Prelude to an Exam Allegro con brio Next Friday - EXAMINATION #2 Watch those WebAssigns .. no more extensions. Monday will be • A Quiz on Circuits A review of circuits and some other problems. Wednesday, more on Magnetism. Only day 1 on the exm. Watch for a new Webassign.

Magnetism

A Whole New Topic



M

Lodestone (Mineral)

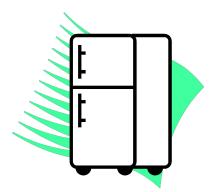


- Lodestones attracted iron filings.
- Lodestones seemed to attract each other.
- Used as a compass.
 - One end always pointed north.
- Lodestone is a natural magnet.

Magnetism

• Refrigerators are attracted to magnets!

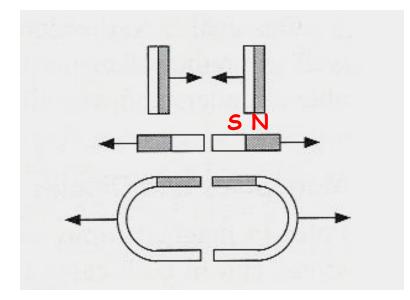






- Motors
- Navigation Compass
- Magnetic Tapes
 - Music, Data
- Television
 - Beam deflection Coil
- Magnetic Resonance Imaging
- High Energy Physics Research

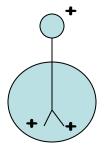
Magnets



Shaded End is NORTH Pole Shaded End of a compass points to the NORTH.

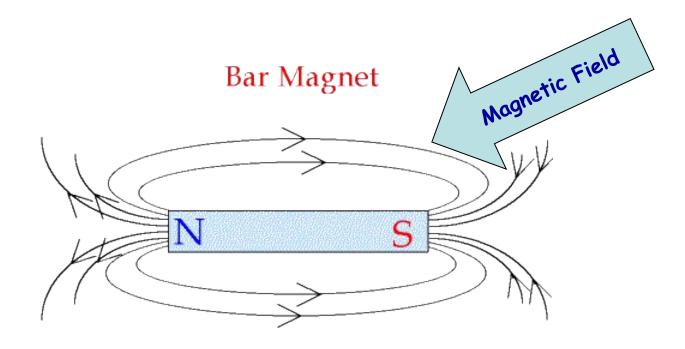
- Like Poles Repel
- Opposite Poles
 Attract
- Magnetic Poles are only found in pairs.
 - No magnetic monopoles have ever been observed.

Observations



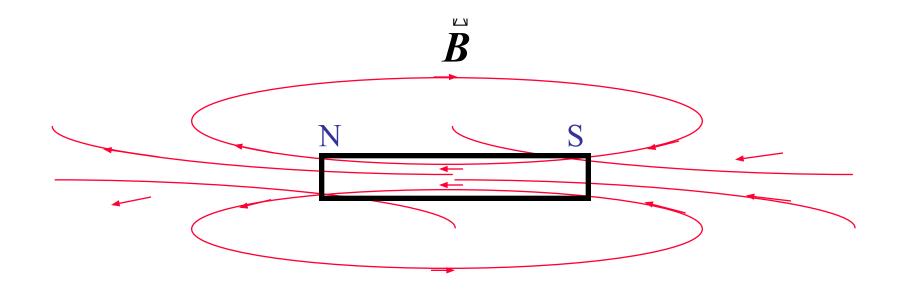
- Bring a magnet to a charged electroscope and nothing happens. No forces.
- Bring a magnet near some metals (Co, Fe, Ni ...) and it will be attracted to the magnet.
 - The metal will be attracted to both the N and S poles independently.
 - Some metals are not attracted at all.
 - Wood is NOT attracted to a magnet.
 - Neither is water.
- A magnet will force a compass needle to align with it. (No big Surprise.)

Magnets

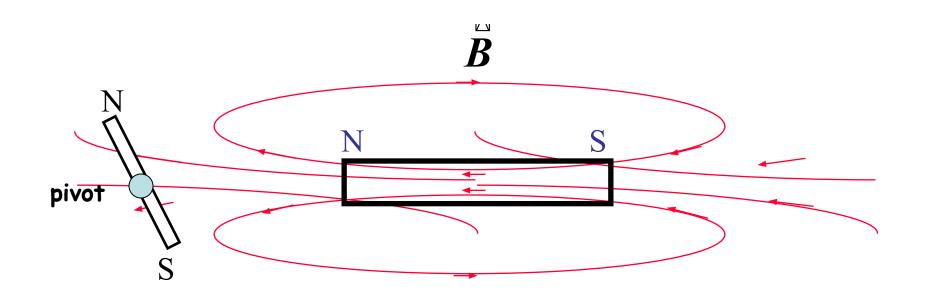


Cutting a bar magnet in half produces TWO bar magnets, each with N and S poles.

Consider a Permanent Magnet

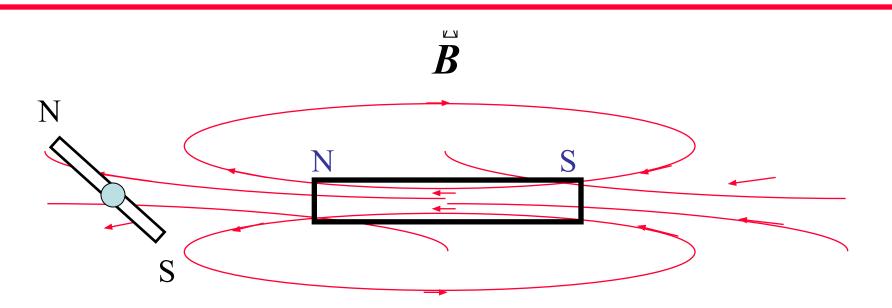


Introduce Another Permanent Magnet



The bar magnet (a magnetic dipole) wants to align with the B-field.

Field of a Permanent Magnet

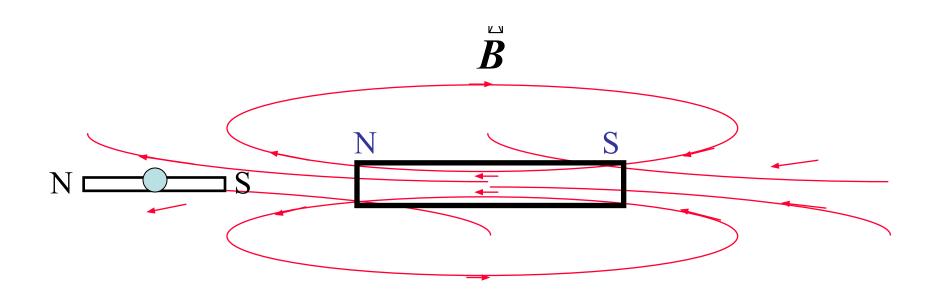


The south pole of the small bar magnet is attracted towards the north pole of the big magnet.

Also, the small bar magnet (a magnetic dipole) wants to align with the **B**-field.

The field attracts and exerts a torque on the small magnet.

Field of a Permanent Magnet



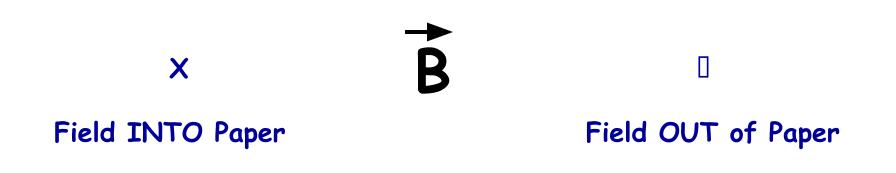
The bar magnet (a magnetic dipole) wants to align with the B-field.

The field exerts a *torque* on the dipole

The Magnetic Field

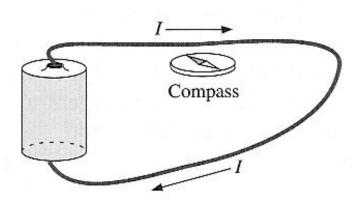
- Similar to Electric Field ... exists in space.
 - Has Magnitude AND Direction.
- The "stronger" this field, the greater is the ability of the field to interact with a magnet.

Convention For Magnetic Fields



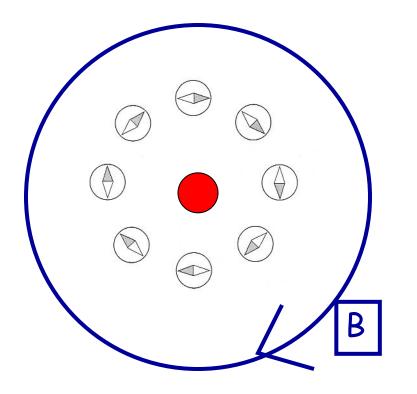
Experiments with Magnets Show

• Current carrying wire produces a circular magnetic field around it.



• Force on Compass Needle (or magnet) increases with current.

Current Carrying Wire



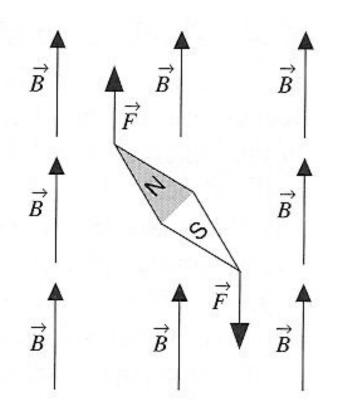
Current into the page.

Right hand Rule-Thumb in direction of the current Fingers curl in the direction of B

Current Carrying Wire

- B field is created at ALL POINTS in space surrounding the wire.
- The B field had magnitude and direction.
- Force on a magnet increases with the current.
- Force is found to vary as ~(1/d) from the wire.

Compass and **B** Field

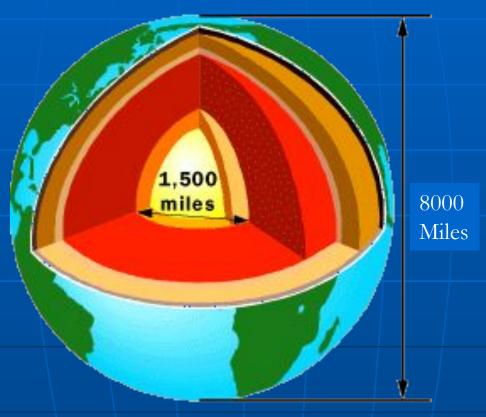


- Observations
 - North Pole of magnets tend to move toward the direction of B while S pole goes the other way.
 - Field exerts a TORQUE on a compass needle.
 - Compass needle is a magnetic dipole.
 - North Pole of compass points toward the NORTH.

Planet Earth



Inside it all.



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On the surface it looks like this..



Inside: Warmer than Floriduh



Much Warmer than Floriduh



Finally



In Between

- The molten iron core exists in a magnetic field that had been created from other sources (sun...).
- The fluid is rotating in this field.
- This motion causes a current in the molten metal.
- The current causes a magnetic field.
- The process is self-sustaining.
- The driving force is the heat (energy) that is generated in the core of the planet.

After molten lava emerges from a volcano, it solidifies to a rock. In most cases it is a black rock known as basalt, which is faintly magnetic, like iron emerging from a melt. Its magnetization is in the direction of the local magnetic force at the time when it cools down.

Instruments can measure the magnetization of basalt. Therefore, if a volcano has produced many lava flows over a past period, scientists can analyze the magnetizations of the various flows and from them get an idea on how the direction of the local Earth's field varied in the past. Surprisingly, this procedure suggested that times existed when the magnetization had the opposite direction from today's. All sorts of explanation were proposed, but in the end the only one which passed all tests was that in the distant past, indeed, the magnetic polarity of the Earth was sometimes reversed.

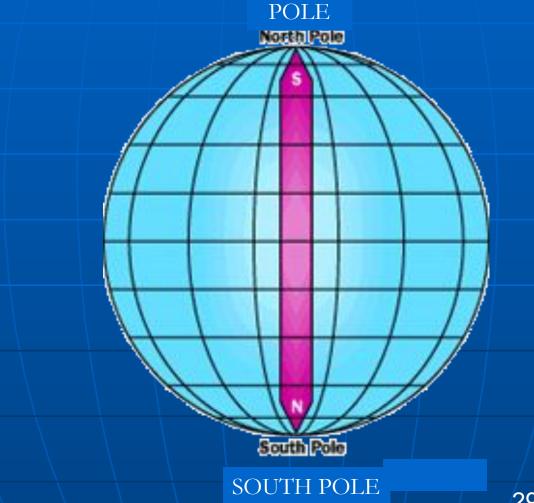
Ancient Navigation



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This planet is really screwed up!

NORTH

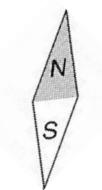


Repeat

Navigation DIRECTION N



S



Compass

Direction

If N direction is pointed to by the NORTH pole of the Compass Needle, then the pole at the NORTH of our planet must be a SOUTH MAGNETIC POLE! Navigation DIRECTION S



Ν

And it REVERSES from time to time.



Geographic North Pole

Geomagnetic Axis

Con

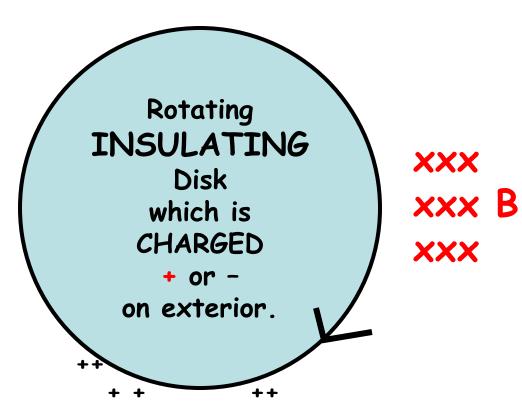
Geomagnetic North Pole



Magnetism

11%

Rowland's Experiment



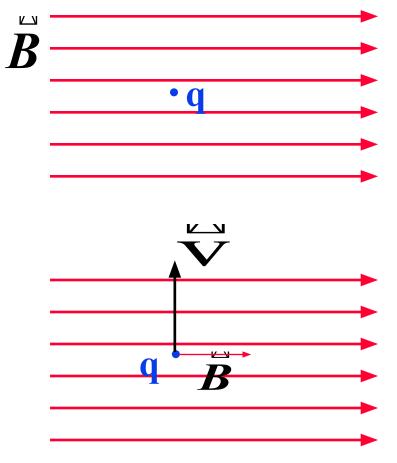
Field is created by any moving charge.

Increases with charge on the disk.

Increases with angular velocity of the disk.

Electrical curent is a moving charge.

A Look at the Physics



There is NO force on a charge placed into a magnetic field if the charge is NOT moving.

There is no force if the charge moves parallel to the field.

If the charge is moving, there is a force on the charge, *perpendicular* to both <u>v</u> and <u>B</u>.

$$\underline{\mathbf{F}} = \mathbf{q} \ \underline{\mathbf{v}} \times \underline{\mathbf{B}}$$
33

WHAT THE HECK IS THAT???

- A WHAT PRODUCT?
- A CROSS PRODUCT Like an angry one??
- Alas, yes
 - F=qv X B

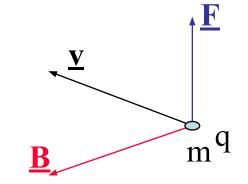
The Lorentz Force

This can be summarized as:

$$\vec{F} = q\mathbf{v} \times \vec{B}$$

or:

$$F = q \vee B \sin \theta$$

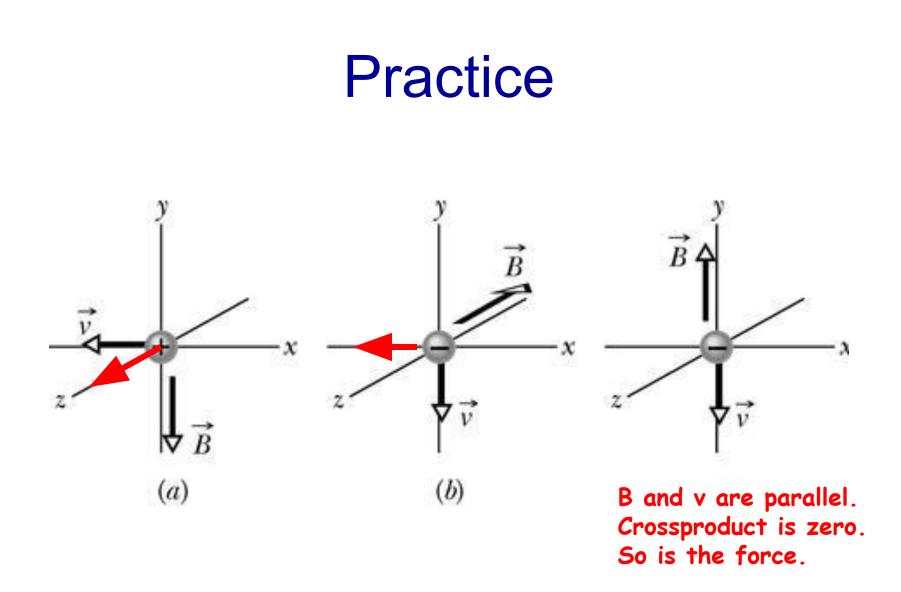


 $\boldsymbol{\theta}$ is the angle between B and V

Note

B is sort of the Force per unit (charge-velocity)

Whatever that is!!

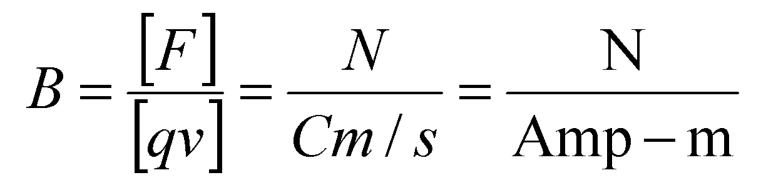


Which way is the Force???

Units

 $F = Bqv Sin(\theta)$

Units :



 $1 \text{ tesla} = 1 \text{ T} = 1 \text{ N/}(A_{2}, m)$





At the Surface of the Earth	3 x 10⁻⁵ T
Typical Refrigerator Magnet	5 x 10 ⁻³ T
Laboratory Magnet	0.1 T
Large Superconducting Magnet	10 T

The Magnetic Force is *Different* From the Electric Force.

Whereas the electric force acts in the same direction as the field:

$$\vec{F} = q\vec{E}$$

The magnetic force acts in a direction orthogonal to the field:

$$\vec{F} = q\vec{v} \times \vec{B}$$

(Use "Right-Hand" Rule to determine direction of \underline{F})

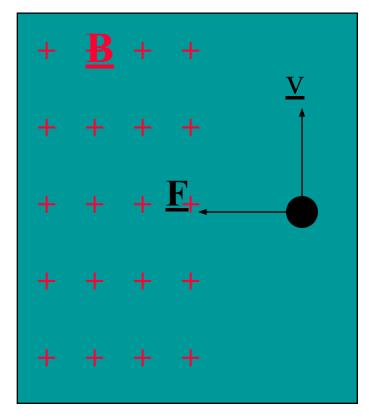
Magneusin

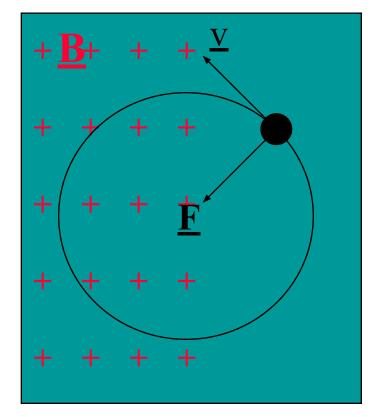


- A moving charge can create a magnetic field.
- A moving charge is acted upon by a magnetic field.
- In Magnetism, things move.
- In the Electric Field, forces and the field can be created by stationary charges.

Trajectory of Charged Particles in a Magnetic Field

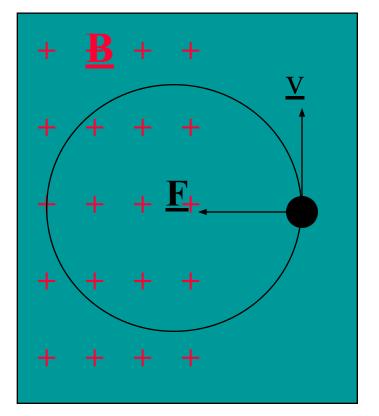
(<u>B</u> field points *into* plane of paper.)

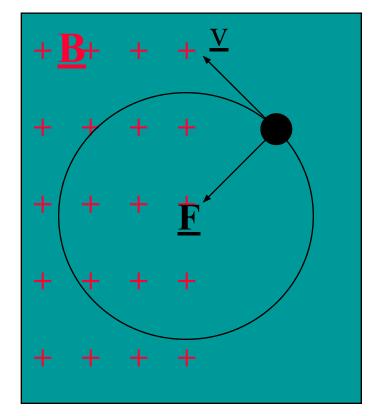




Trajectory of Charged Particles in a Magnetic Field

(<u>B</u> field points *into* plane of paper.)





Magnetism Magnetic Force is a <u>centripetal</u> fqsce

Review of Rotational Motion

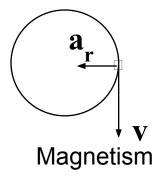
$$\theta = s / r \implies s = \theta r \implies ds/dt = d\theta/dt r \implies v = \omega r$$

 θ = angle, ω = angular speed, α = angular acceleration

 $a_t = r \alpha$ tangential acceleration $a_r = v^2 / r$ radial acceleration

The radial acceleration changes the direction of motion, while the tangential acceleration changes the speed.

Uniform Circular Motion

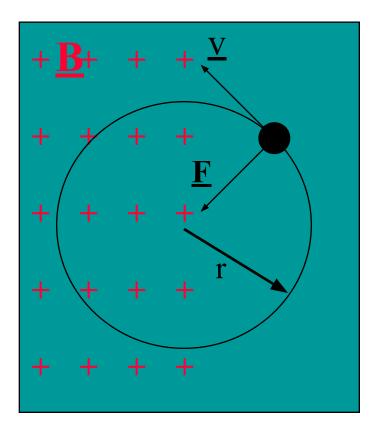


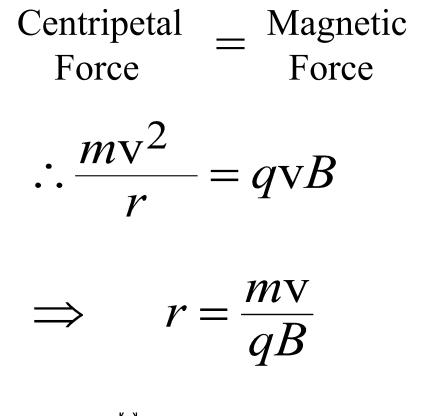
 $\omega = \text{constant} \Rightarrow \text{v} \text{ and } a_{r} \text{ constant but direction changes}$

$$a_{r} = v^{2}/r = \omega^{2} r - \begin{bmatrix} KE = \frac{1}{2} mv^{2} = \frac{1}{2} mw^{2}r^{2} \\ F = ma_{r} = mv^{2}/r = 44\omega^{2}r \end{bmatrix}$$

YES ! You have to remember this stuff.

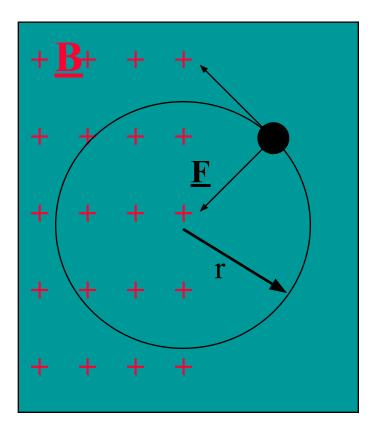
Radius of a Charged Particle Orbit in a Magnetic Field





Note: as $\overline{F} \perp \overline{\mathbf{v}}$, the magnetic force does no werk!

Cyclotron Frequency



Magnetism

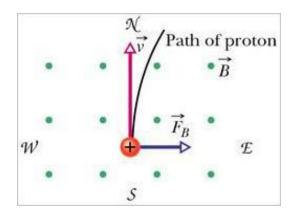
The time taken to complete one orbit is:

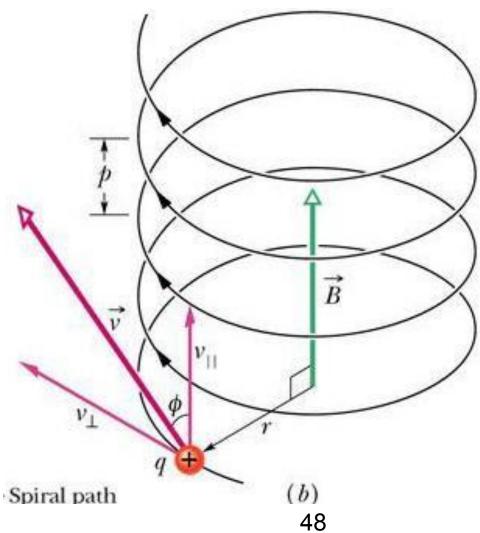
$$T = \frac{2\pi r}{v}$$
$$= \frac{2\pi}{v} \frac{mv}{qB}$$

$$f = \frac{1}{T} = \frac{qB}{2\pi m}$$

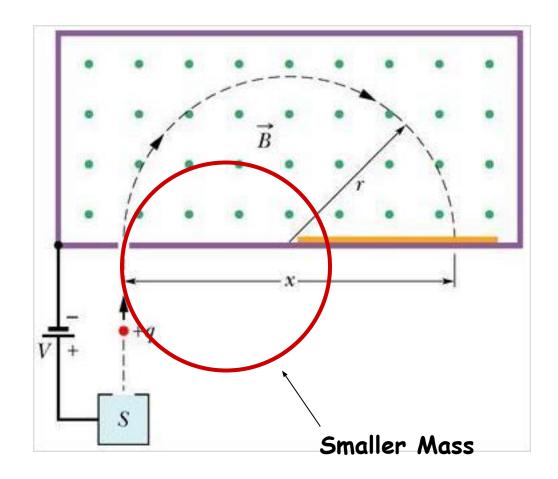
$$\omega_c = 2\pi f = \frac{qB}{m}$$

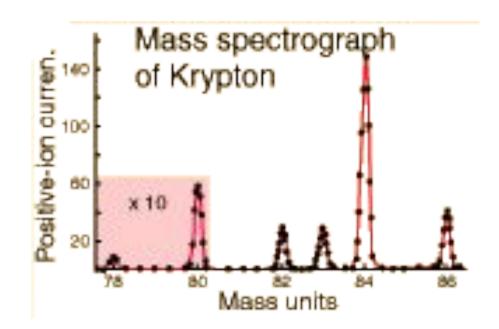
More Circular Type Motion in a Magnetic Field



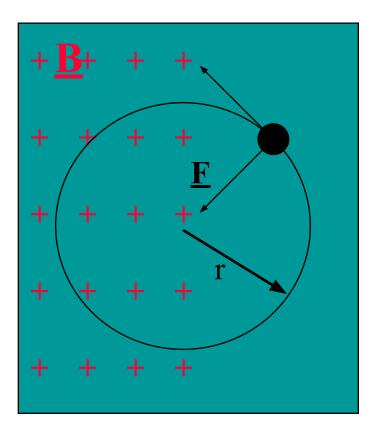


Mass Spectrometer





Cyclotron Frequency



Magnetism

The time taken to complete one orbit is:

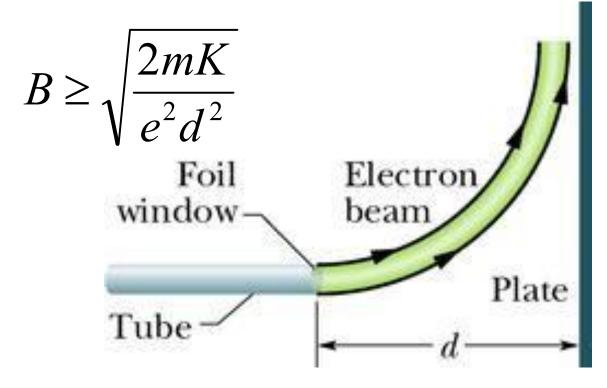
$$T = \frac{2\pi r}{v}$$
$$= \frac{2\pi}{v} \frac{mv}{qB}$$

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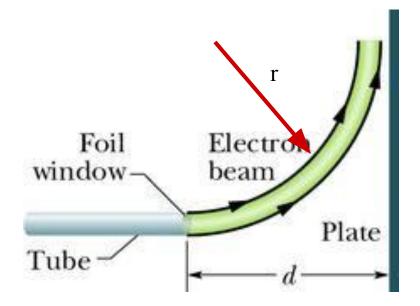
$$\omega_c = 2\pi f = \frac{qB}{m}$$

An Example

A beam of electrons whose kinetic energy is K emerges from a thin-foil "window" at the end of an accelerator tube. There is a metal plate a distance dfrom this window and perpendicular to the direction of the emerging beam. Show that we can prevent the beam from hitting the plate if we apply a uniform magnetic field B such that



Problem Continued



From Before

$$r = \frac{mv}{qB}$$

$$K = \frac{1}{2}mv^{2} \text{ so } v = \sqrt{\frac{2K}{m}}$$

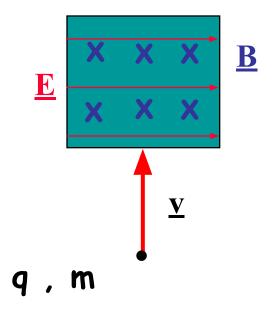
$$r = \frac{m}{eB}\sqrt{\frac{2K}{m}} = \sqrt{\frac{2mK}{e^{2}B^{2}}} \le d$$
Solve for B:
$$B \ge \sqrt{\frac{2mK}{e^{2}d^{2}}}$$
53

Some New Stuf

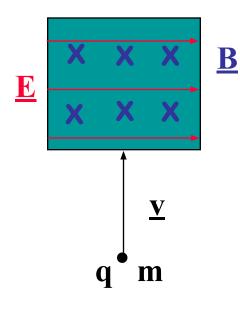
Magnetism and Force

5

Let's Look at the effect of crossed **E** and **B** Fields:



What is the relation between the intensities of the electric and magnetic fields for the particle to move in a straight line ?.



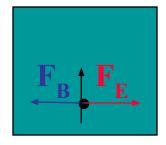
$$\mathbf{F}_{\mathbf{E}} = \mathbf{q} \mathbf{E}$$
 and $\mathbf{F}_{\mathbf{B}} = \mathbf{q} \mathbf{v} \mathbf{B}$

If $F_E = F_B$ the particle will move following a straight line trajectory

$$\mathbf{q} \mathbf{E} = \mathbf{q} \mathbf{v} \mathbf{B}$$



$$\mathbf{v} = \mathbf{E} / \mathbf{B}$$



What does this mean??

- This equation only contains the E and B fields in it.
- Mass is missing!
- Charge is missing!
- This configuration is a velocity filter!

"Real" Mass Spectrometer

- Create ions from injected species.
 - This will contain various masses, charges and velocities.
 - These are usually accelerated to a certain ENERGY (KeV) by an applied electric field.
 - The crossed field will only allow a selected velocity to go forward into the MS.
 - From before: R=mv/Bq

Components of MS:

Accelerate the ions through a known potential difference.

$$\frac{1}{2}mv^{2} = qV_{applied}$$
So
$$\frac{q}{m} = \frac{1}{2}v^{2}\frac{1}{V_{applied}}$$

The velocity can be selected via an $E \times B$ field and the MS will separate by:

$$R = \frac{mv}{Bq}$$
 Unknown is mass to charge ratio which can be sorted from the spectrum





VECTOR CALCULATIONS $\mathbf{a} \times \mathbf{b} = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ a_x & a_y & a_z \\ b_x & b_y & b_z \end{vmatrix}$

Problem: A Vector Example A proton of charge +e and mass m is projected into a uniform magnetic field B=Bi with an initial velocity $v=v_{0x}i +v_{0y}j$. Find

the velocity at a later time.

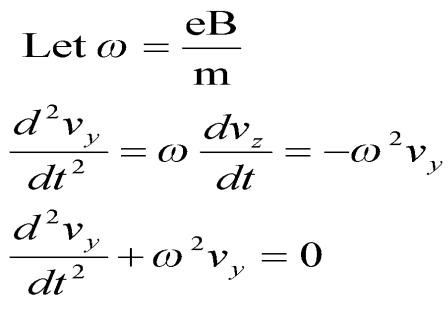
$$\mathbf{F} = e\mathbf{v} \times \mathbf{B}$$
$$\mathbf{F} = \begin{vmatrix} i & j & k \\ v_x & v_y & v_z \\ B & 0 & 0 \end{vmatrix} = eB(v_z\mathbf{j} - v_y\mathbf{k}) = m\mathbf{a}$$
$$ma_x = m\frac{dv_x}{dt} \text{ etc. for y and z.}$$

Equating components :

$$\frac{dv_x}{dt} = 0 \qquad \frac{dv_y}{dt} = \frac{eB}{m}v_z \quad \text{and} \quad \frac{dv_z}{dt} = -\frac{eB}{m}v_y$$

$$v_x \text{ is constant} \qquad 62$$

More



Simple circular motion!

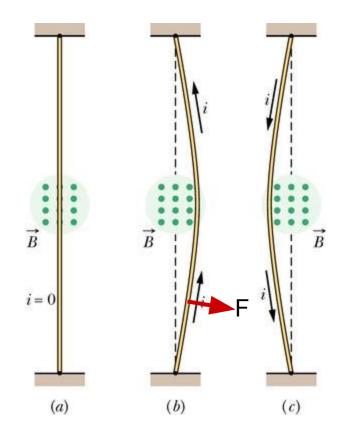
$$\mathbf{v}_{y} = \mathbf{v}_{0y} \cos(\omega t)$$

Same thing for z.



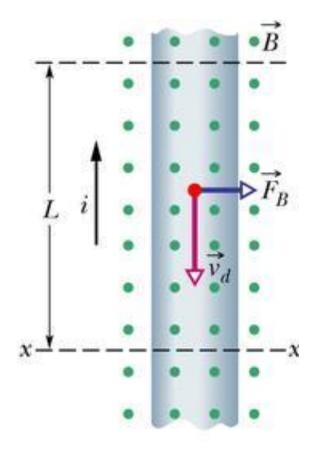
Wires

- A wire with a current contains moving charges.
- A magnetic field will apply a force to those moving charges.
- This results in a force on the wire itself.
 - The electron's sort of PUSH on the side of the wire.



Remember: Electrons go the "other way".

The Wire in More Detail



Assume all electrons are moving with the same velocity v_d.

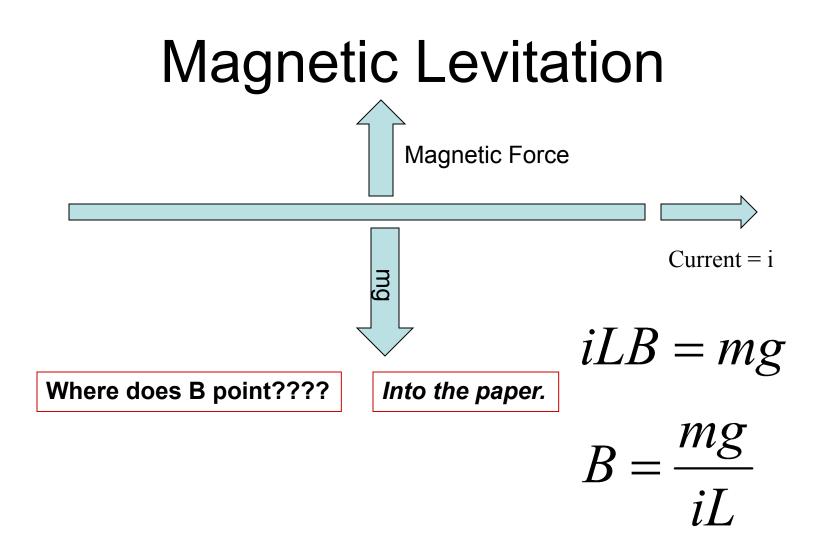
$$q = i \times t = i \frac{L}{v_d}$$
$$F = qv_d B = i \frac{L}{v_d} v_d B = iLB$$

vector:

 $\mathbf{F} = i\mathbf{L} \times \mathbf{B}$

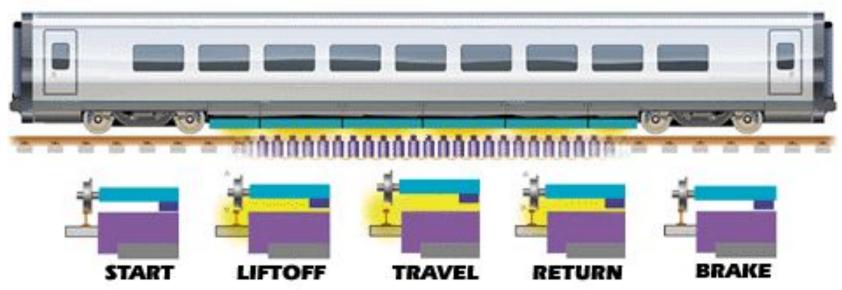
L in the direction of the motion of POSITIVE charge (i).

B out of plane of the paper Magnetism

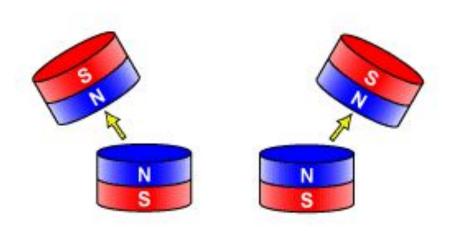




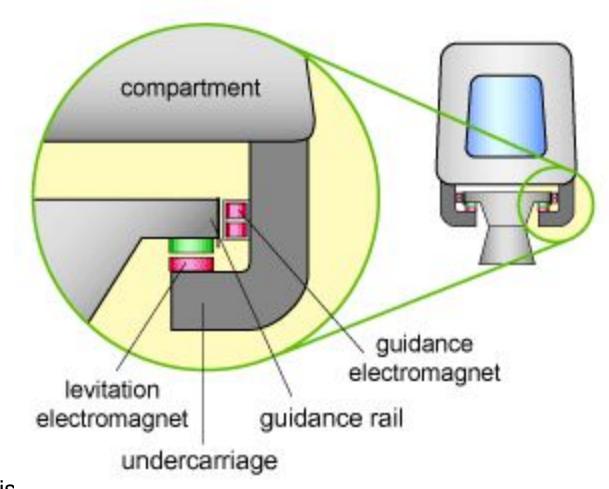
Traveling Over The Rails



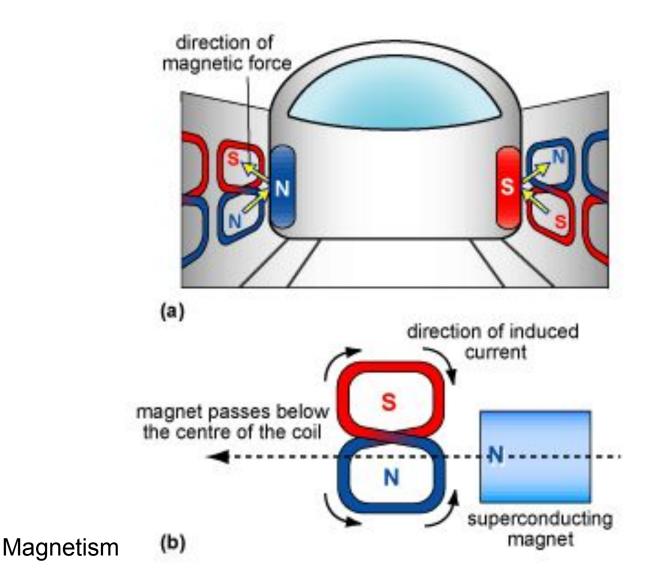
Magnetic Repulsion



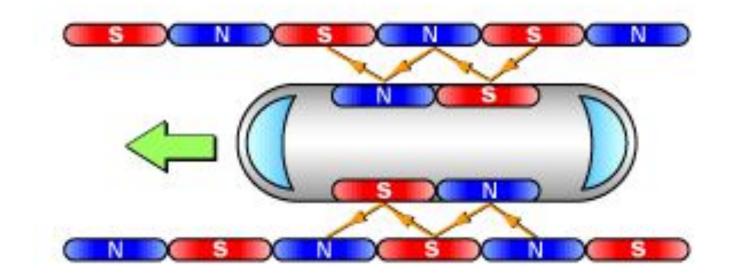




Moving Right Along



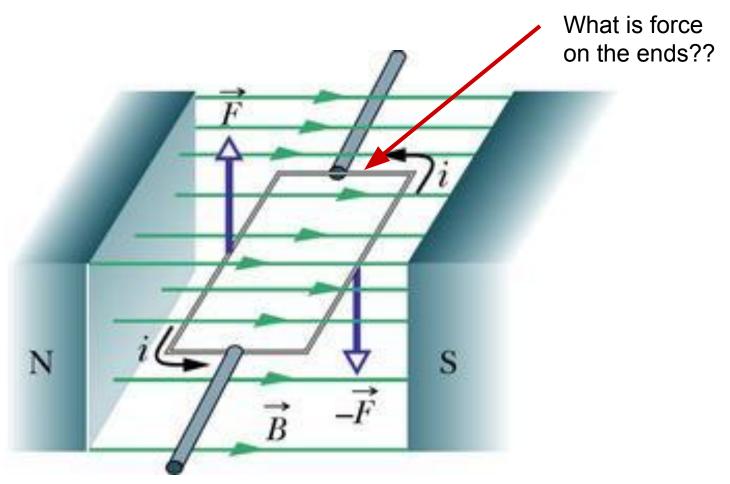
Acceleration



Don't Buy A Ticket Quite Yet..

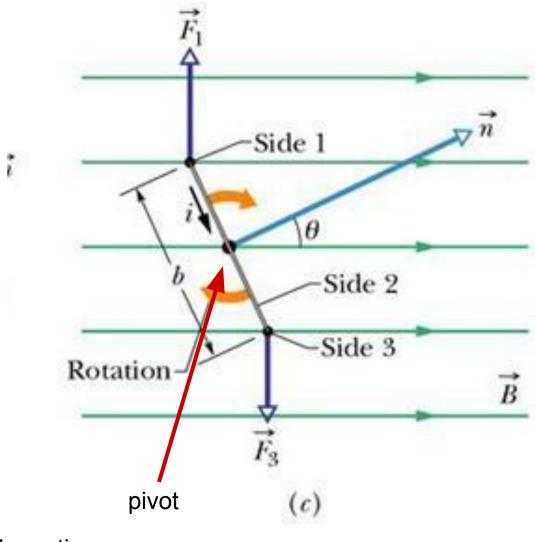
- This is still experimental.
- Much development still required.
- Some of these attempts have been abandoned because of the high cost of building a MagLev train.
 Probably 10-20 years out.
 Or More.

Current Loop



Loop will tend to rotate due to the <u>torque</u> the field applies to the loop. Magnetism 74

The Loop

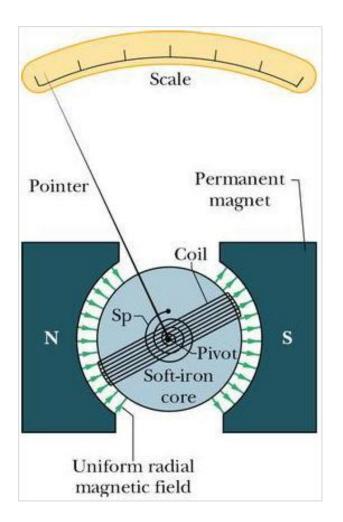


OBSERVATION

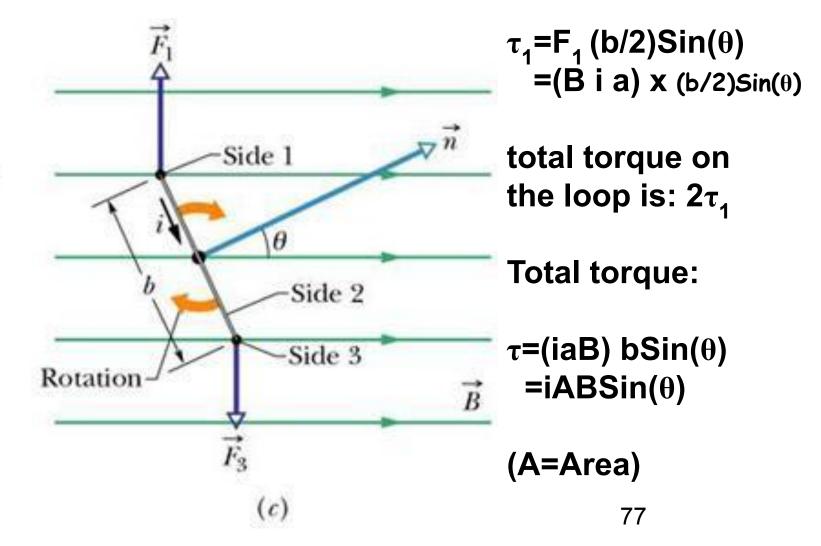
Force on Side 2 is out of the paper and that on the opposite side is into the paper. No net force tending to rotate the loop due to either of these forces.

The net force on the loop is also zero,

An Application The Galvanometer



The other sides

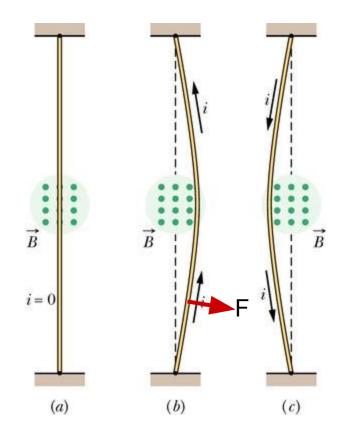


Watcha Gonna Do

- Quiz Today
- Return to Magnetic Material
- Exams not yet returned. Sorry.

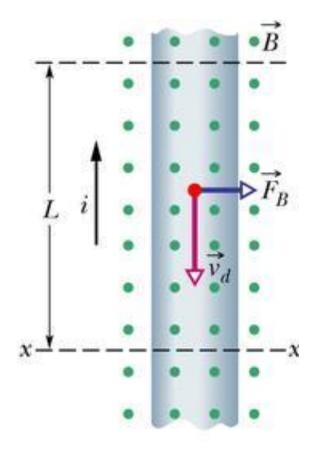
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$$q = i \times t = i \frac{L}{v_d}$$
$$F = qv_d B = i \frac{L}{v_d} v_d B = iLB$$

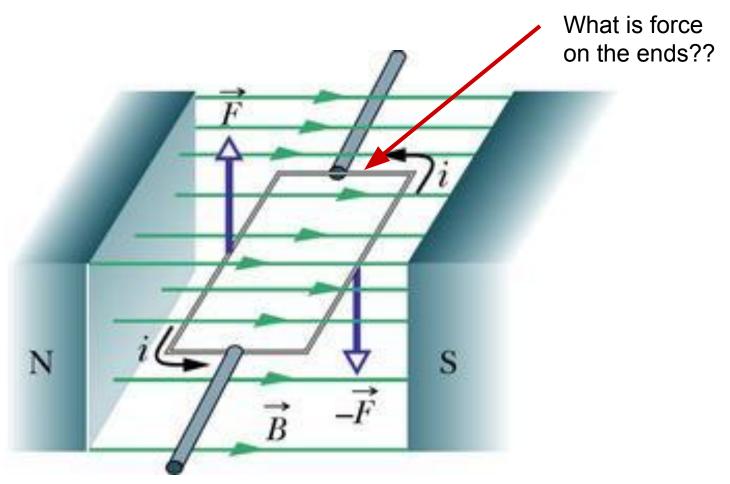
vector:

 $\mathbf{F} = i\mathbf{L} \times \mathbf{B}$

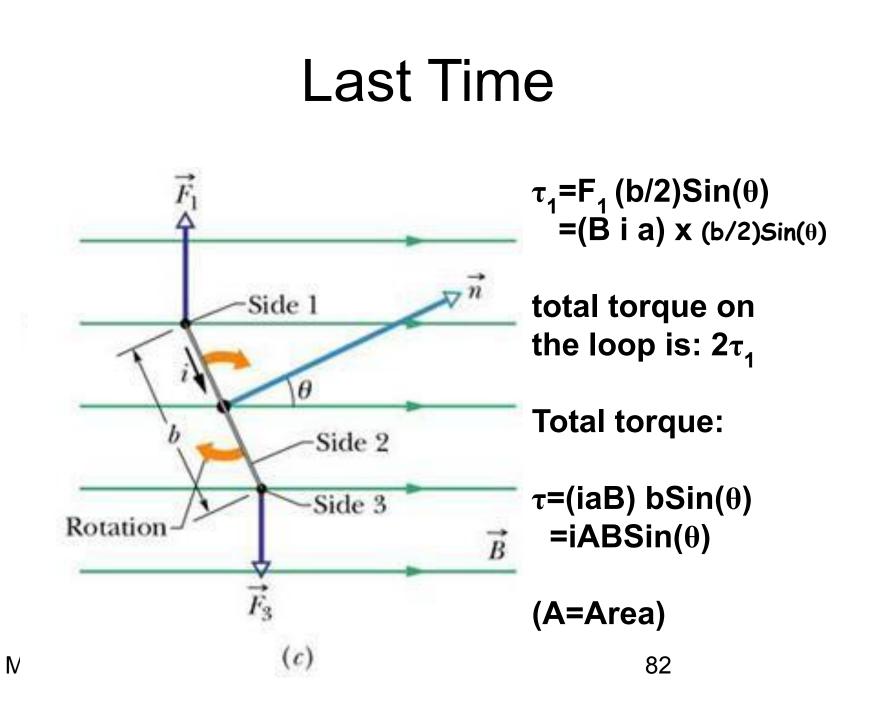
L in the direction of the motion of POSITIVE charge (i).

B out of plane of the paper Magnetism

Current Loop



Loop will tend to rotate due to the <u>torque</u> the field applies to the loop. Magnetism 81

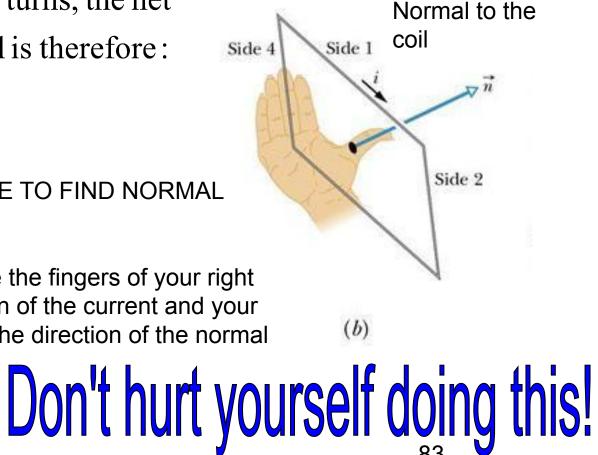


A Coil

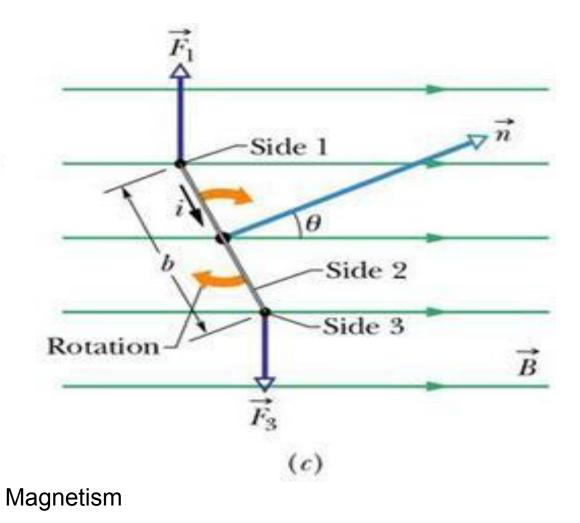
For a COIL of N turns, the net torque on the coil is therefore: $\tau = NiABSin(\theta)$

RIGHT HAND RULE TO FIND NORMAL TO THE COIL:

"Point or curl you're the fingers of your right hand in the direction of the current and your thumb will point in the direction of the normal to the coil.



Dipole Moment Definition



Define the magnetic dipole moment of the coil µ as:

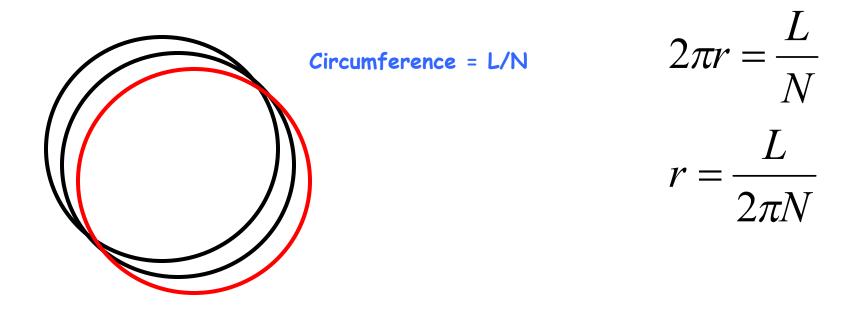
μ=NiA

We can convert this to a vector with A as defined as being normal to the area as in the previous slide.

Current Loop

 $\tau = iAB\sin\theta$ Consider a coil with N turns of wire. Define Magnetic Moment $\boldsymbol{\mu} = Ni\boldsymbol{A}$ and $\tau = \mathbf{\mu} \times \mathbf{B}$

A length L of wire carries a current *i*. Show that if the wire is formed into a circular coil, then the maximum torque in a given magnetic field is developed when the coil has one turn only, and that maximum torque has the magnitude ... well, let's see.



Problem continued...

 $\tau = NiAB$ since sin(μ , B) is maximum

when the angle is 90°

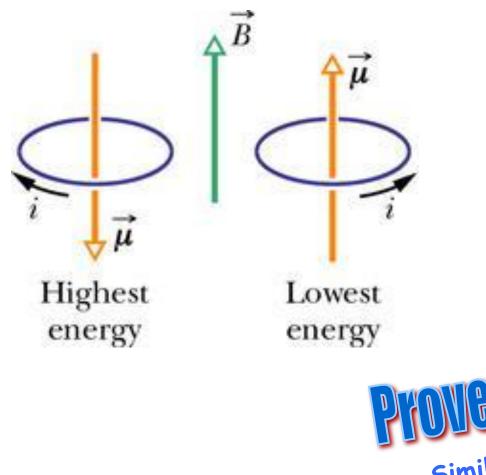
 $A = \pi r^2$

$$\tau = NiB\pi \left(\frac{L}{2\pi N}\right)^{2}$$
$$\tau = iB\pi \left(\frac{L\sqrt{N}}{2\pi N}\right)^{2} = iB\pi \frac{L^{2}}{4\pi^{2}N} \quad (BiA)$$

Maximum when N = 1 and

$$\tau = \frac{iBL^2}{4\pi}$$

Energy



Like the electric dipole $U(\theta) = -\mu \bullet \mathbf{B}$ μ and B want to be aligned!



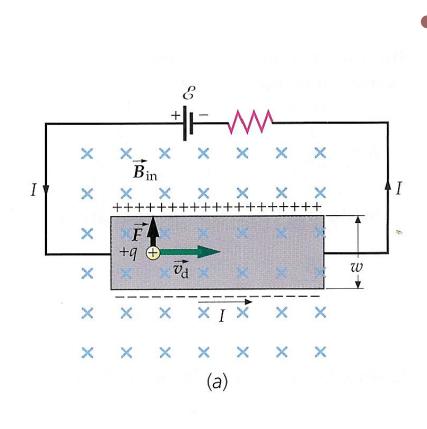
The Hall Effect

What Does it Do?

- Allows the measurement of Magnetic Field if a material is known.
- Allows the determination of the "type" of current carrier in semiconductors if the magnetic field is known.
 - Electrons

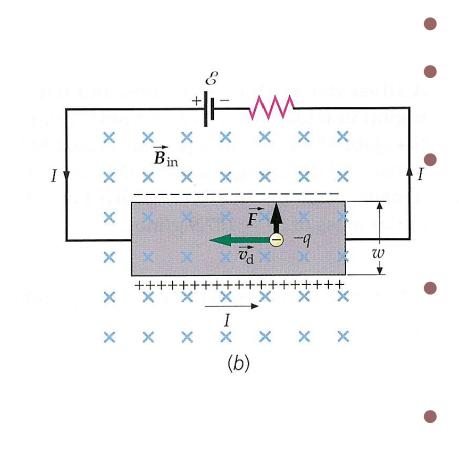
Magnetismoles

Hall Geometry (+ Charge)



- Current is moving to the right. (v_d)
 Magnetic field will force the charge to the top.
 - This leaves a deficit (-) charge on the bottom.
 - This creates an electric field and a potential difference.

Negative Carriers



- Carrier is negative.
 - Current still to the right.
 - Force pushes negative charges to the top.
- Positive charge builds up on the bottom.
- Sign of the potential difference is

Hall Math

or

 Eventually, the field due to the Hall effect will allow the current to travel un-deflected through the conductor. balance :

$$qv_d B = qE_{Hall} = q\frac{V_{Hall}}{w}$$

$$V_{Hall} = w v_d B$$

$$J = nev_d = i / A$$

$$v_d = \frac{i}{neA}$$

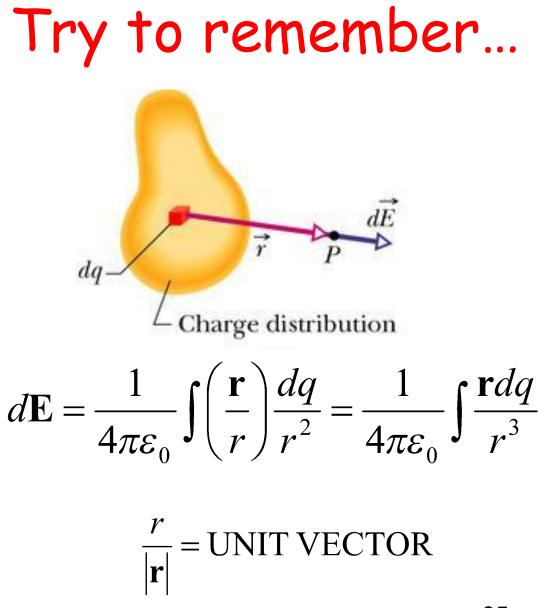
$$V_{Hall} = wv_d B = wB \frac{i}{neA}$$

$$A = wt$$

$$V_{Hall} = wB \frac{i}{newt} = \frac{iB}{net}$$

Magnetic Fields Due to Currents

Chapter 30



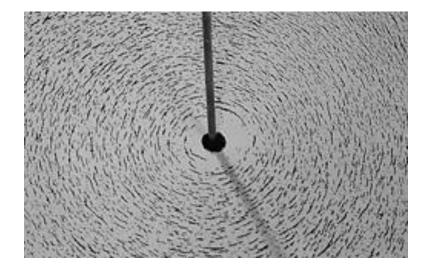
For the Magnetic Field, current "elements" create the field. This is the Law of **Biot-Savart** In a similar fashion to E field : $\frac{d\vec{B}(\text{into})}{\text{page}}\mathbf{B} = \frac{\mu_0}{4\pi} \int \frac{id\mathbf{s} \times \mathbf{r}_{unit}}{r^2} = \frac{\mu_0}{4\pi} \int \frac{id\mathbf{s} \times \mathbf{r}}{r^3}$ permeability $\mu_{0} = 4\pi \times 10^{-7} Tm / A = 1.26 \times 10^{-7} Tm$ **BY DEFINITION** Current distribution

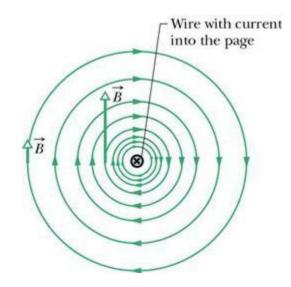
This, defines B!

Magnetic Field of a Straight Wire

- We intimated via magnets that the Magnetic field associated with a straight wire seemed to vary with 1/d.
- We can now PROVE this!

From the Past





Using Magnets

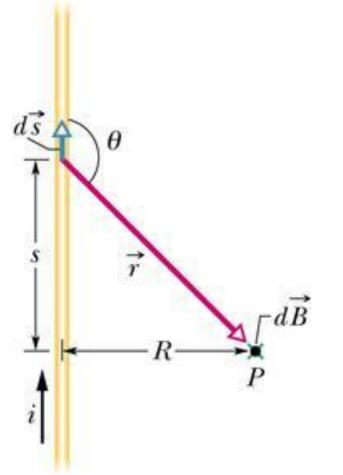
Directions: The Right Hand Rule

<u>Right-hand rule</u>: Grasp the element in your right hand with your extended thumb pointing in the direction of the current. Your fingers will then naturally curl around in the direction of the magnetic field lines due to that element.

Magnetism

(b)

Let's Calculate the FIELD



Note: For ALL current elements d**s** X **r**

is into the page

The Details

$$dB = \frac{\mu_0}{4\pi} \frac{ids\sin(\theta)}{r^2}$$

Negative portion of the wire contributes an equal amount so we integrate from 0 to ∞ and DOUBLE it.

$$B = \frac{\mu_0 i}{2\pi} \int_0^\infty \frac{\sin(\theta) ds}{r^2}$$

Magnetism

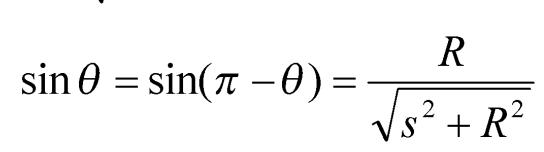
dB

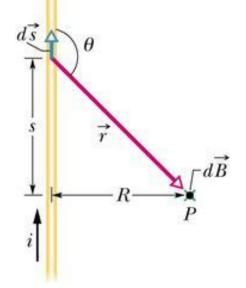
 $d\vec{s}$

Moving right along

$$r = \sqrt{s^2 + R^2}$$

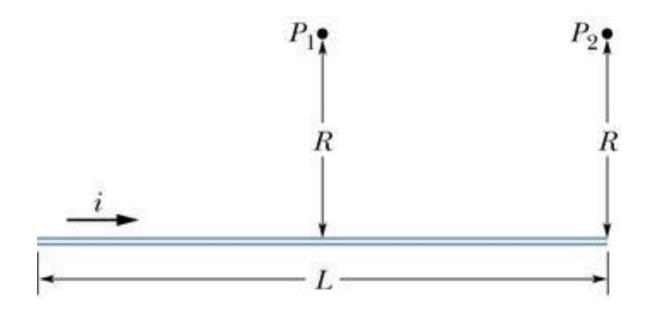
So



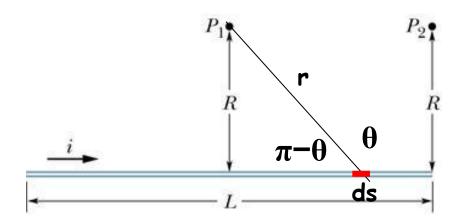


$$B = \frac{\mu_0 i}{2\pi} \int_0^\infty \frac{r ds}{\left(s^2 + R^2\right)^{3/2}} = \frac{\mu_0 i}{2\pi R} \int_0^{1/2} d$$

A bit more complicated A finite wire



P₁



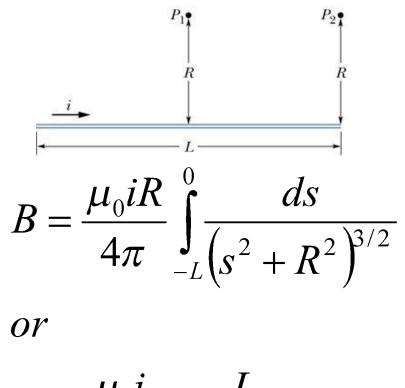
NOTE : $sin(\theta) = sin(\pi - \theta)$ $ds \times r = ds r \sin(\theta)$ $\sin(\theta) = \frac{R}{-}$ $dB = \frac{\mu_0 i}{4\pi} \frac{ds \sin(\theta)}{r^2}$ $r = \left(s^2 + R^2\right)^{1/2}$

Magnetism

More P₁ $B = \frac{\mu_0 i}{4\pi} \int_{-L/2}^{+L/2} \frac{ds}{\left(s^2 + R^2\right)^{3/2}}$ and $B = \frac{\mu_0 i}{2\pi R} \frac{L}{\sqrt{L^2 + 4R^2}}$ when $L \Longrightarrow \infty$. $\mathbf{B} \Longrightarrow \frac{\mu_0 \mathbf{i}}{2\pi R}$

Magnetism

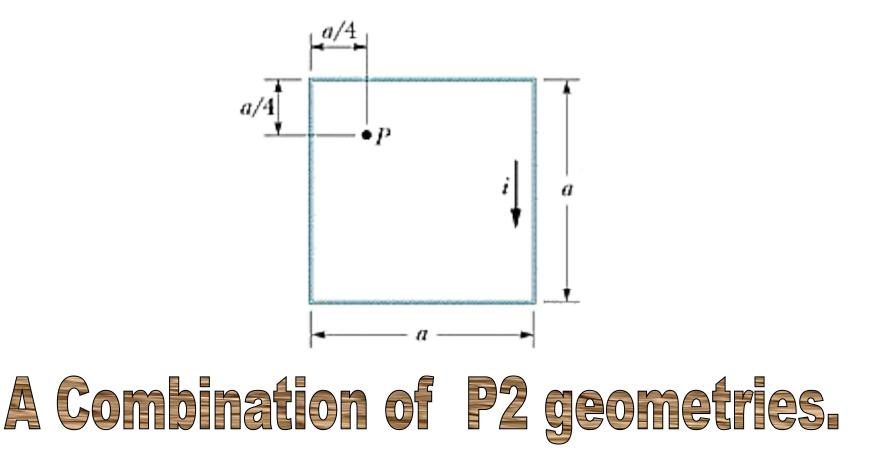
P2



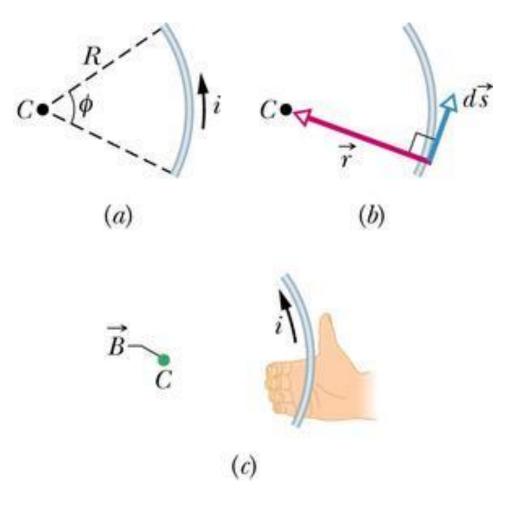
$$B = \frac{\mu_0 i}{4\pi R} \frac{L}{\sqrt{s^2 + R^2}}$$

Magnetism

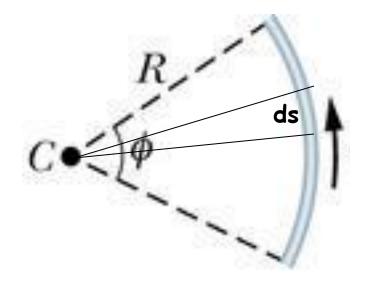
APPLICATION: Find the magnetic field B at point P in for i = 10 A and a = 8.0 cm.



Circular Arc of Wire



More arc...

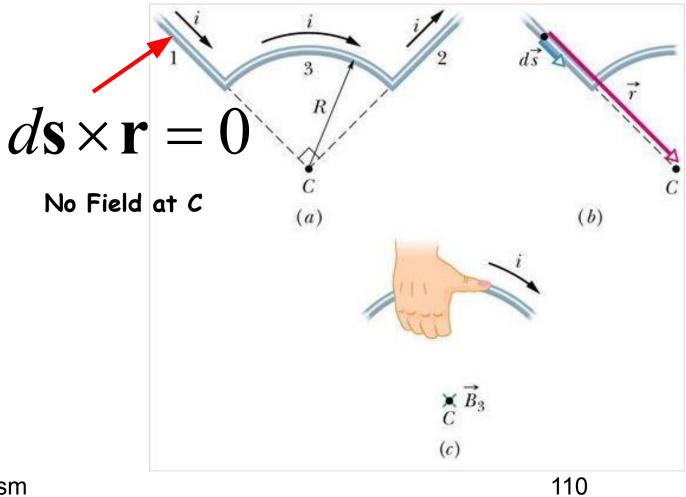


 $ds = Rd\phi$ $dB = \frac{\mu_0}{\Delta \pi} \frac{ids}{R^2} = \frac{\mu_0}{\Delta \pi} \frac{iRd\phi}{R^2}$ $B = \int dB = \int_{0}^{\phi} \frac{\mu_0}{4\pi} \frac{iRd\phi}{R^2} = \frac{\mu_0 i}{4\pi R} \int_{0}^{\phi} d\phi$ $B = \frac{\mu_0 i \phi}{4\pi R}$ at point C

Magnetism

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Howya Do Dat??



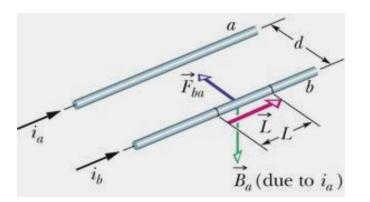
Force Between Two Current Carrying Straight Parallel Conductors

Wire "a" creates a field at wire "b'

 \vec{B}_a (due to i_a)

Current in wire "b" sees a force because it is moving in the magnetic field of "a". 111

The Calculation



The FIELD at wire "b" due to

wire "a" is what we just calculated :

$$B_{\text{at "b"}} = \frac{\mu_0 i_a}{2\pi d}$$

$$F_{\text{on "b"}} = i_b \mathbf{L} \times \mathbf{B}$$

Since **L** and **B** are at right angle

Since L and B are at right angles...

$$\mathbf{F} = \frac{\mu_0 L i_a i_b}{2\pi d}$$

Definition of the Ampere

The force acting between currents in parallel wires is the basis for the definition of the ampere, which is one of the seven SI base units. The definition, adopted in 1946, is this: The ampere is that constant current which, if maintained in two straight, parallel conductors of infinite length, of negligible circular cross section, and placed 1 m apart in vacuum, would produce on each of these conductors a force of magnitude 2 \times 10-7 newton per meter of length.

TRANSITION

AMPERE

Welcome to Andre' Marie Ampere's Law

Normally written as a "circulation" vector equation. We will look at another form, but first...

Remember GAUSS'S LAW??

 $\oint \mathbf{E} \bullet d\mathbf{A} = \frac{q_{enclosed}}{c}$ \mathcal{E}_{0} Surface Integral

Gauss's Law

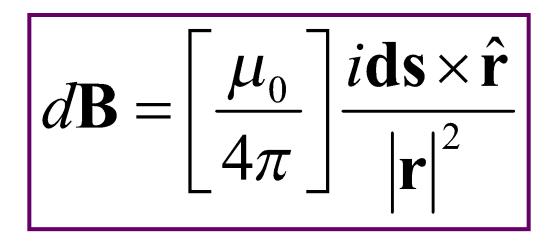
- Made calculations easier than integration over a charge distribution.
- Applied to situations of HIGH SYMMETRY.
- Gaussian SURFACE had to be defined which was consistent with the geometry.
- AMPERE'S Law is the Gauss' Law of Magnetism! (Sorry)

The next few slides have been lifted from **Seb Oliver** on the internet

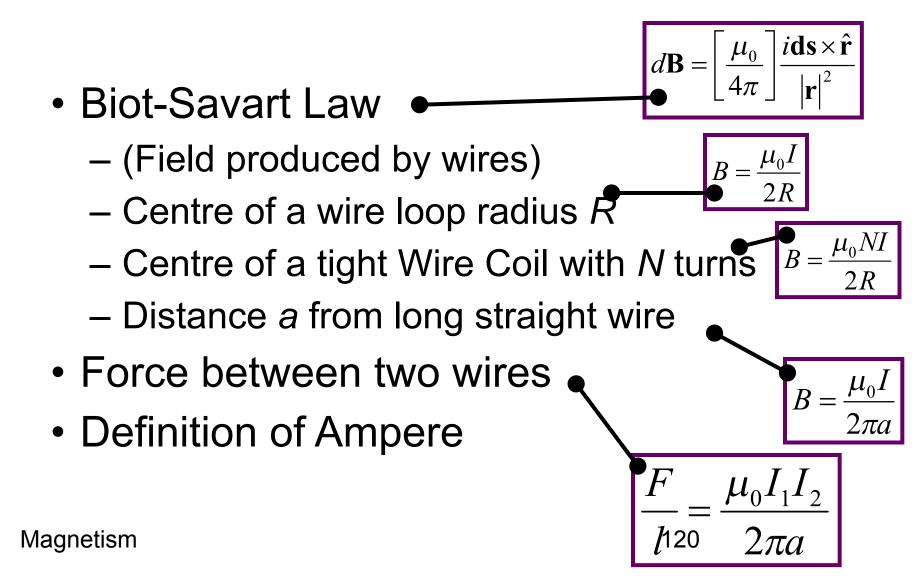
Whoever he is!

Biot-Savart

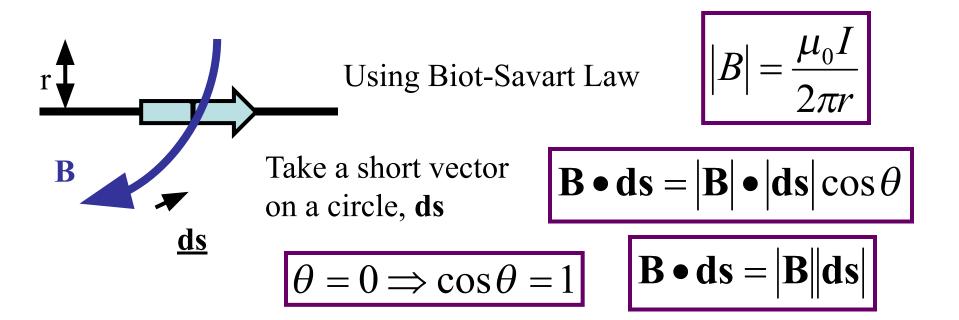
• The "Coulombs Law of Magnetism"



Invisible Summary



Magnetic Field from a long wire



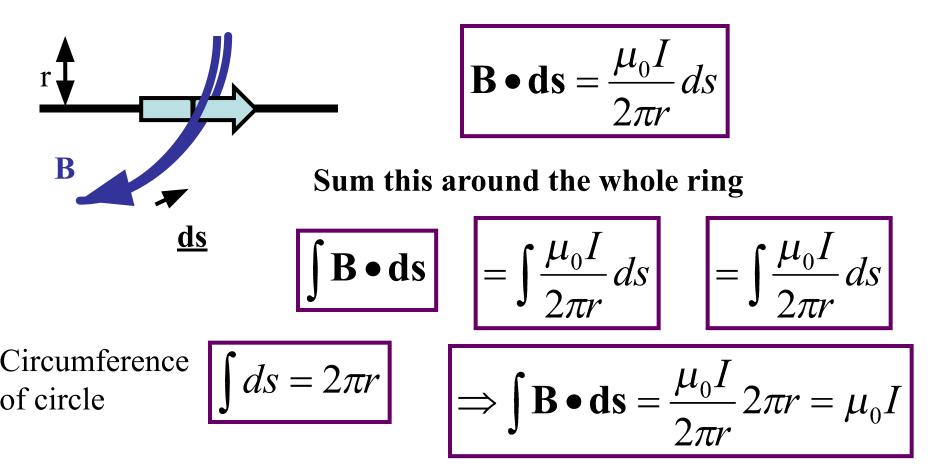
Thus the dot product of **B** & the short vector **ds** is:

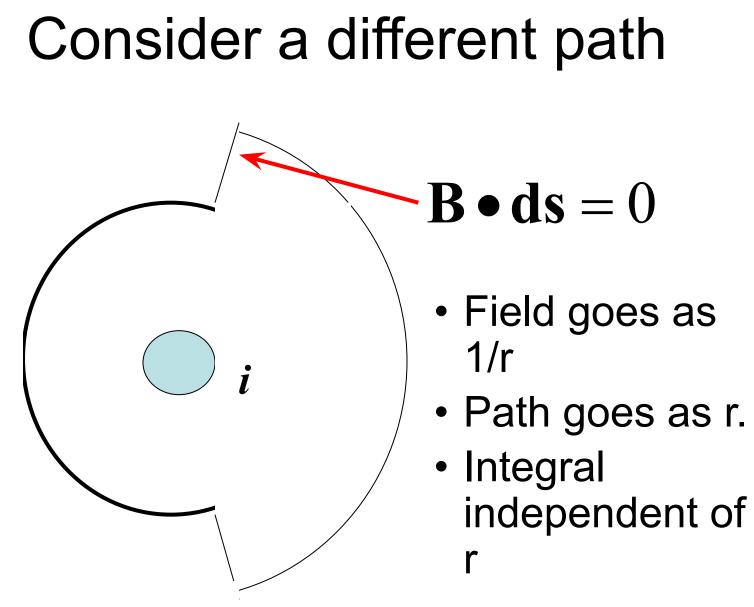
$$\mathbf{B} \bullet \mathbf{ds} = \frac{\mu_0 I}{2\pi r} ds$$

Magnetism

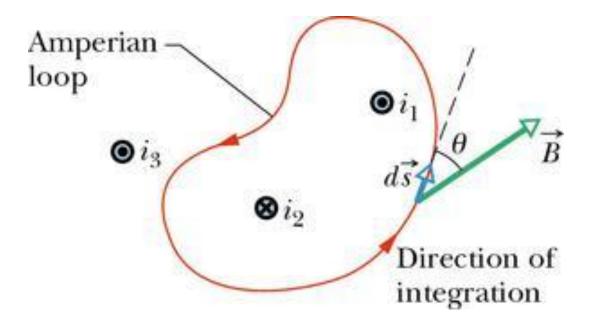
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Sum B'ds around a circular path



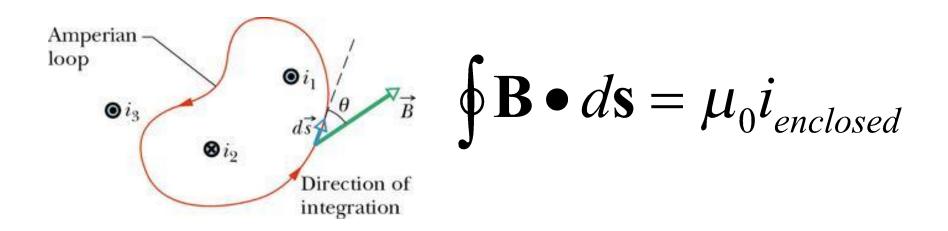


SO, AMPERE'S LAW by SUPERPOSITION:



We will do a LINE INTEGRATION Around a closed path or LOOP.

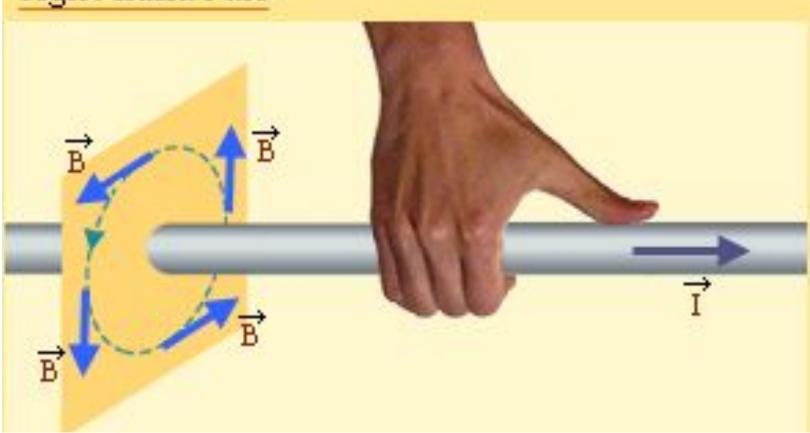
Ampere's Law



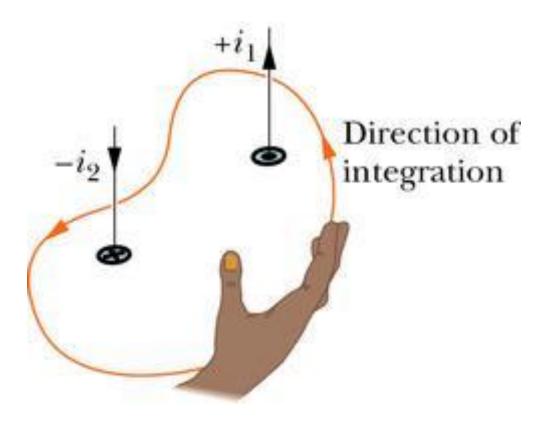
USE THE RIGHT HAND RULE IN THESE CALCULATIONS

The Right Hand Rule

right-hand rule



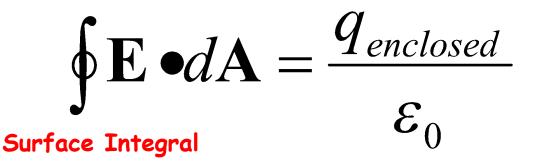
Another Right Hand Rule



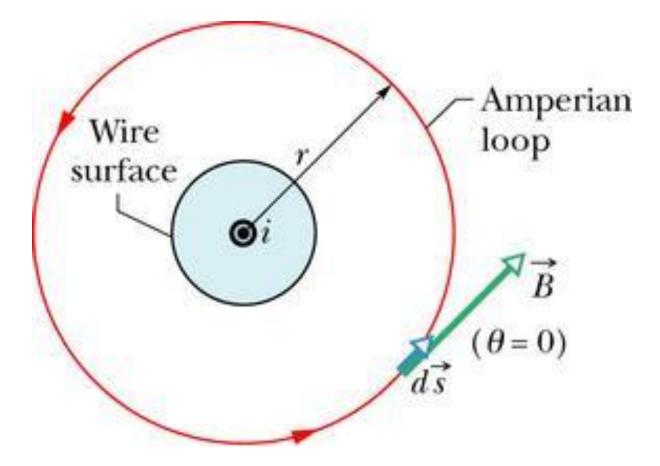
COMPARE

 $\oint \mathbf{B} \bullet d\mathbf{s} = \mu_0 i_{enclosed}$

Line Integral

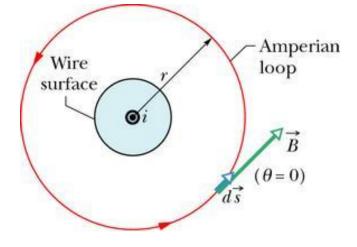


Simple Example



Field Around a Long Straight Wire

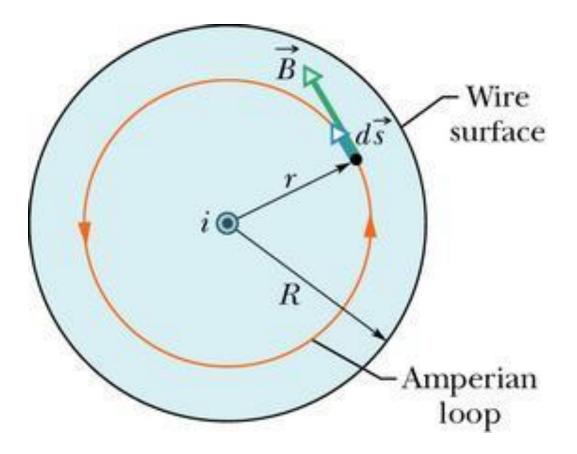
$$\oint \mathbf{B} \bullet d\mathbf{s} = \mu_0 i_{enclosed}$$



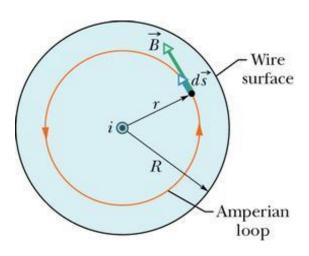
$$B \times 2\pi r = \mu_0 i$$

$$B = \frac{\mu_0 i}{2\pi r}$$

Field INSIDE a Wire Carrying UNIFORM Current

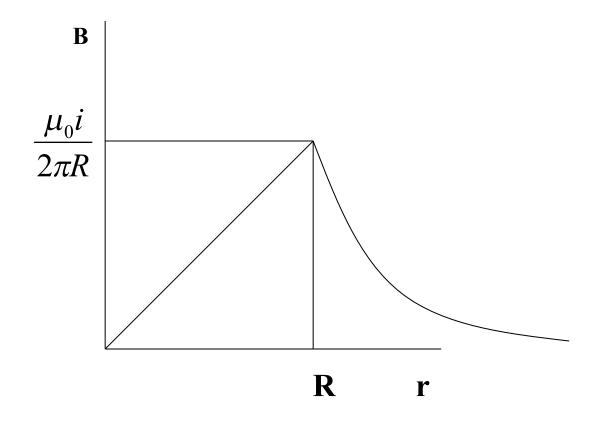


The Calculation



$$\oint \mathbf{B} \bullet d\mathbf{s} = B \oint ds = 2\pi r B = \mu_0 i_{enclosed}$$

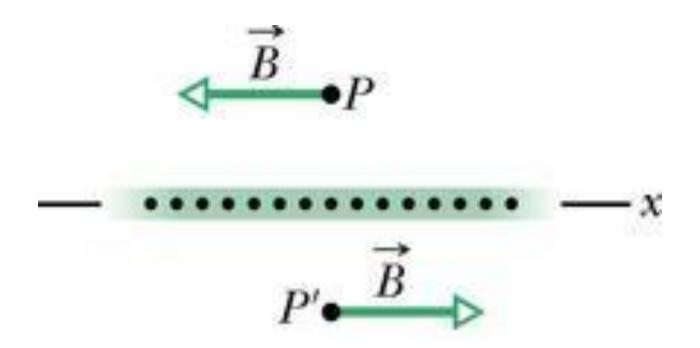
$$i_{enclosed} = i \frac{\pi r^2}{\pi R^2}$$
and
$$B = \left(\frac{\mu_0 i}{2\pi R^2}\right) r$$

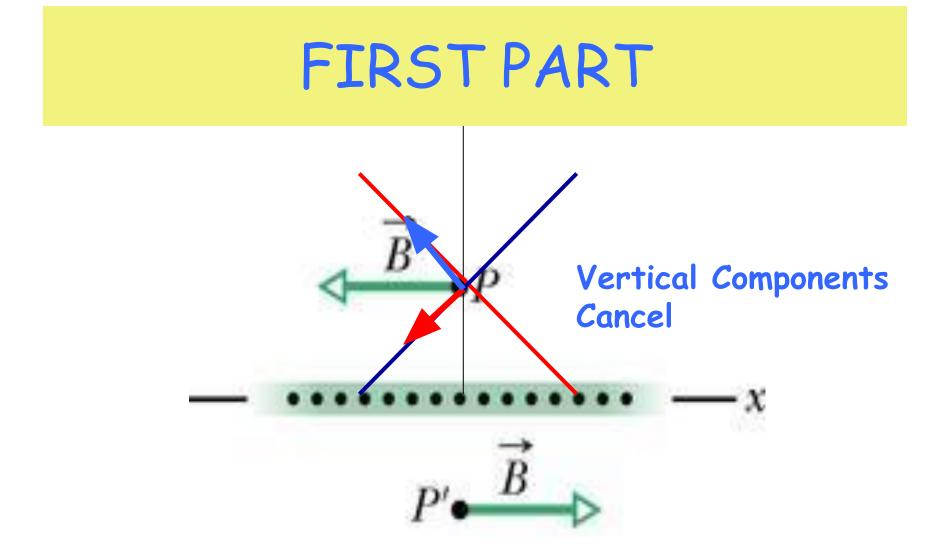


Procedure

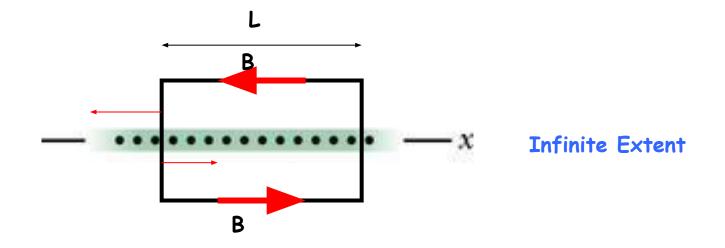
- Apply Ampere's law only to highly symmetrical situations.
- Superposition works.
 - Two wires can be treated separately and the results added (VECTORIALLY!)
- The individual parts of the calculation can be handled (usually) without the use of vector calculations because of the symmetry.
- THIS IS SORT OF LIKE GAUSS'S LAW
 WITH AN ATTITUDE!

The figure below shows a cross section of an infinite conducting sheet carrying a current per unit x-length of l; the current emerges perpendicularly out of the page. (a) Use the Biot-Savart law and symmetry to show that for all points P above the sheet, and all points P' below it, the magnetic field B is parallel to the sheet and directed as shown. (b) Use Ampere's law to find B at all points P and P'.

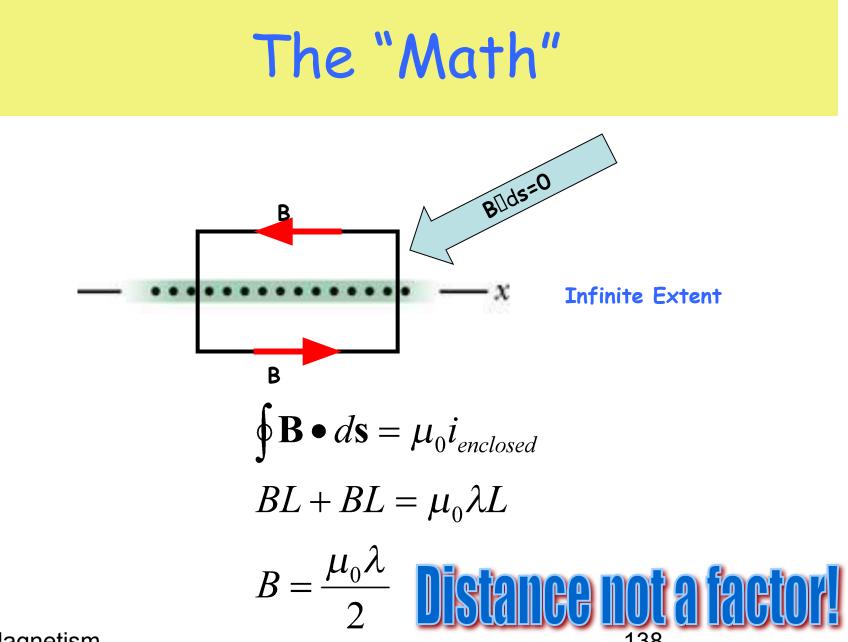




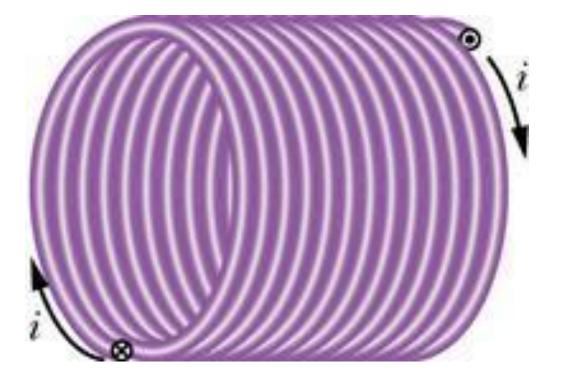
Apply Ampere to Circuit



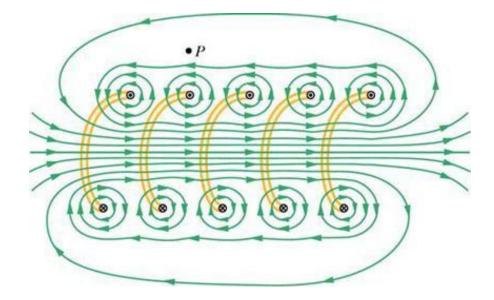
 λ = current per unit length Current inside the loop is therefore : $i = \lambda L$



A Physical Solenoid



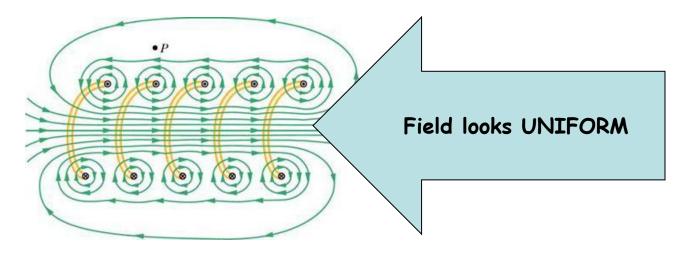
Inside the Solenoid



For an "INFINITE" (long) solenoid the previous problem and SUPERPOSITION suggests that the field OUTSIDE this solenoid is ZERO!

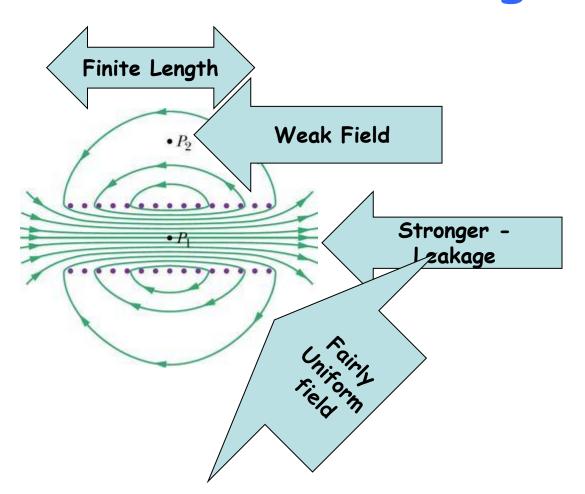
More on Long Solenoid

Field is ZERO!

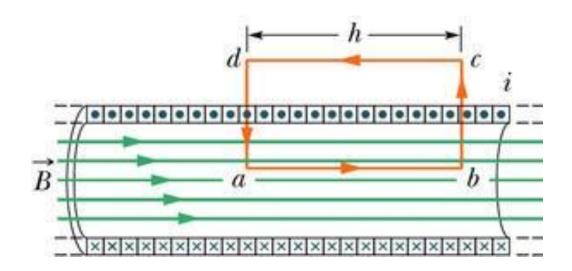


Field is ZERO

The real thing.....



Another Way

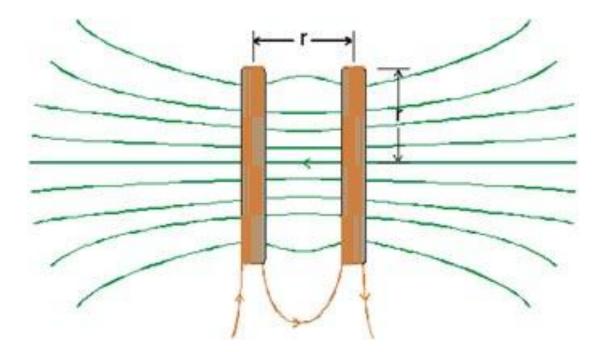


Ampere : $\oint \mathbf{B} \bullet d\mathbf{s} = \mu_0 i_{enclosed}$ $0h + Bh = \mu_0 nih$ $B = \mu_0 ni$

Application

- Creation of Uniform Magnetic Field Region
- Minimal field outside
 - except at the ends!





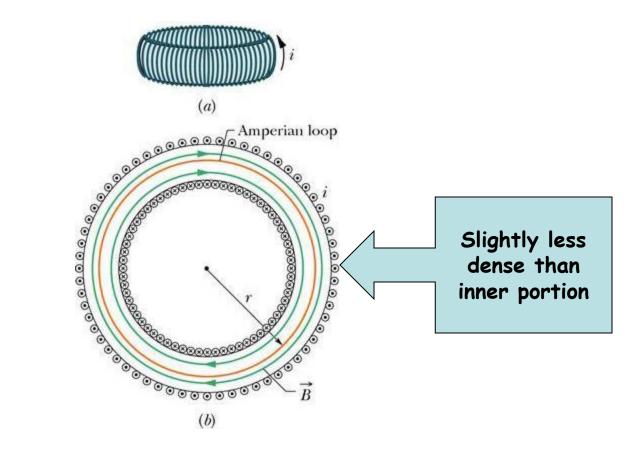
"Real" Helmholtz Coils



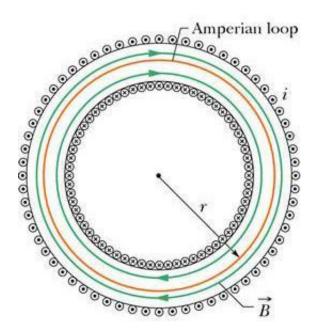
Used for experiments.

Can be aligned to cancel out the Earth's magnetic field for critical measurements.

The Toroid



The Toroid



Ampere again. We need only worry about the INNER coil contained in the path of integration : $\oint \mathbf{B} \bullet d\mathbf{s} = B \times 2\pi r = \mu_0 Ni \text{ (N} = total \# \text{ turns)}$ so $B = \frac{\mu_0 Ni}{2\pi r}$