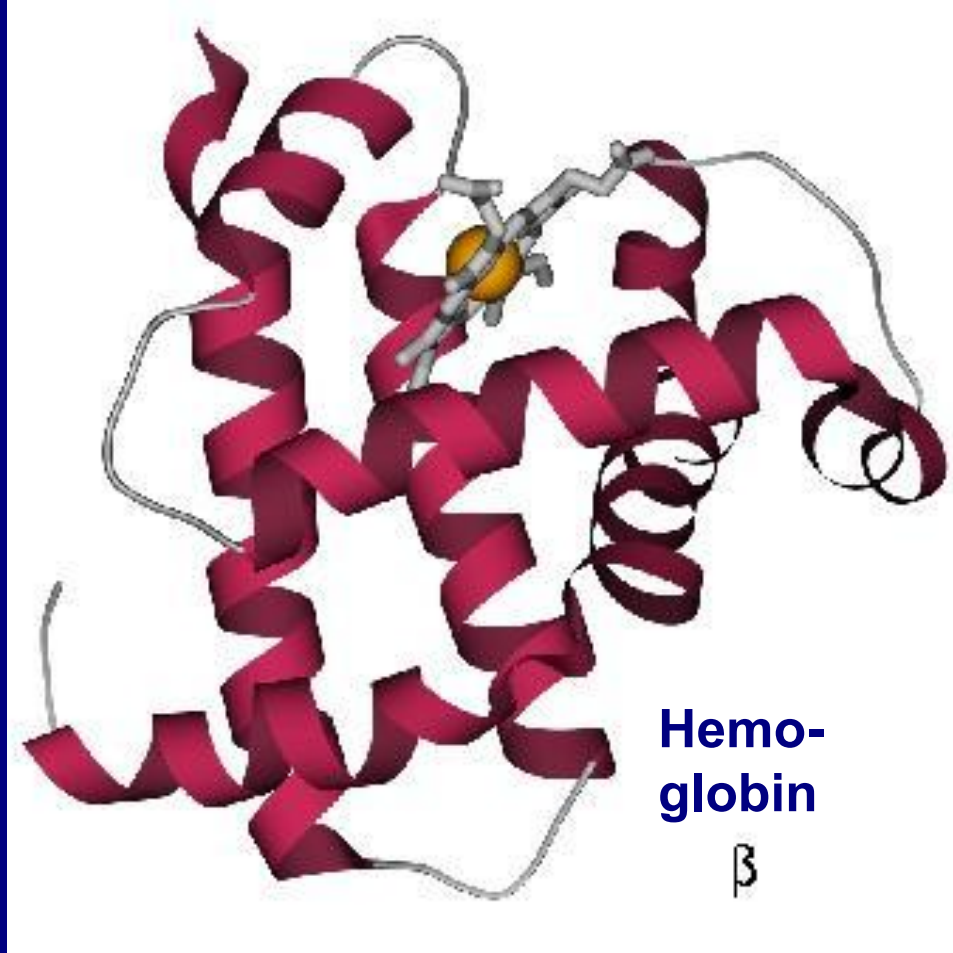
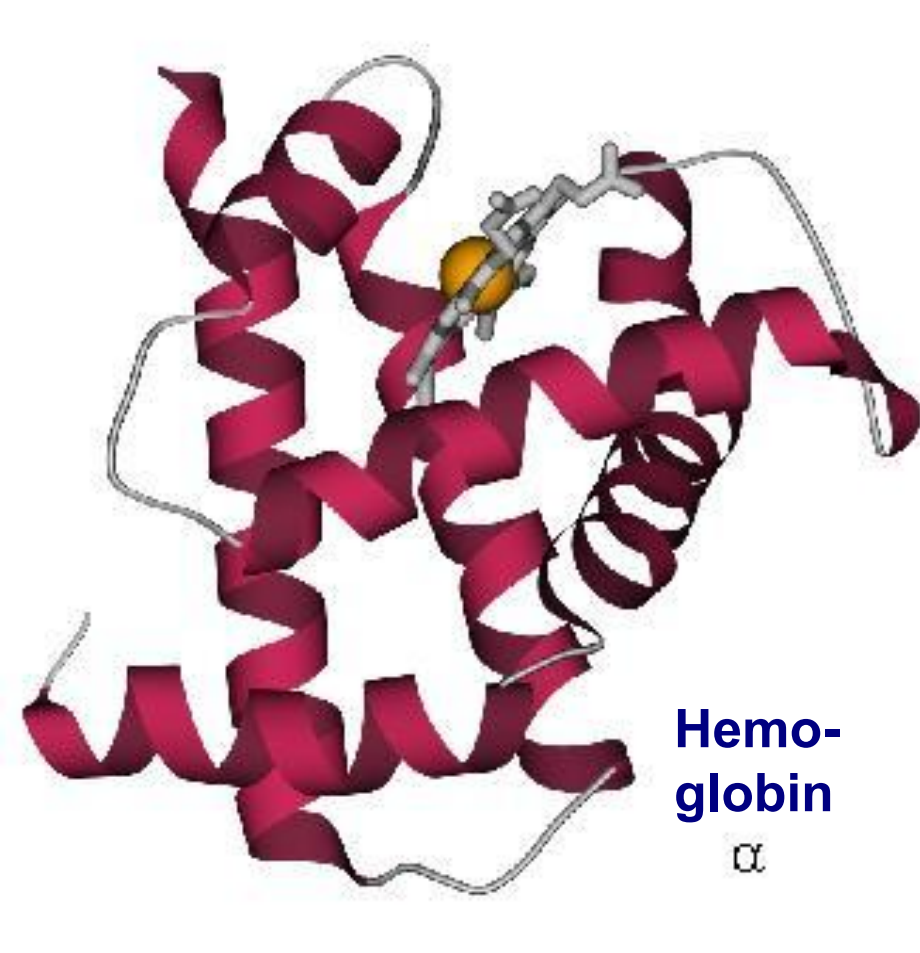


Max Ferdinand **Perutz**  
(1914 –2002)  
Nobel Prize 1962

## NMR 3D protein structure



Kurt **Wüthrich**, 1938  
Nobel Prize 2002



**Homologous proteins have similar folds.**

**True, but trivial.**

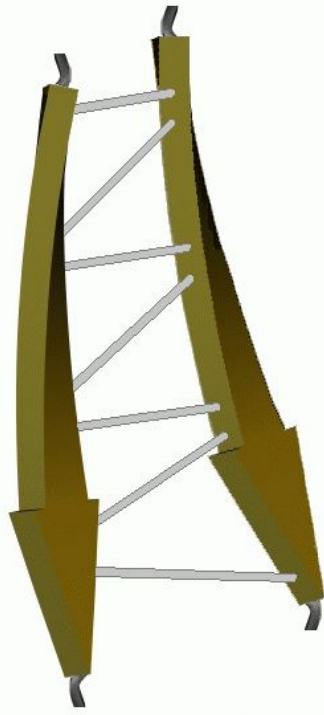
**NON-trivial:**

**Many NON-homologous proteins have similar folds.**

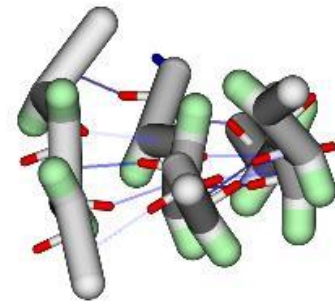
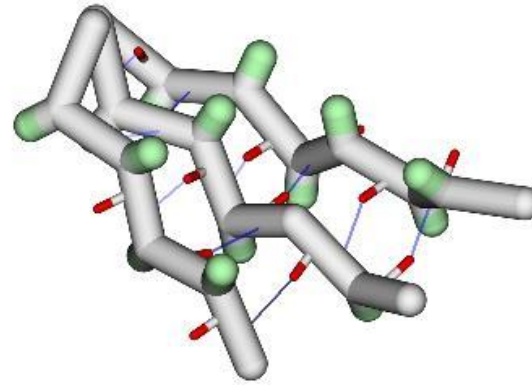




$\beta \uparrow$



$\beta \downarrow$



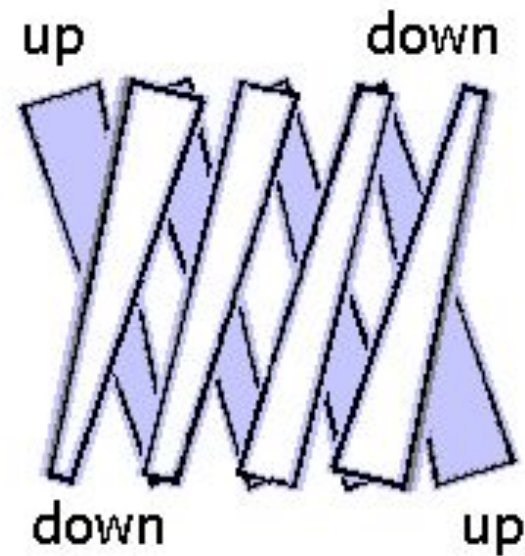
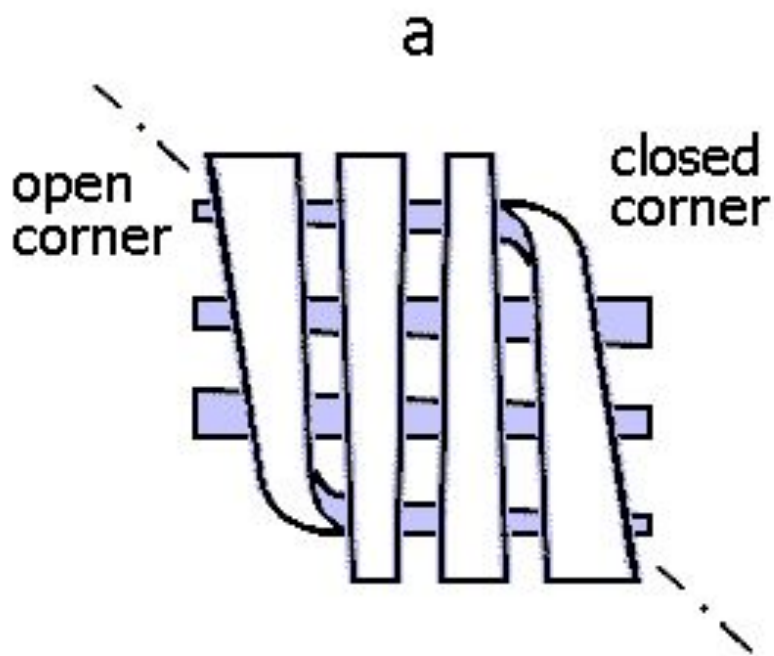
**$\beta$ -sheets: usually, twisted  
(usually, right-)  $\uparrow$**

**$\beta$ -proteins**

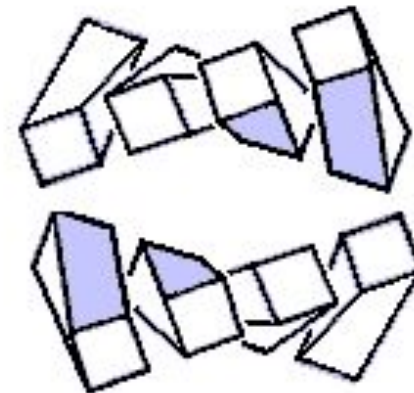
**H-bonds: within sheets**

**Hydrophobics: between sheets**





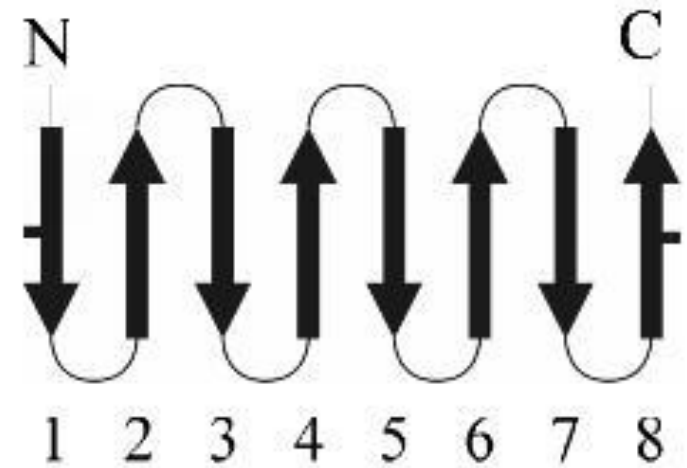
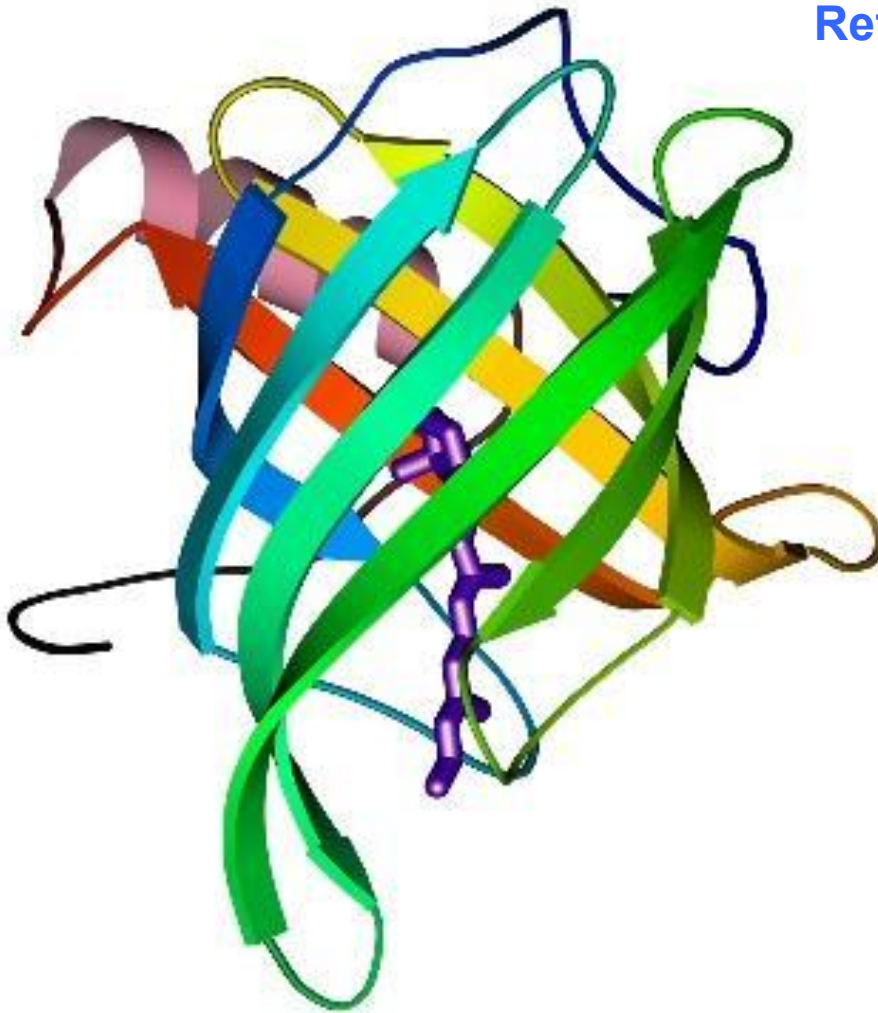
sandwiches  
&  
cylinders



Orthogonal packing  
of  $\beta$ -sheets

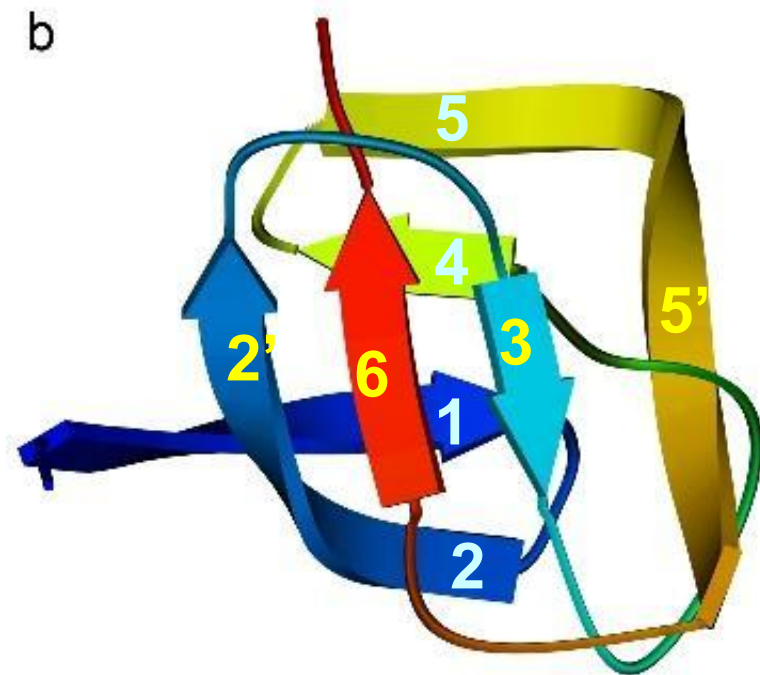
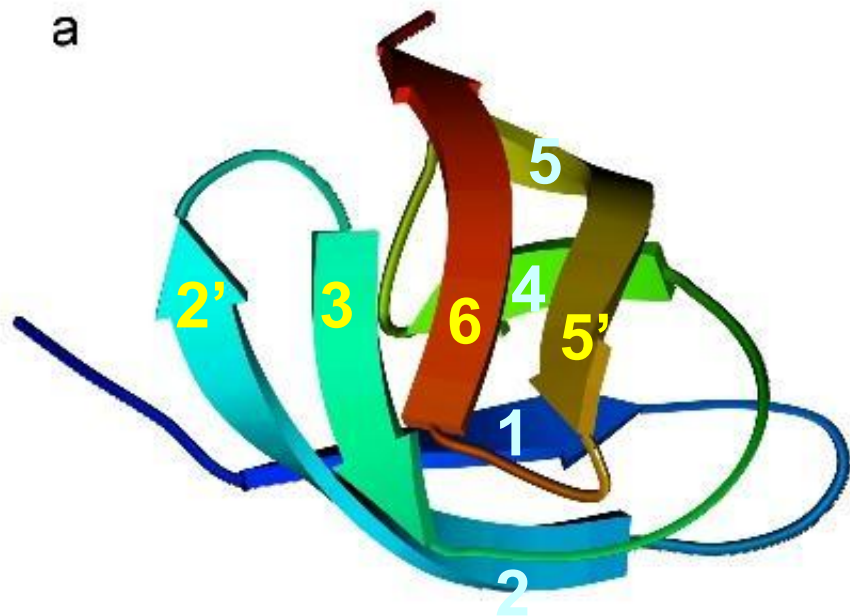
Aligned packing  
of  $\beta$ -sheets

## Retinol-binding protein



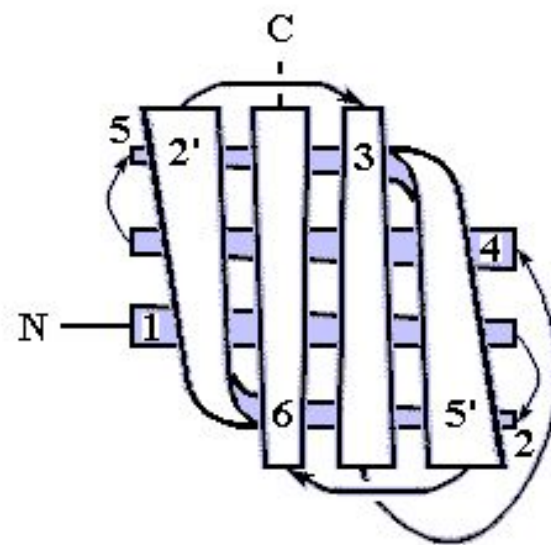
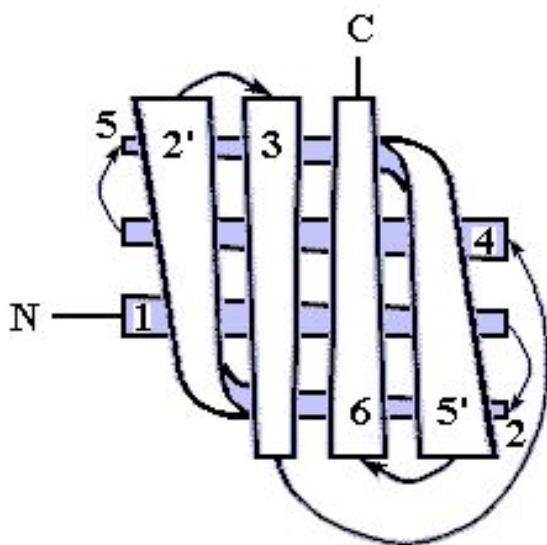
meander

**orthogonal packing  
of one rolled  
 $\beta$ -sheet**



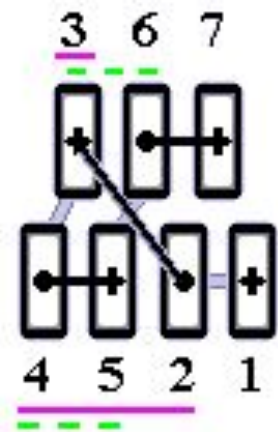
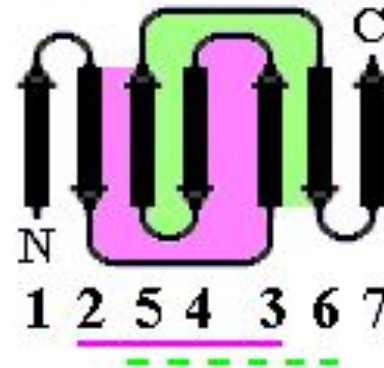
**Trypsin-like SER-protease  
orthogonal packings of  $\beta$ -sheets**

**Acid-protease**





**IG-fold:**



**Greek key 2::5**

**Greek key 3::6**

**non-crossed loops**



**aligned packing of  $\beta$ -sheets**



# $\beta$ -sandwich h

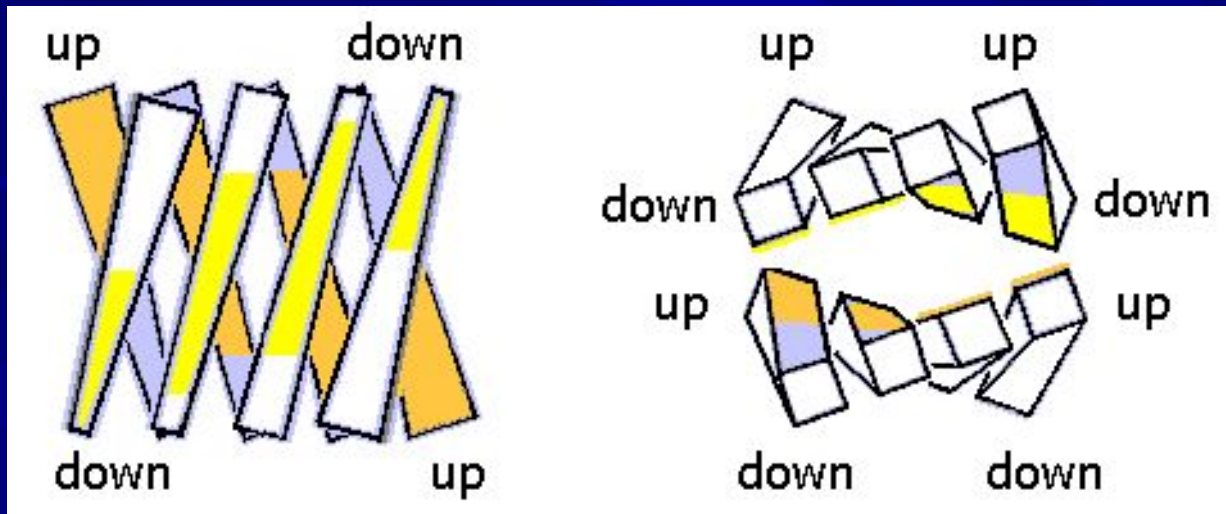
Greek key:  
edge of sandwich

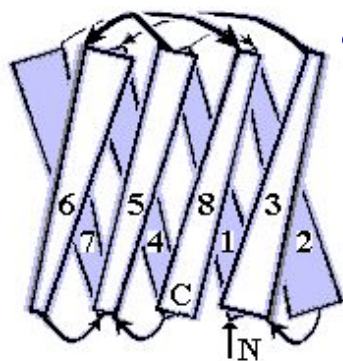
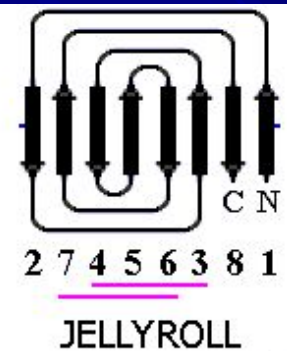
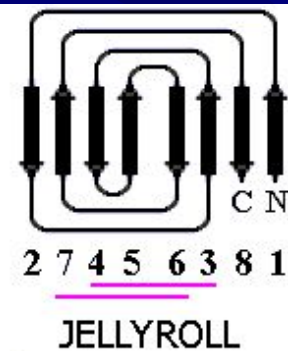
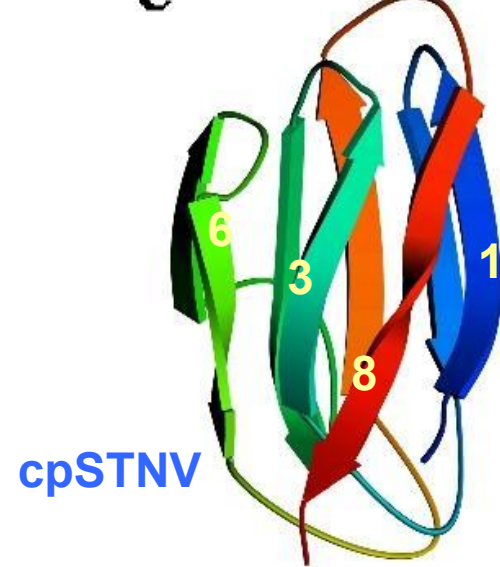
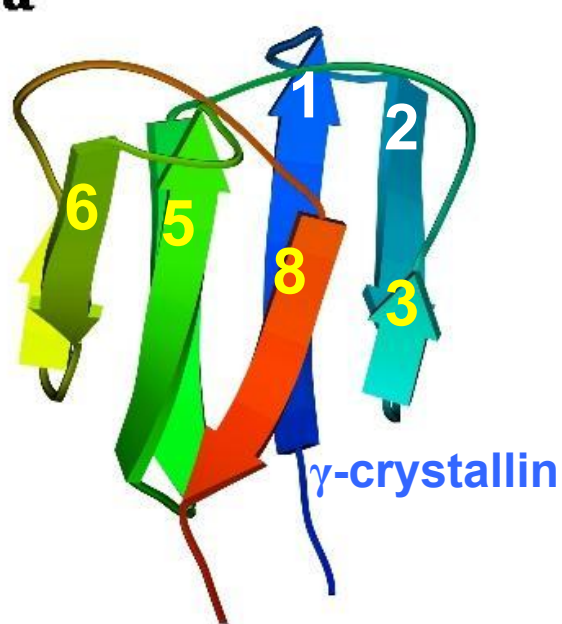


Interlocked pairs:  
center of sandwich



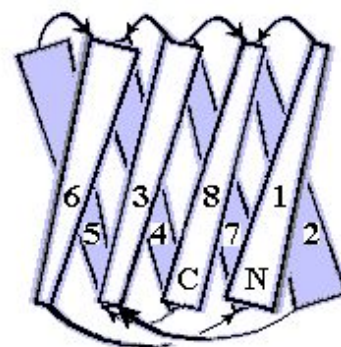
Hydrophobic surfaces  
of sheets of the sandwich



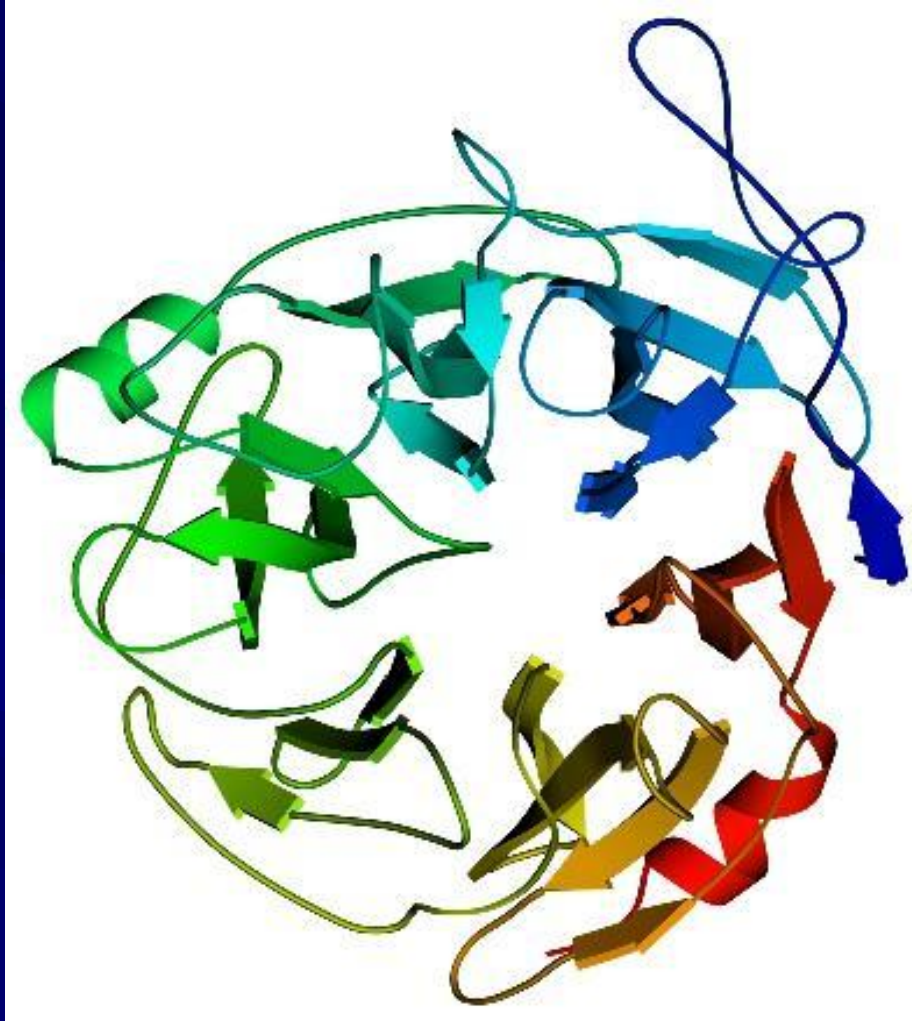


**aligned packings  
of β-sheets**

**a) different:  
only topologies**



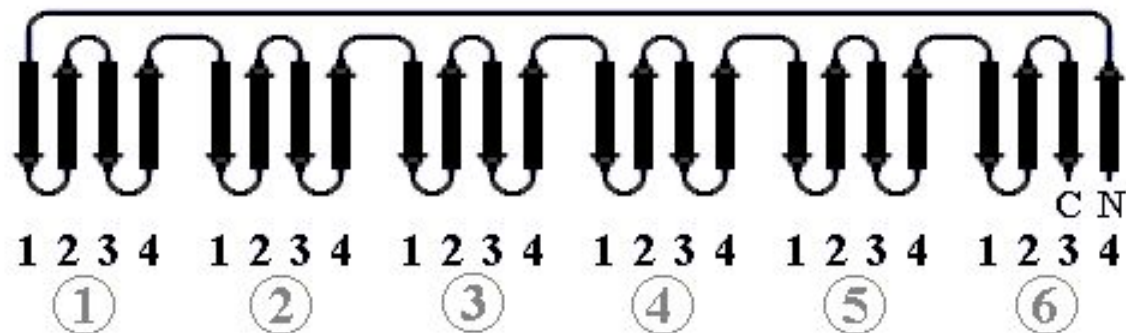
**b) equal:  
even  
topology**



aligned packing  
of  $\beta$ -sheets

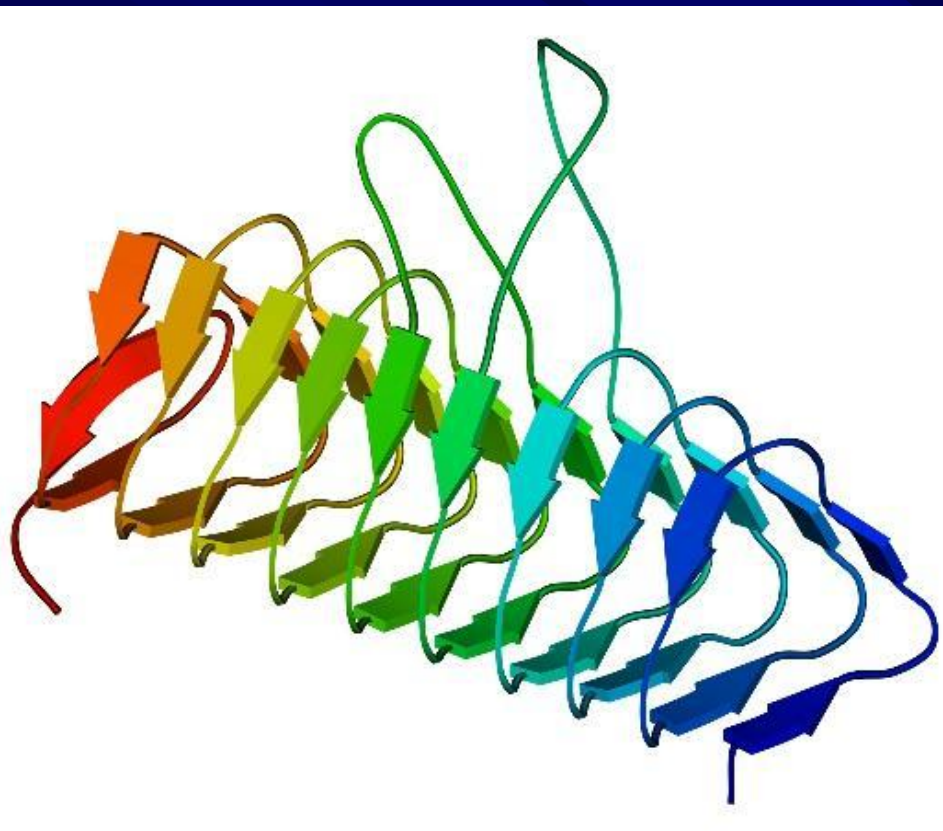
6-bladed propeller

neuraminidase

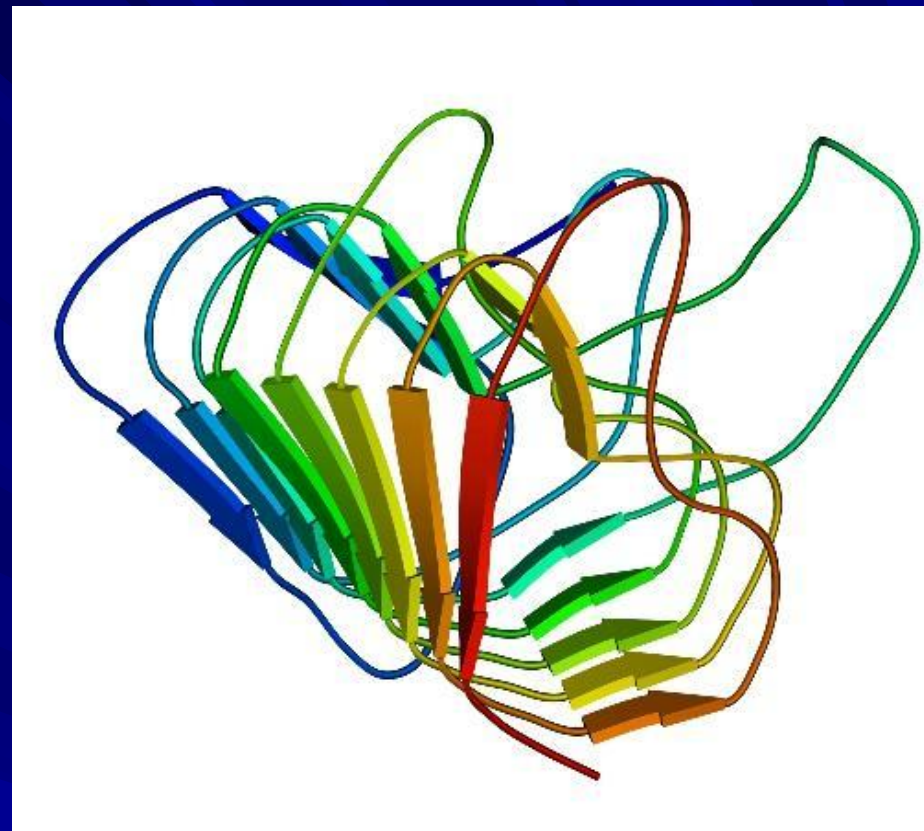




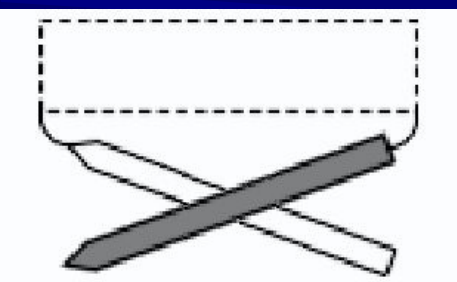
Left-handed  $\beta$ -prism: Acyl transferase



Right-handed  $\beta$ -prism: Pectate lyase

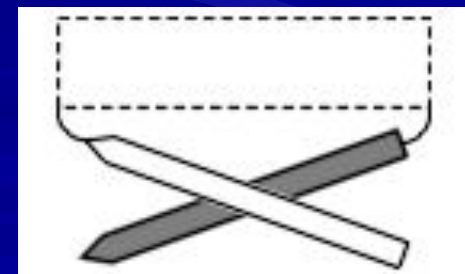


## TOPOLOGY of chain turns between parallel $\beta$ -strands



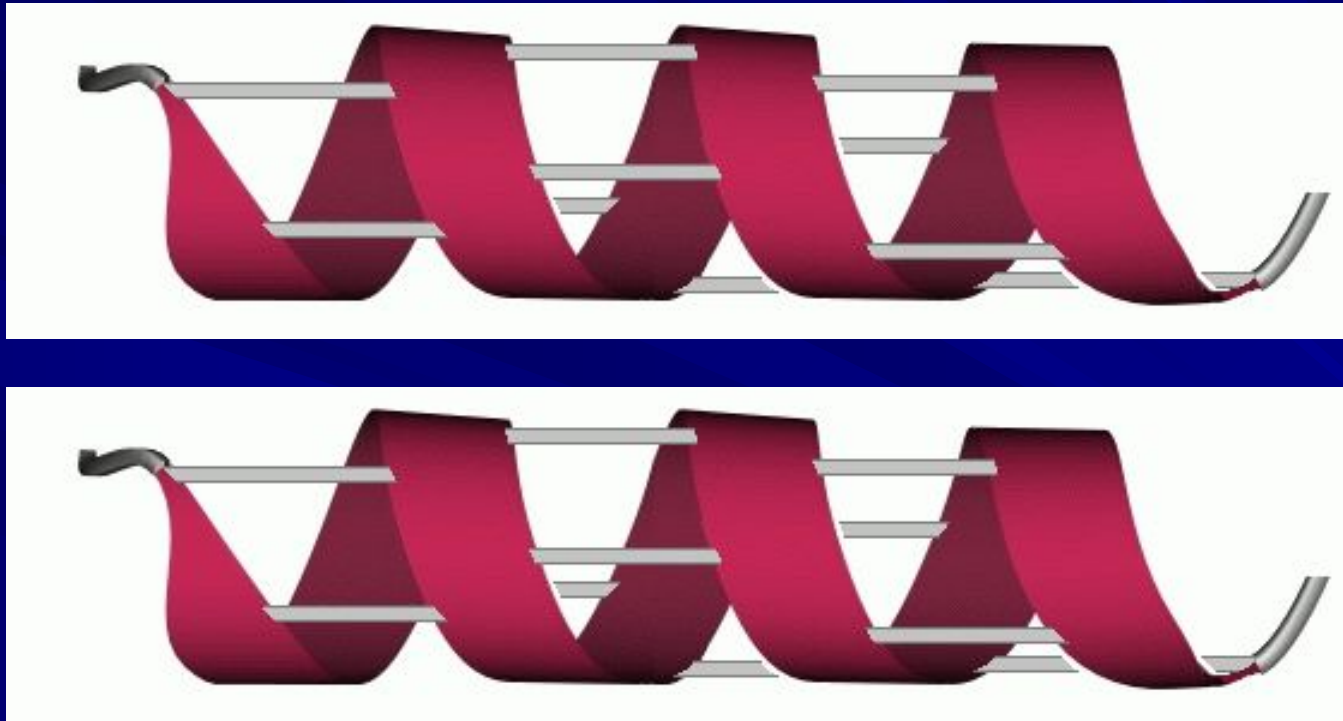
**UNusual**  
**LEFT**-HANDED  
chain turns  
(AND NO  
 $\beta$ -TWIST!)

**Usual**  
RIGHT-HANDED  
chain turns  
(AND RIGHT  
 $\beta$ -TWIST!)

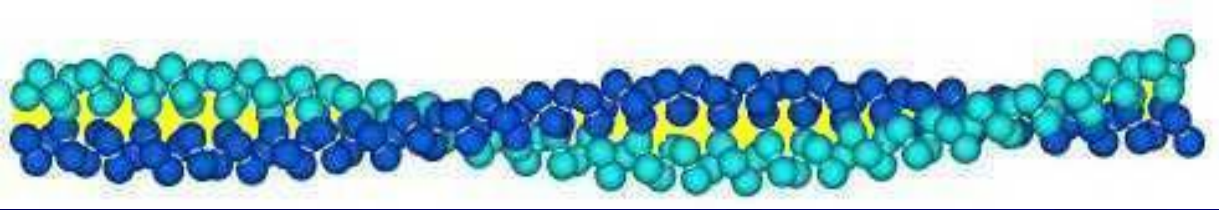




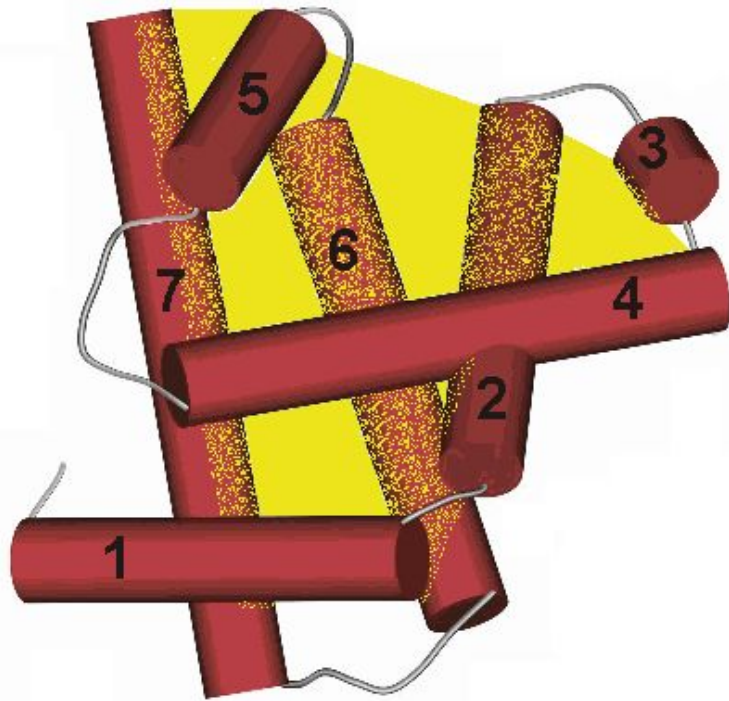
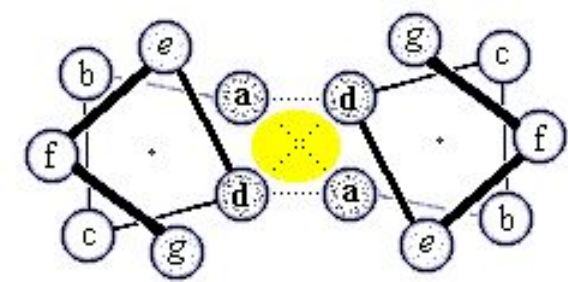
# $\alpha$ -proteins



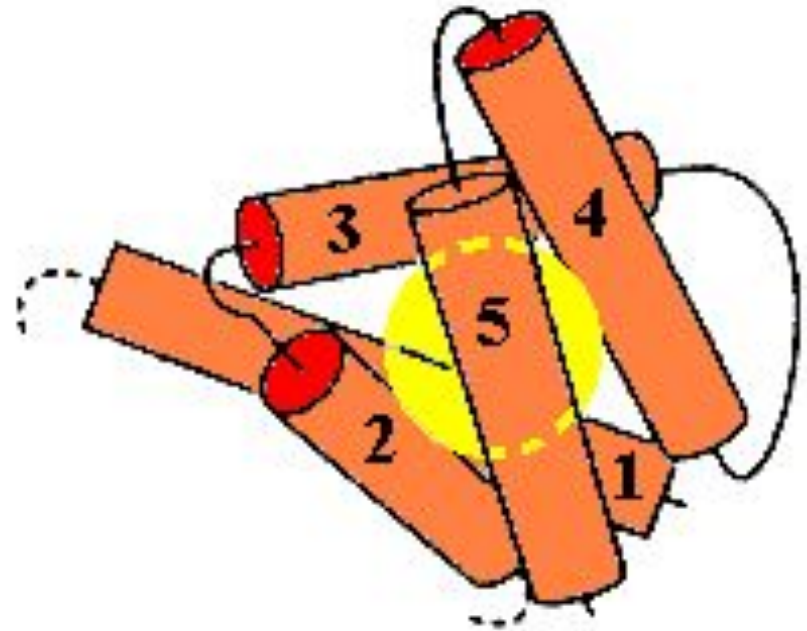
H-bonds: within helices  
&  
Hydrophobics: between helices



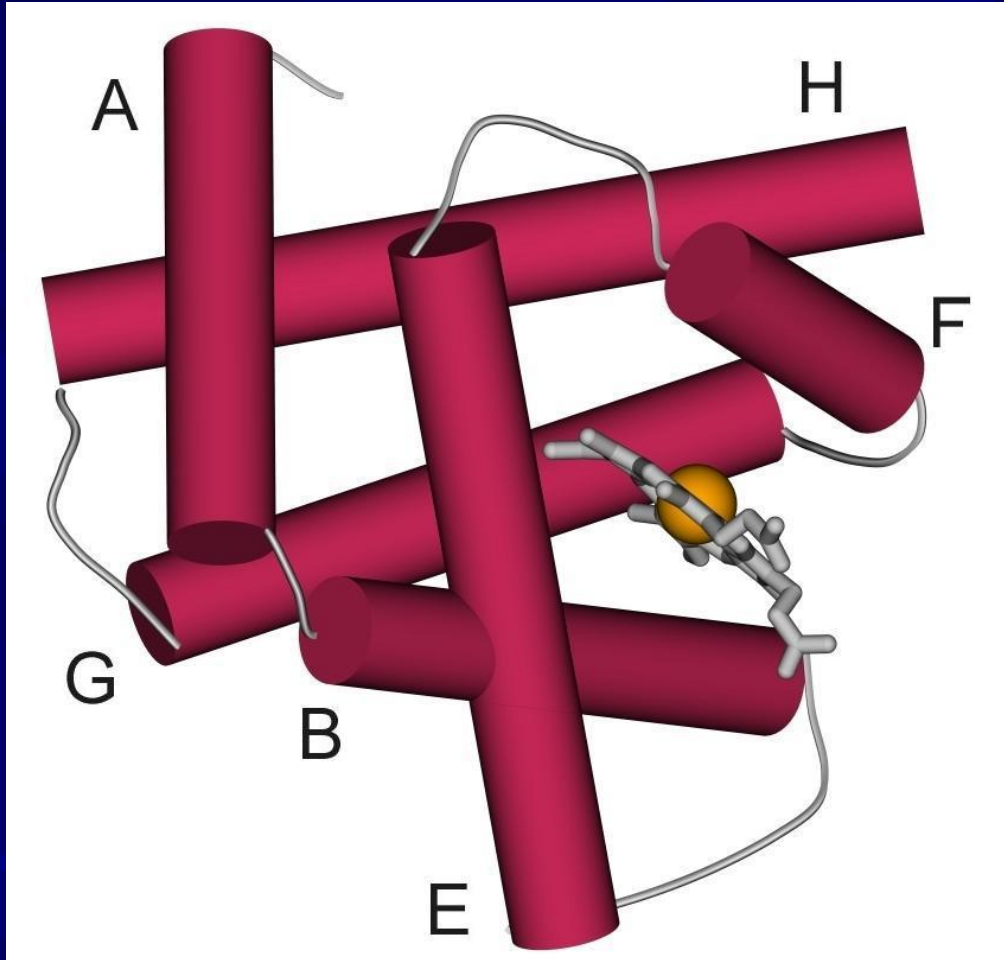
Quasi-cylindrical core (in fibrous)



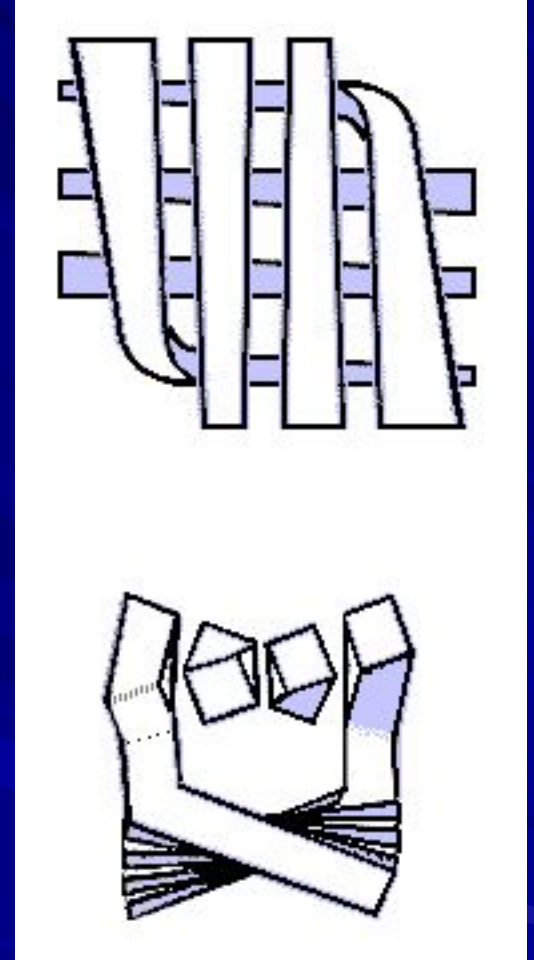
Quasi-flat core



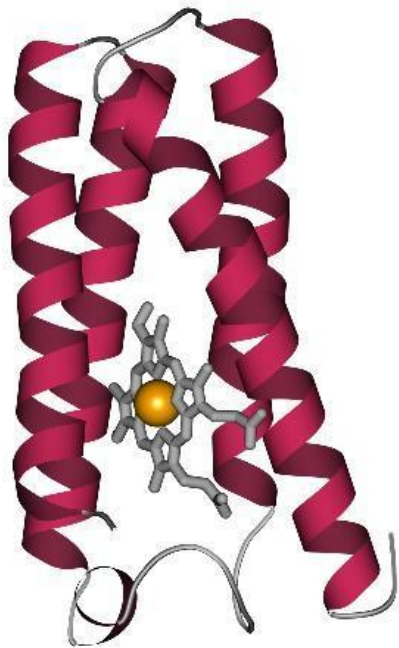
Quasi-spherical core  
**MOST COMMON**



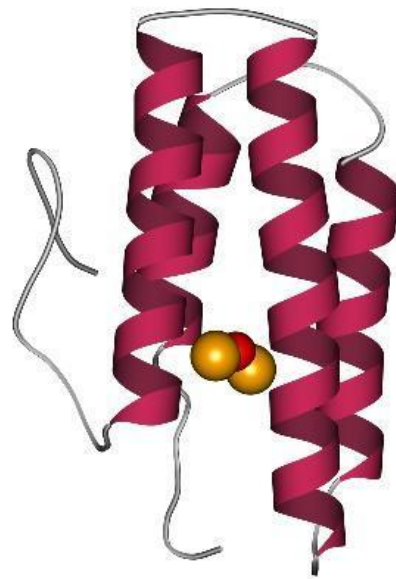
**Orthogonal packing  
of LONG  $\alpha$ -helices**



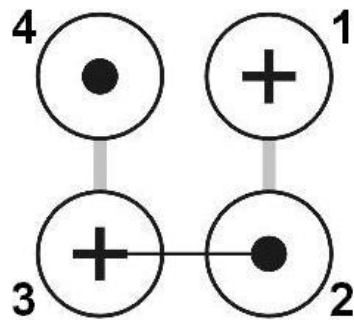
**Similar to orthogonal  
packing of  $\beta$ -sheets**



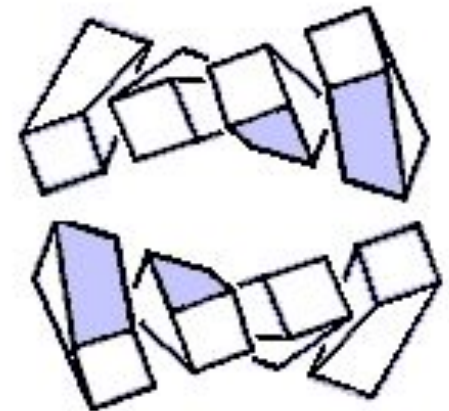
*Cytochrome c'*



*Hemerythrin*

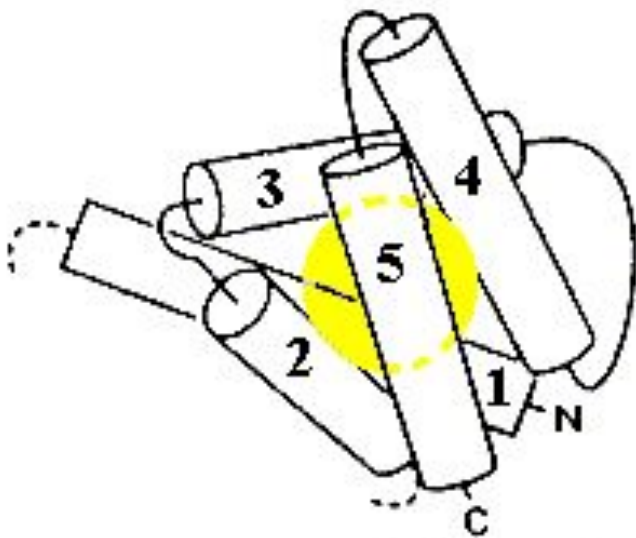


**Aligned packing  
of LONG  $\alpha$ -helices**



**Similar to aligned  
packing of  $\beta$ -sheets**



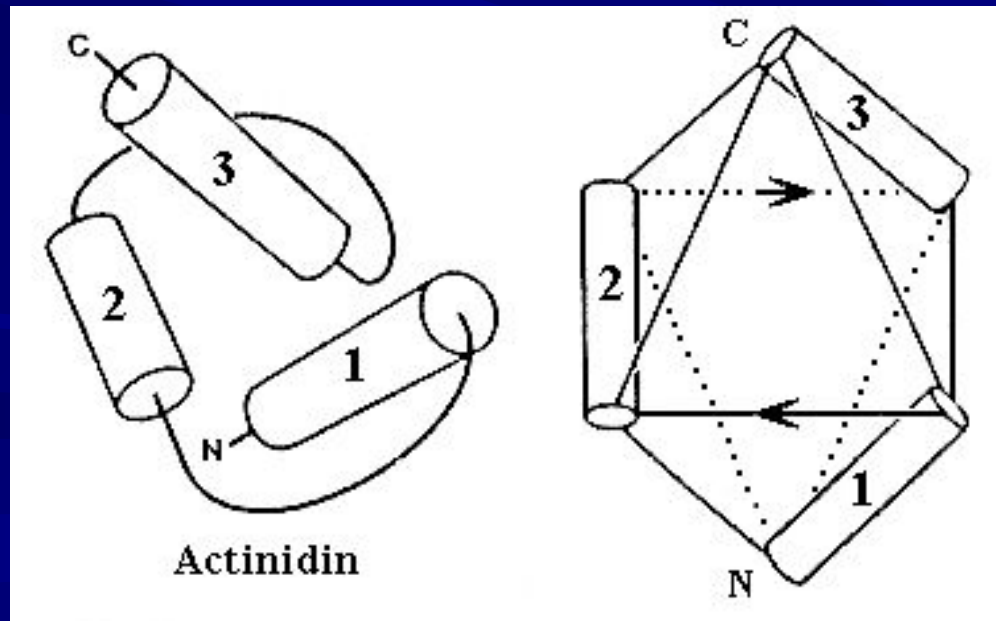


Thermolysin, domain 2

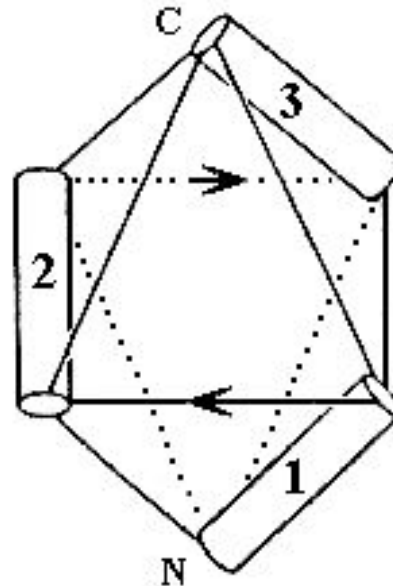


Quasi-  
spherical  
core:

**MOST COMMON**



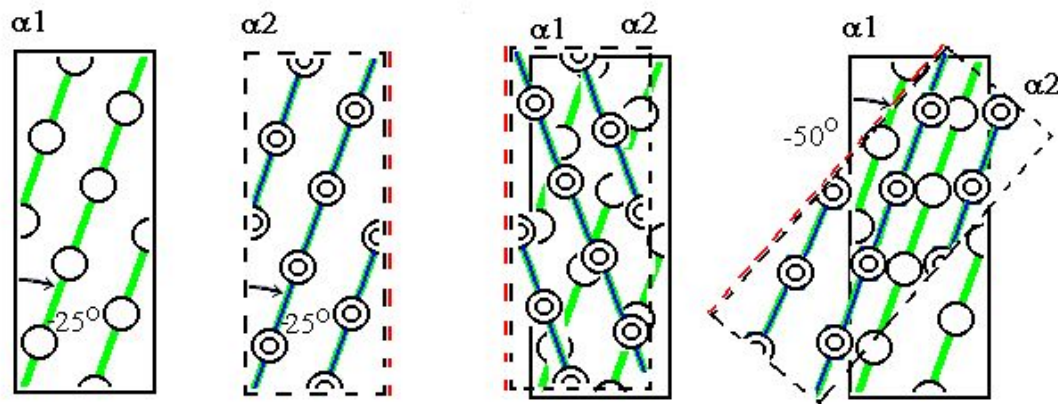
Actinidin



Quasi-spherical  
polyhedra

no loop turns of  $\sim 360^\circ$   
no loop crossings

a

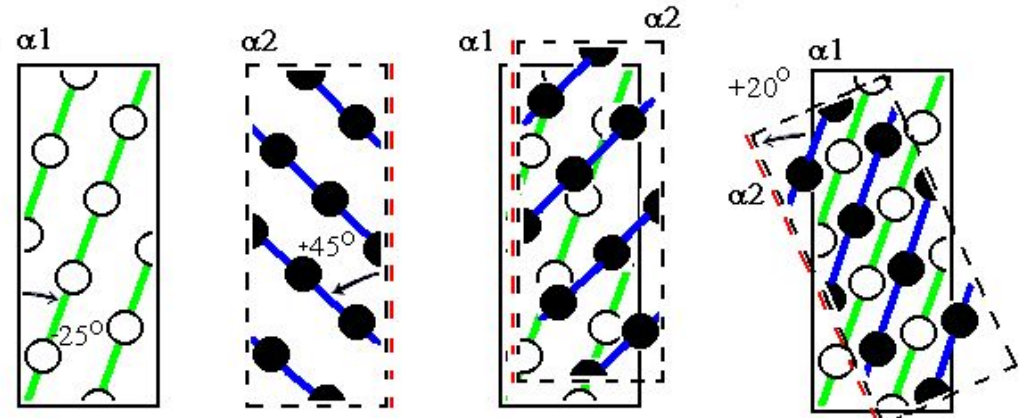


# CLOSE PACKING

## Packing of ridges:

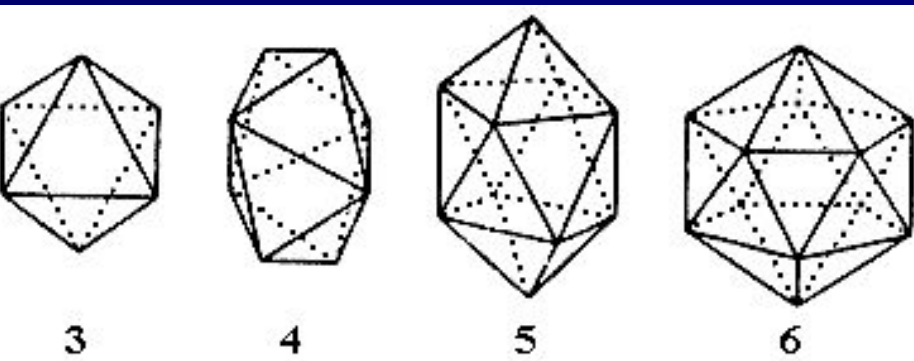
“0-4” & “0-4”:  $-50^\circ$

b

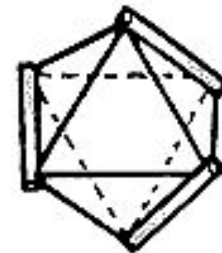


“0-4” & “1-4”:  $+20^\circ$

$-60^\circ \approx -50^\circ$      $+60^\circ \neq +20^\circ$



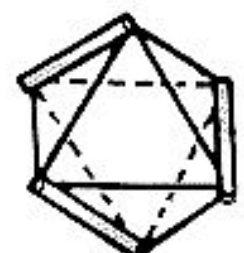
IDEAL POLYHEDRA



right-

( $-60^\circ$  between helices)

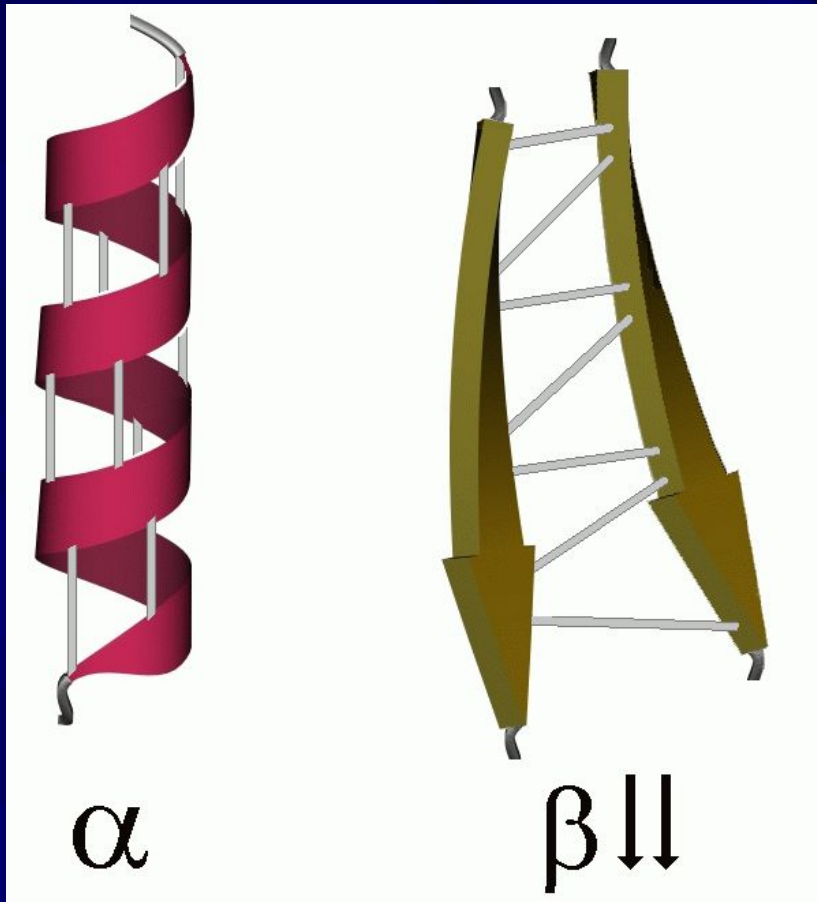
\* often \*



left-

( $+60^\circ$  between helices)

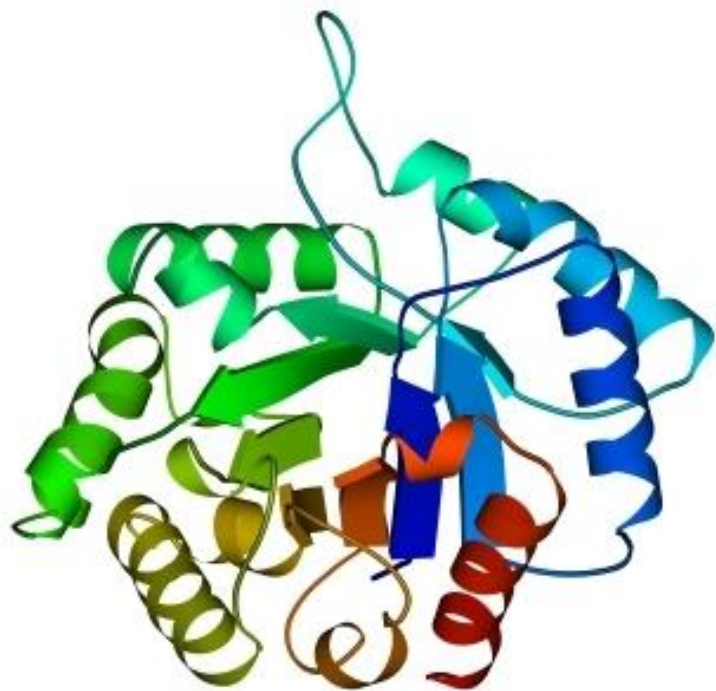
rare



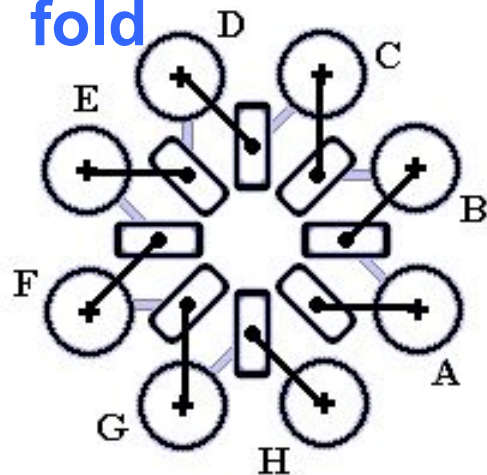
## $\alpha/\beta$ proteins

**H-bonds: within helices & sheets**

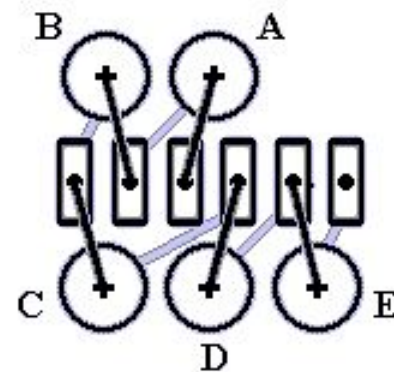
**Hydrophobics: between helices & sheets**



a **TIM barrel fold**



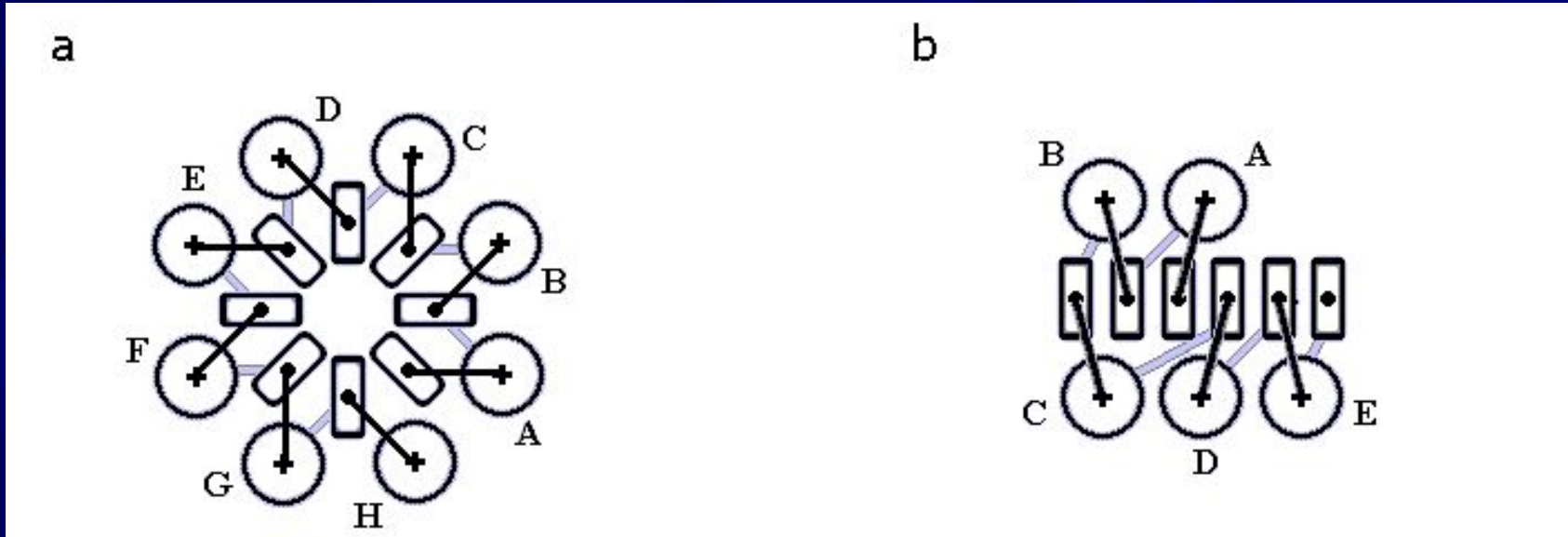
b **Rossmann**



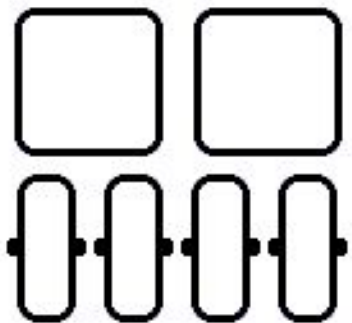


# Regular secondary structure sequence:

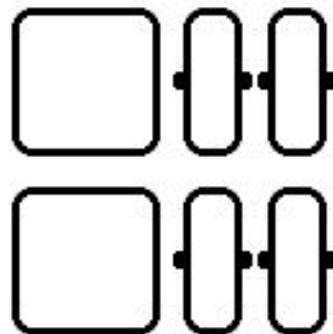
$\beta - \alpha - \beta - \alpha - \beta - \alpha - \beta - \alpha - \beta - \dots$



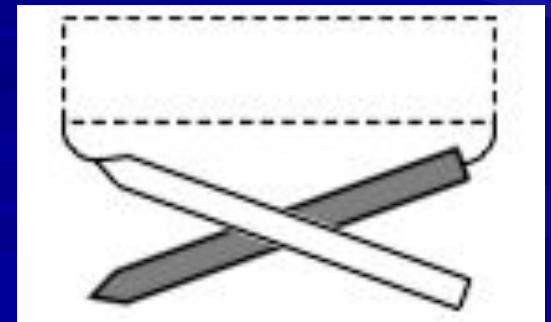
$\alpha$  and  $\beta$  layers

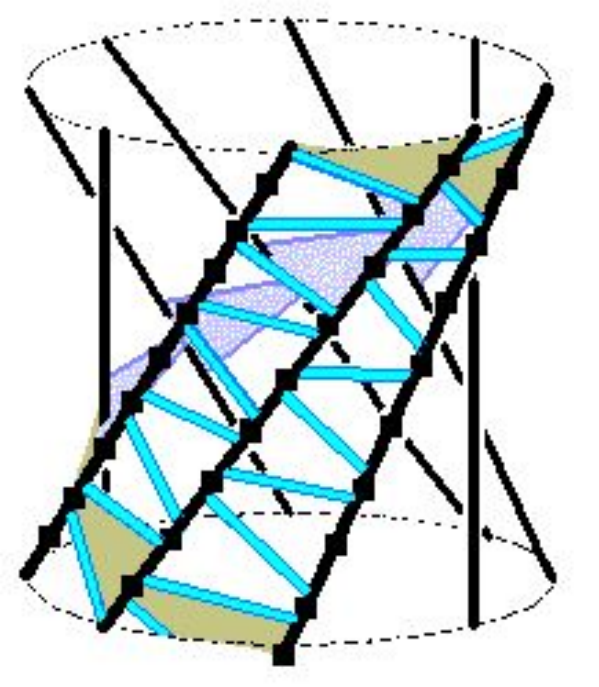


NO:

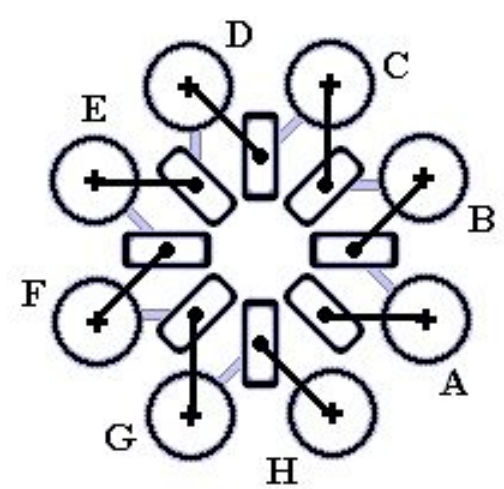


right-handed  
superhelices

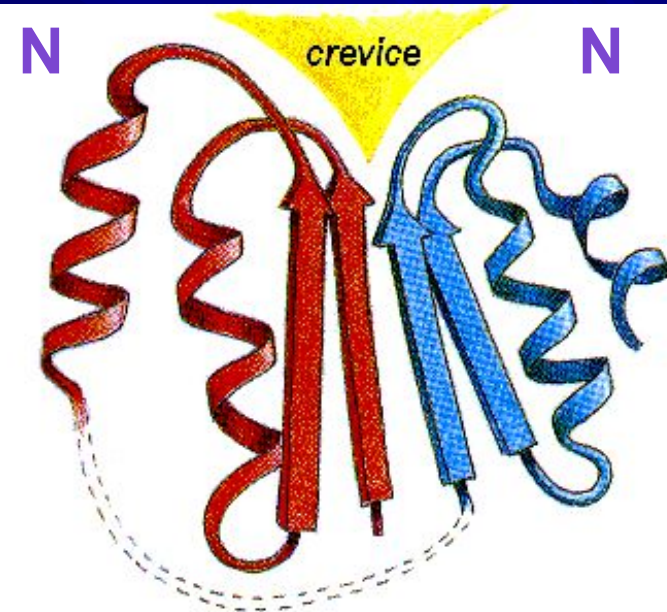
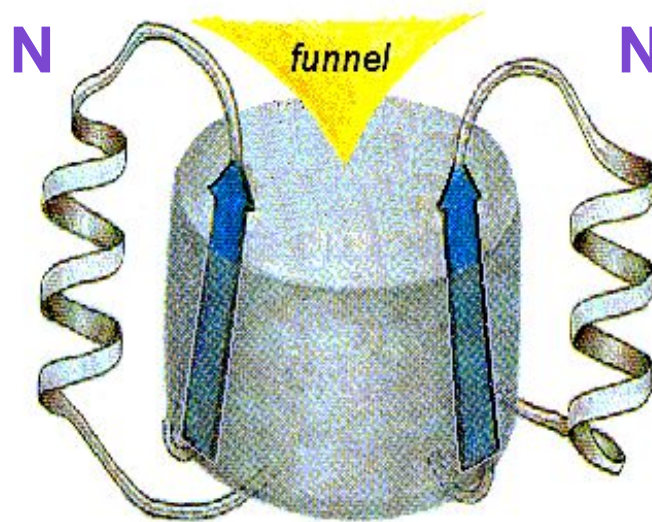




**Classification of  $\beta$ -barrels:**  
**“share number” S**  
**and**  
**strand number N.**  
**Here: S=8, N=8**



**Standard  
 active site  
 position is  
 given by  
 the archi-  
 tecture**





$\alpha$



$\beta \downarrow \uparrow$

$\alpha + \beta$  proteins

**H-bonds: within helices & sheets**

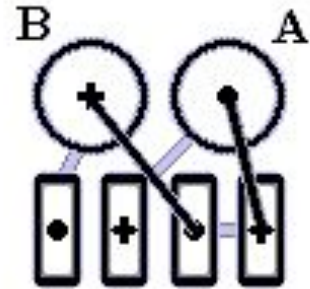
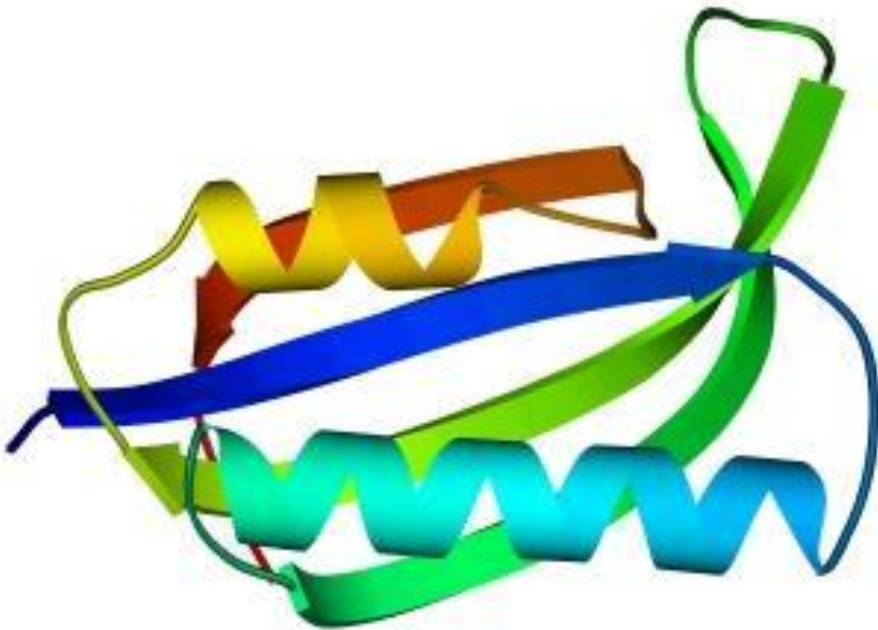
**Hydrophobics: between helices & sheets**



# $\alpha + \beta$ :

a) A kind of regularity in the secondary structure sequence:

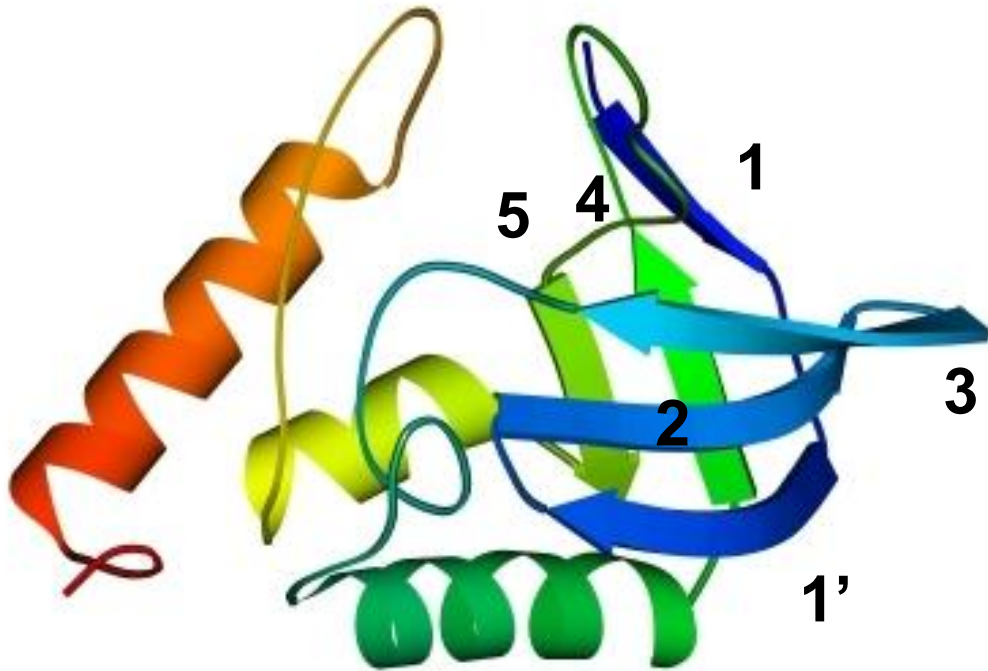
$\beta - \alpha - \beta - \beta - \alpha - \beta \dots$



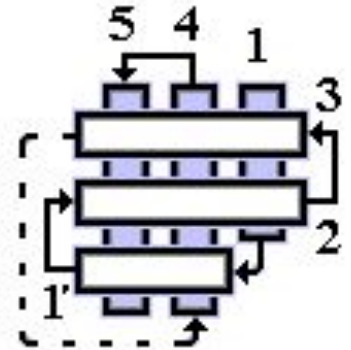
**Ferridoxin  
fold**

$\alpha + \beta$ :

b) Secondary structure sequence:  
composed of irregular blocks, e.g.:  
 $\beta - \beta - \beta - \beta - \beta - \alpha - \beta - \beta - \alpha - \alpha \dots$



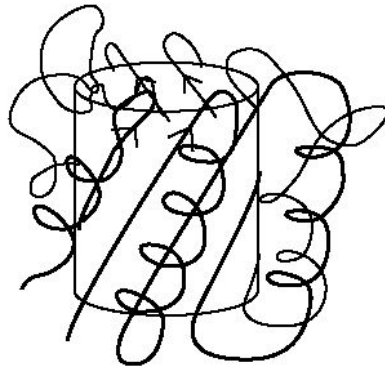
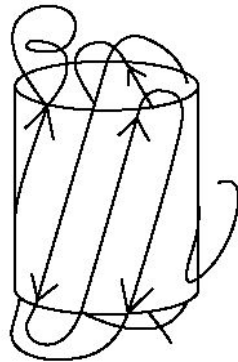
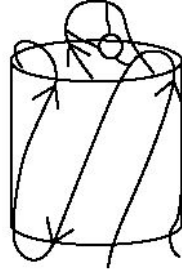
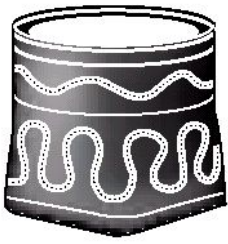
Nuclease fold



OB-fold

of the  $\beta$ -subdomain  
of nuclease

(“Russian doll effect”)



## TYPICAL FOLDING PATTERNS (1977)

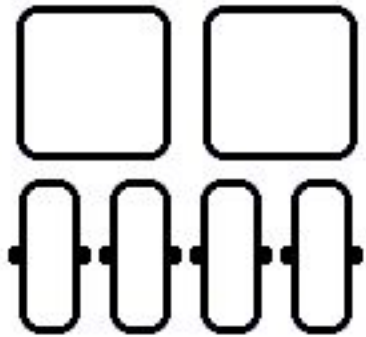


Jane Shelby  
Richardson,  
1941

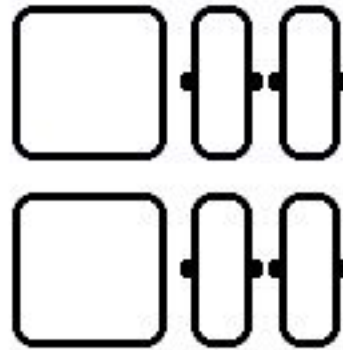


# EMPIRICAL RULES

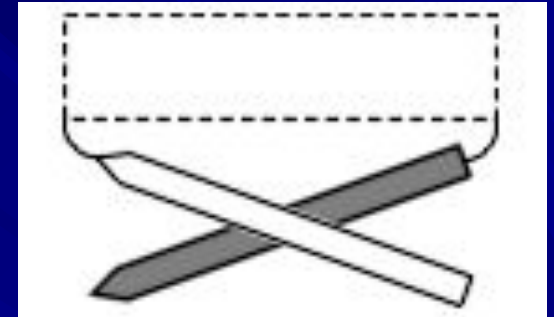
separate  $\alpha$  and  $\beta$  layers



NO:

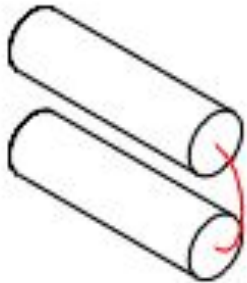


right-handed  
superhelices

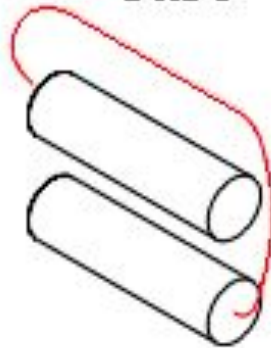


Lost H-bonds: defect!

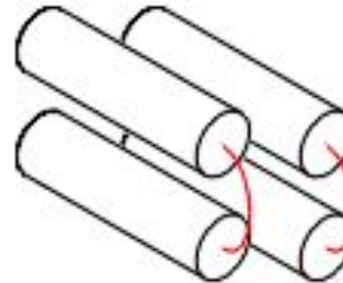
frequent



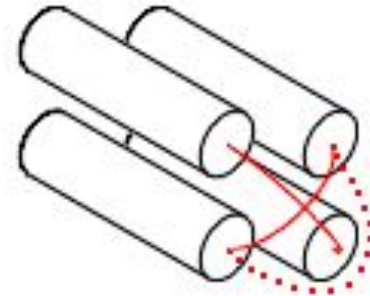
rare



frequent



rare



no large,  $\sim 360^\circ$  turns

NO 'defects'

no loop crossings

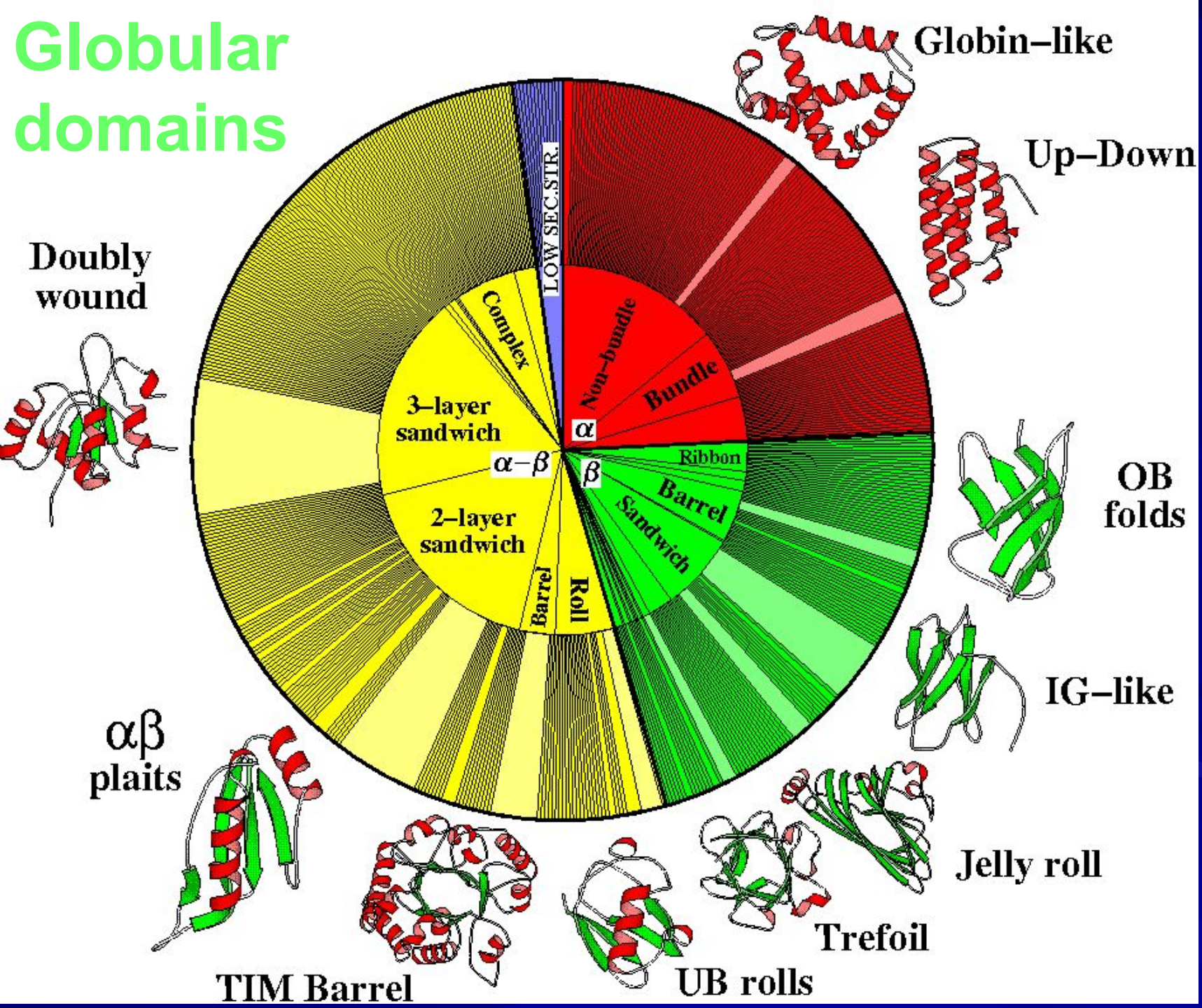
**RESULT:**  
**NARROW SET**  
**OF PREDOMINANT FOLDING PATTERNS**  
**these are those that have no 'defects'**

ALSO,

these are “**natively disordered proteins**”,  
which form a definite structure  
only when bound  
to some another molecule  
(ligand, DNA, protein...)



# Globular domains



# Classification of 3D protein folds



Алексей Григорьевич  
Мурзин, 1956

**SCOP**



Cyrus Homi **Chothia**,  
1942



**CATH**

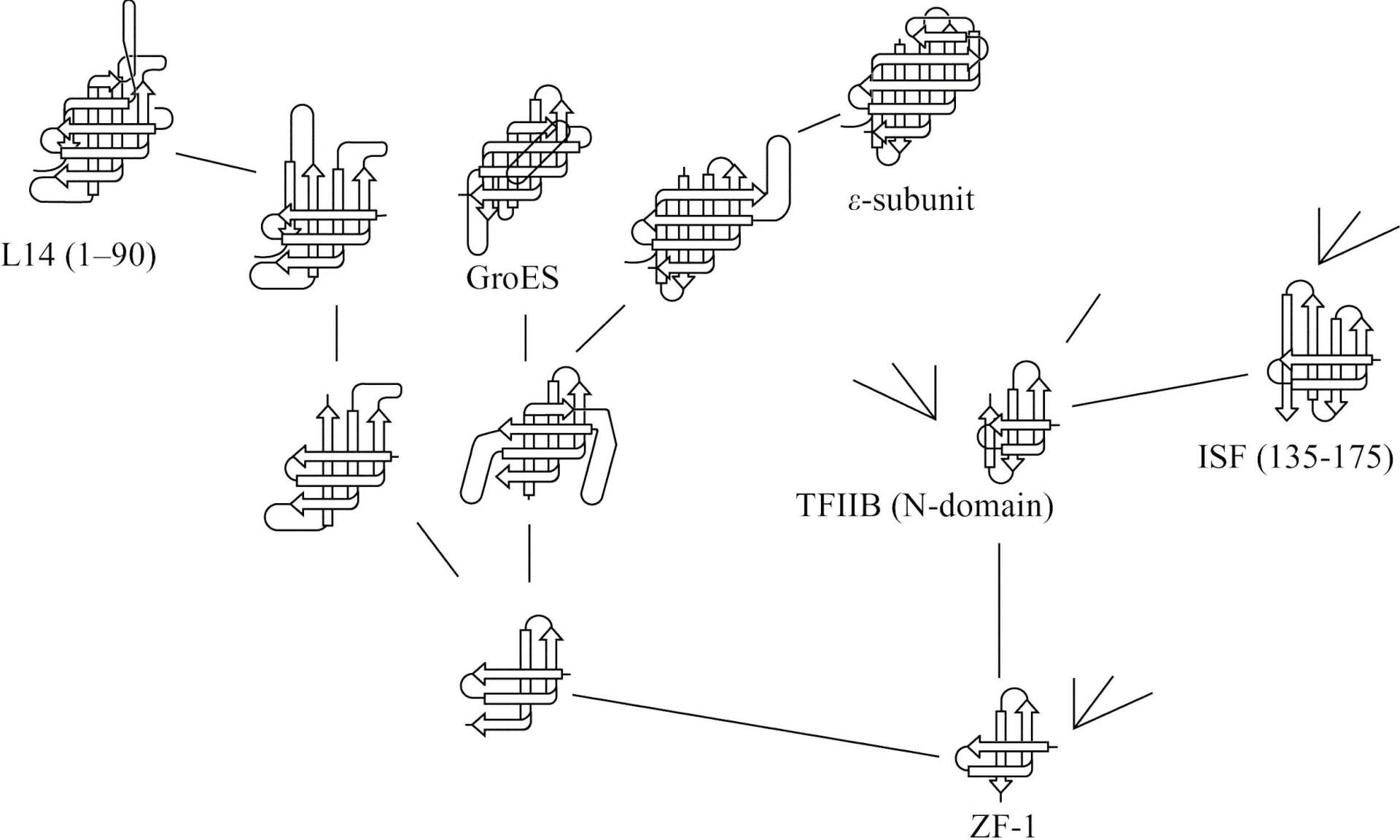
*Dame*  
Janet Maureen  
**Thornton**,  
1949

**«Деревья»**

Александр  
Васильевич  
**Ефимов**,  
1954







Efimov's "trees"



## 80/20 LAW:

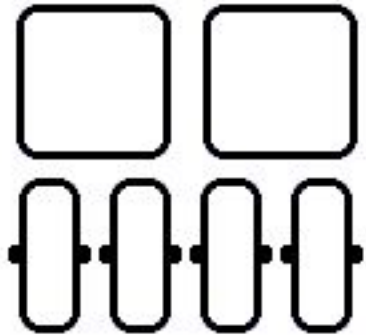
**80% OF BEER IS CONSUMED BY ONLY  
20% OF THE POPULATION**

**80% OF PROTEINS BELONG TO ONLY  
20% OF OBSERVED FOLDS**

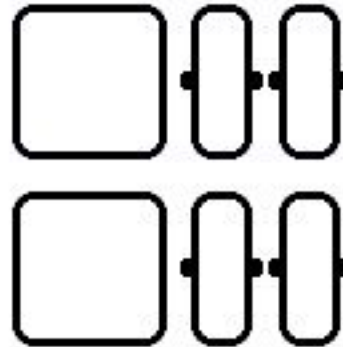
These folds are "typical" for proteins.  
The remaining 20% of proteins are scattered  
over "unusual" folds, which form 80% of  
observed folds

# EMPIRICAL RULES for FREQUENT FOLDS

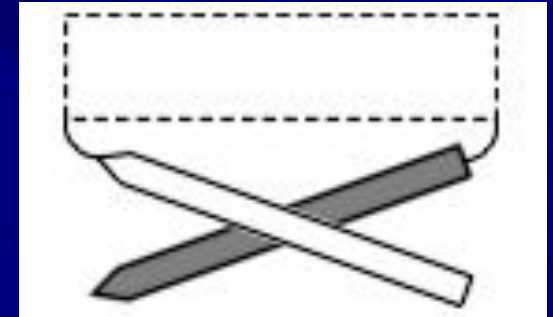
$\alpha$  and  $\beta$  structures,  
separate  $\alpha$  and  $\beta$  layers



NO:

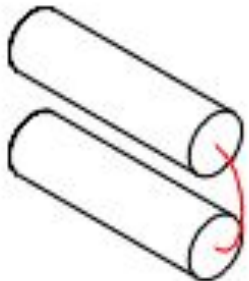


right-handed  
superhelices

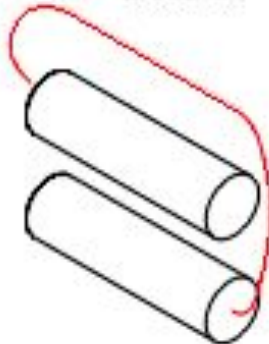


**Lost H-bonds: defect!**

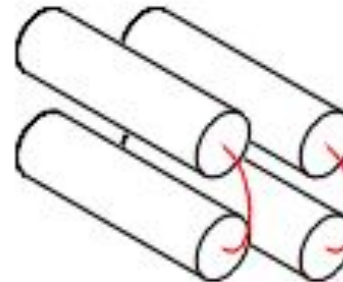
frequent



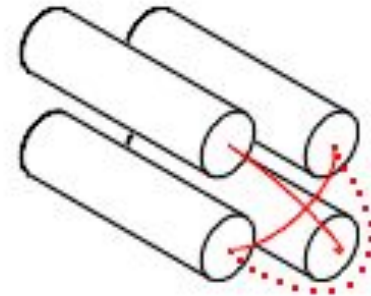
rare



frequent



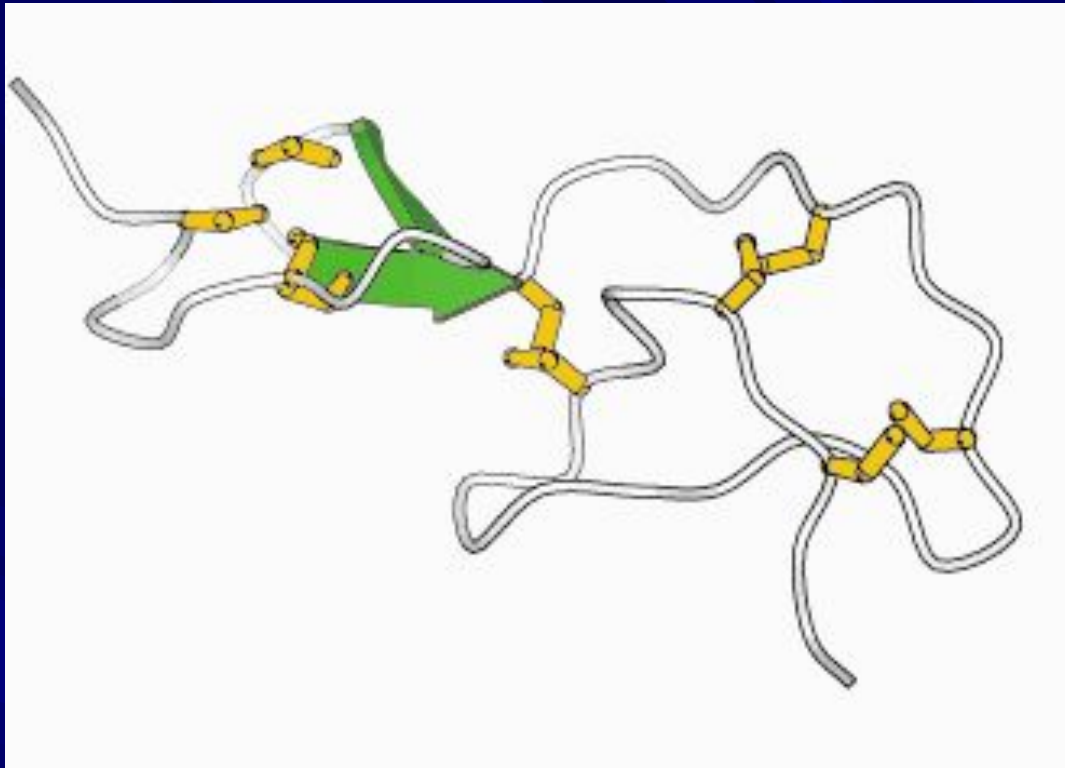
rare



no large (360-degree) turns

no loop crossing

e.g.:



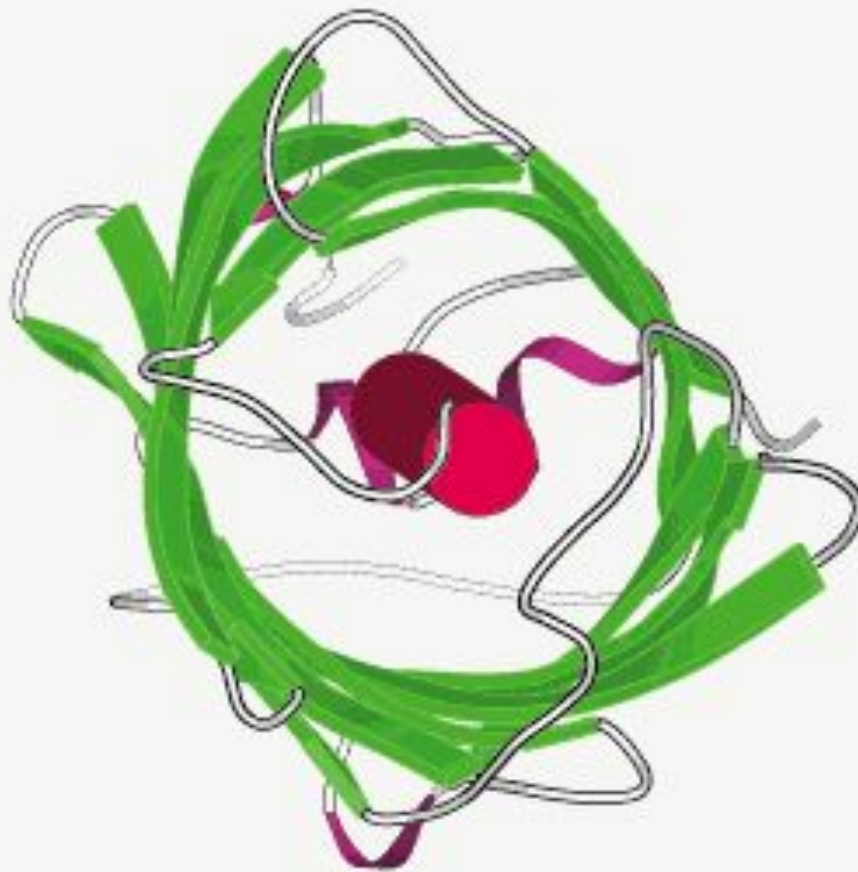
**Unusual fold**

(no  $\alpha$ , almost no  $\beta$  structure: **bad for stability**) -

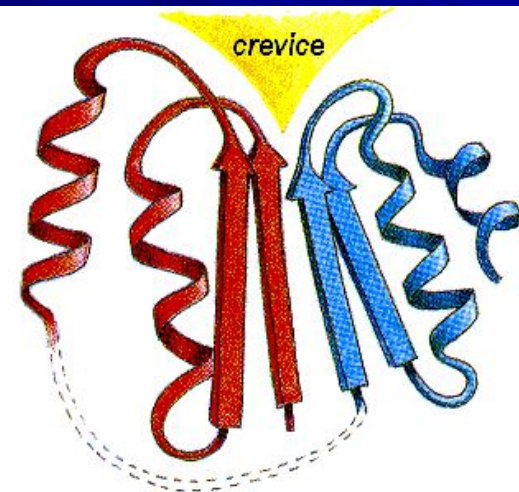
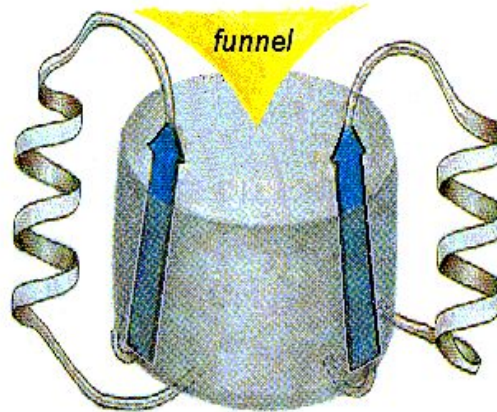
**BUT: very special sequence**

(very many Cysteins, and therefore  
very many S-S bonds)

Unusual  
fold (GFP):  
helix inside

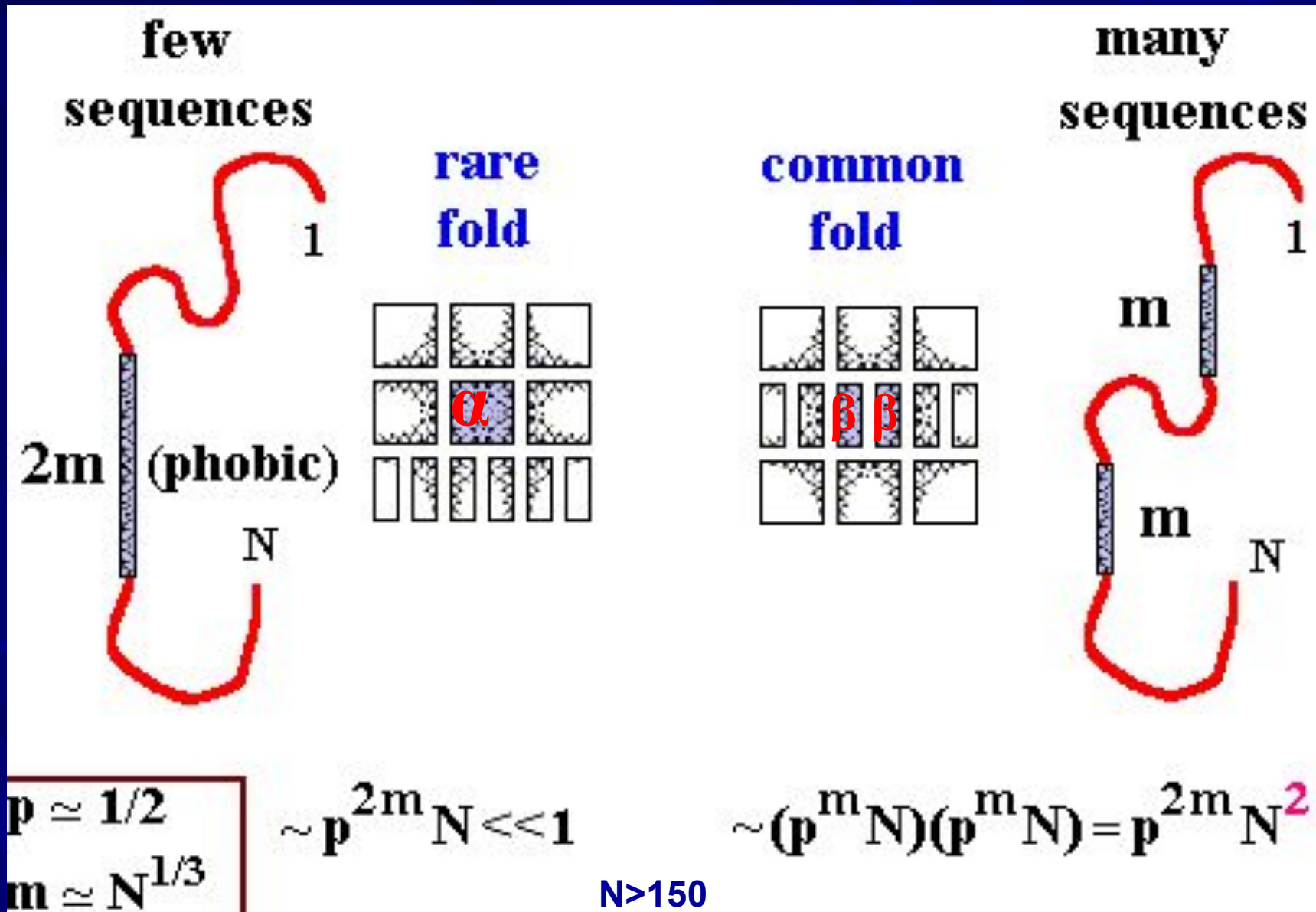


Usual folds:  
helices outside



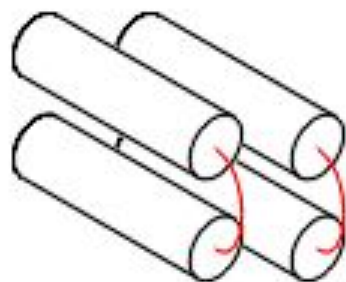


What is more usual:  
sequence providing  $\alpha$  inside or  $\beta\beta$  inside?

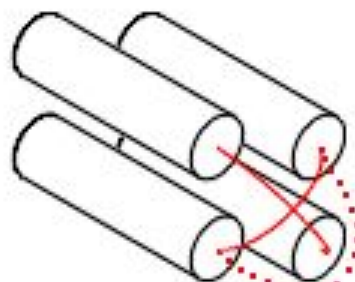


## Selected elements

**common**



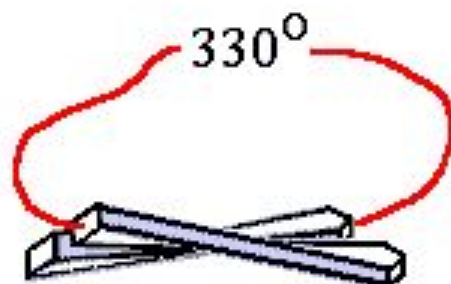
**rare**



**Defect: Loop crossing.**

Either lost H-bond (energy defect,  $\simeq +2$  kcal/mol  $\simeq +3kT$ ), or additional bending, or special sequence

**common**



**rare**



**Defect: additional bending.**

$\simeq +3kT$ . Entropic defect ?!  
 $\sim 20$  times less conformations  
= 20 times less chance to include the lowest-energy conformation

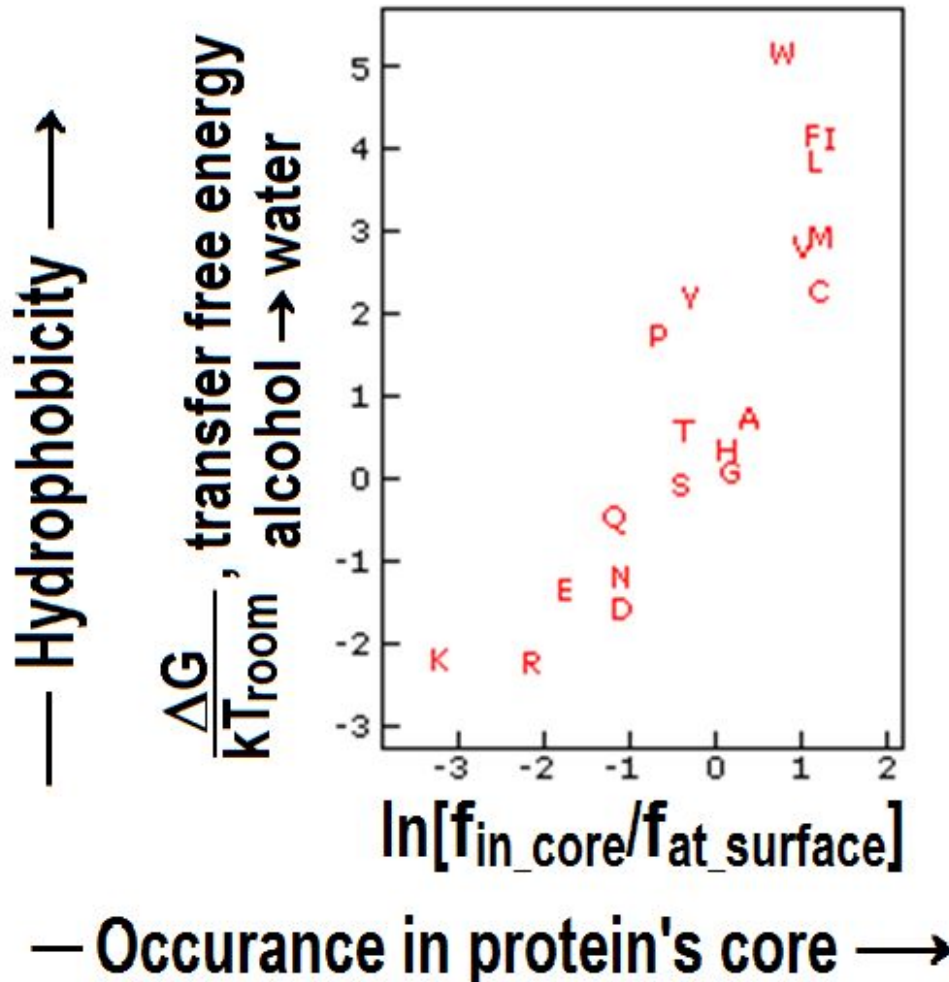
**free energy DEFECTS**

**common folds — NO DEFECTS — common sequences?**

**rare folds — WITH DEFECTS — rare sequences?**

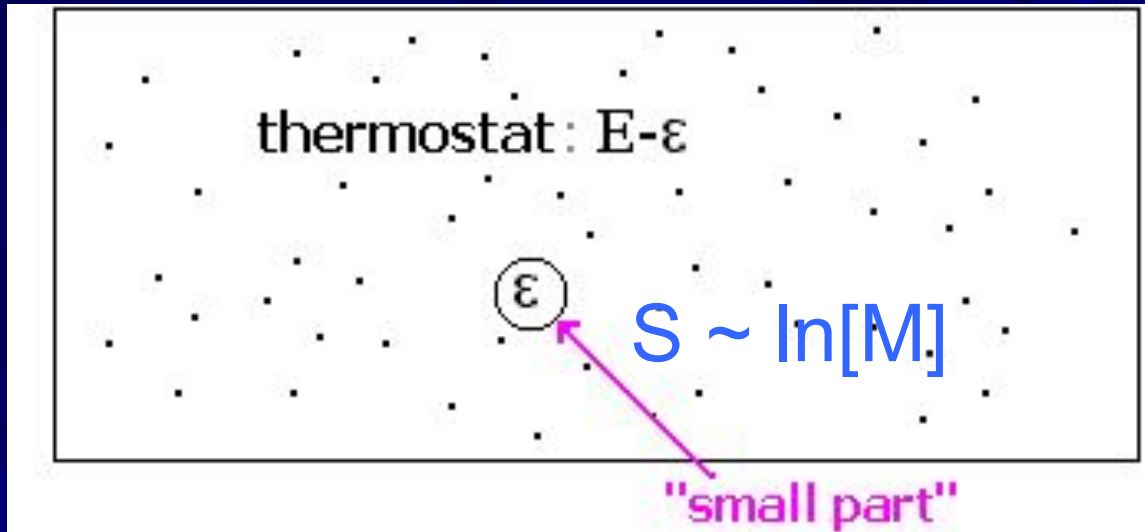
# Small protein details

Observation (Pohl, 1971):  
Occurrence  $\sim \exp\left[-\frac{\text{Free energy}}{kT_c}\right]$



Miller,  
Janin,  
Chothia  
1984

# WHAT IS “TEMPERATURE”?



## THEORY

Closed  
system:  
energy  
 $E = \text{const}$

CONSIDER: 1 state of “small part” with  $\varepsilon$  & all states of thermostat with  $E-\varepsilon$ .  $M(E-\varepsilon) = 1 \cdot M_{\text{th}}(E-\varepsilon)$

$$S_t(E-\varepsilon) = k \cdot \ln[M_t(E-\varepsilon)] \cong S_t(E) - \varepsilon \cdot (dS_t/dE)|_E$$

$$M_t(E-\varepsilon) = \exp[S_t(E)/k] \cdot \exp[-\varepsilon \cdot (dS_t/dE)|_E/k]$$

Thus:  $d[\ln(M_t)]/dE = 1/kT$



Gibbs:  $\frac{1}{kT} = \frac{d}{dE} \ln[\text{\#states}]$

'state' = *configuration*

E - *its energy*

as well:

'state' = *a. a. sequence*

E - *the structure's stability  
for this sequence*

**Protein structure is stable,  
if its free energy is below some threshold**

**For example:**

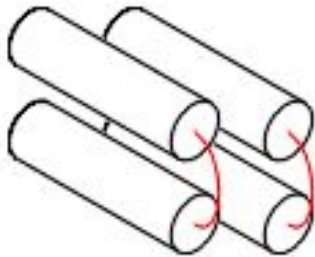
**below that of completely unfolded chain;**

**or:**

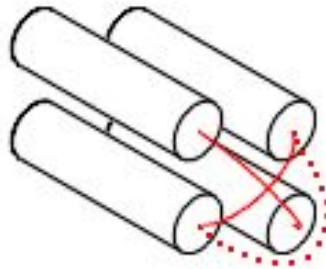
**below that of any other globular structure**

## PHYSICAL SELECTION OF FOLDS

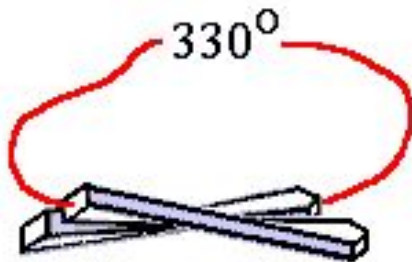
**common**



**rare**



**common**



**rare**



**free energy DEFECTS**

**common folds — NO DEFECTS —**  
— common sequences.

**rare folds — WITH DEFECTS —**  
— rare sequences.

*More stable detail —  
more random sequences*

*Less stable detail —  
less random sequences*

**What's good for protein's  
detail is good for the whole  
protein structure**

**“What's good for General  
Motors is good for America”**

*(a famous misquote of  
Charles Erwin **Wilson**)*

# **“Multitude principle”**

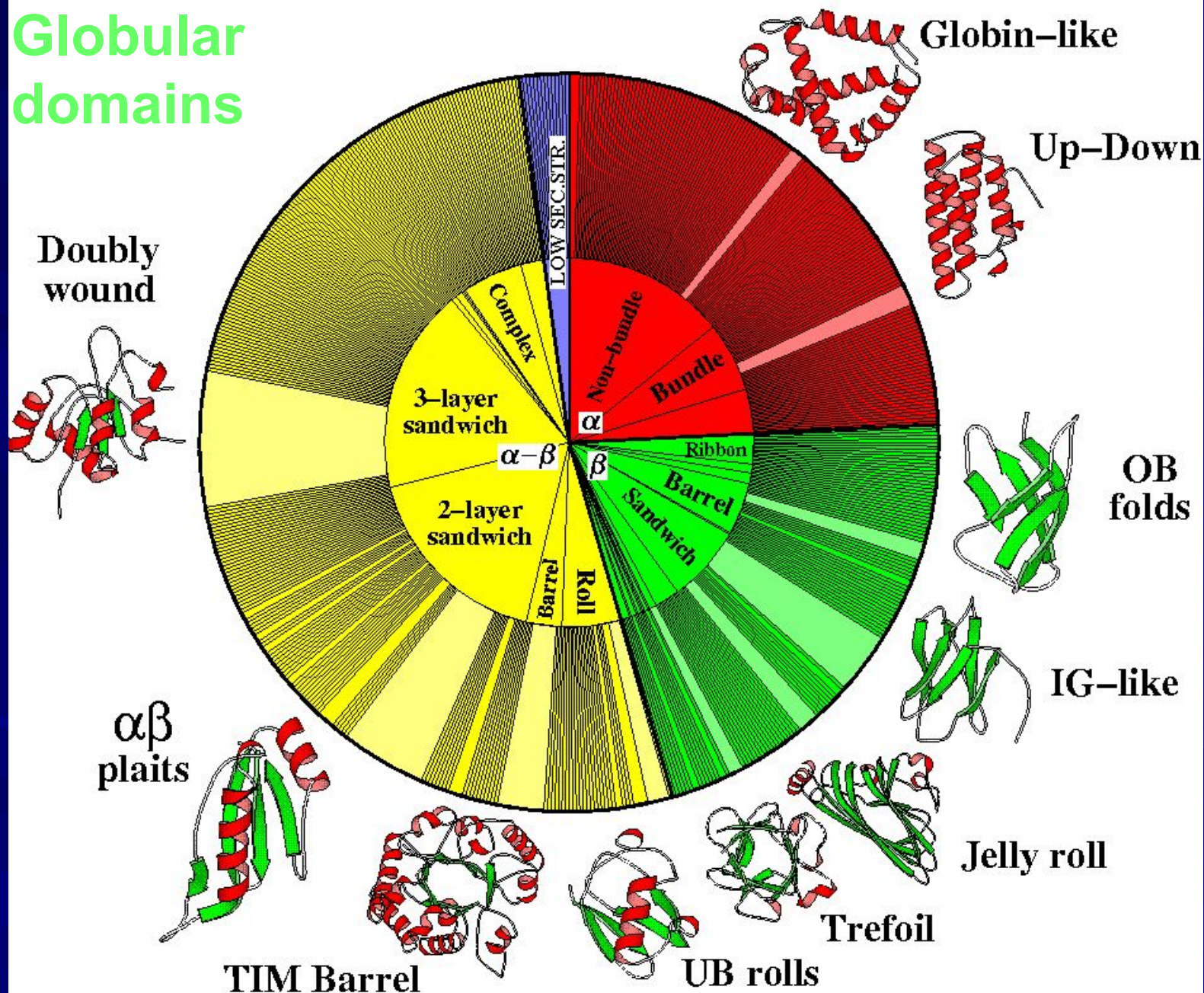
for physical selection of folds  
of globular proteins (*now*: **“designability”**):

*the more sequences fit the given  
architecture without destroying its stability,  
the higher the occurrence of this  
architecture in natural proteins.*



# RATIONAL STRUCTURAL CLASSIFICATION OF PROTEINS

Globular domains



CATH

≈

SCOP



- Structures of water-soluble globular proteins
- Physical selection of protein structures: *min. of defects!*
- Rational structural classification of proteins